ABSTRACT

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Computer programming is a particularly apt and well-explored domain for Intelligent Tutoring Systems (ITSs). Central to the success of a programming ITS is the code understanding system. This thesis explores the possibility of using dynamically constructed Bayes nets (DCBNs) to understand student coding actions. DCBNs use the observed evidence to heuristically limit instantiation of the Bayes net to only the relevant portion.

Prior work has applied DCBNs to sketch recognition and story understanding. The code understanding system described in this work develops heuristics for the domain of Java™ code understanding and adds two main extensions to the technique. First, support has been added for the alteration of prior evidence to allow for student editing of earlier code. Second, a heuristic has been proposed and tested for the construction of Bayes nets when all the evidence is not equally informative (e.g., the “;” token is less discriminative than the “for” token).

The DCBN-based code understanding system was evaluated against a top-down recursive descent parser and a minimum edit distance approach. It was found that, although the system performed as well as the minimum edit distance baseline and prior DCBN intent recognition systems (i.e., Wimp3), and could support a fine-grained student model, the unpredictable behavior, variable execution time and high implementation cost/complexity make a DCBN-based code understanding system unsuitable for integration into an ITS.
Code Understanding for an Intelligent Tutoring System

by
Robert Phillips

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APPROVED BY:

______________________________
Dr. James C. Lester
Committee Chair

______________________________
Dr. Jon Doyle

______________________________
Dr. Dennis Bahler
DEDICATION

To Lily, Catherine and Jonathan.
BIOGRAPHY

Robert Phillips graduated from Harvard University magna cum laude in 1990. He then pursued a year of post-Baccalaureate studies at Columbia University before joining Numerical Design Ltd.—a small 3D computer graphics software development firm. While there, he helped develop the r+ photo-realistic rendering package and the NetImmerse 3D game engine. In 2003, he joined Applied Research Associates, Inc. and in 2004 began graduate studies at North Carolina State University.
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CHAPTER 1
Introduction

Human tutoring has a long history in education and has been shown to be very effective. Bloom’s studies of human tutors (Bloom, 1984) showed expert human tutoring resulted in excellent learning gains (i.e., tutored students performed two standard deviations better than control students) and reduced learning differences (i.e., 90% of the tutored students performed as well as the top 20% of the control students). Additionally, human tutoring was shown to improve student affect including attitude towards learning, interest and motivation (Anania, 1983). Unfortunately, human tutoring is expensive and cannot scale effectively to a large number of students.

Intelligent Tutoring Systems (ITSs) are a product of educational theory, Artificial Intelligence (AI), and computer-human factors and attempt to provide the benefits of human tutoring to an unlimited number of students. ITSs have been developed for a wide variety of domains (e.g., ITSpoke for physics (Litman & Silliman, 2004), AutoTutor for physics and computer literacy (Graesser, Jackson, Mathews, Mitchell, Olney, Ventura, Chipman, Franceschetti, Hu, Louwerse, & Person, 2003), CIRCSIM-Tutor for blood pressure (Evens, Brandle, Chang, Freedman, Glass, Lee, Shim, Woo, Zhang, Zhou, Michael & Rovick, 2001) and the Geometry Explanation Tutor for mathematics (Aleven, Koedinger & Popescu, 2003)) and have yielded impressive cognitive and affective results. In several studies (Graesser et al., 2003; VanLehn, Lynch, Schulze, Shapiro, Shelby, Taylor, Treacy, Weinstein &
Wintersgill, 2005; Anderson, Corbett, Koedinger & Pelletier, 1995), ITSs have been shown to provide about a one standard deviation improvement in learning.

As a subject dear to the hearts of computer scientists, it should not be surprising that programming has been a popular domain for ITSs. Computer programming is a difficult skill to acquire, has been well studied educationally, has a wealth of supporting tools and technology (e.g., parsing tools and development environments) and is in high demand. All these features make programming an attractive domain for ITSs.

To improve learning and keep students motivated, an ITS (programming or otherwise) must provide effective interactions with students. To achieve this, ITSs generally consist of six main components (see Figure 1). First, the natural language understanding (NLU) module converts student queries to a format the ITS can process. In parallel, for task oriented domains, the action tracking module interprets student actions, informs the dialog manager and updates the student model. Next, the dialog manager (DM) interacts closely with the pedagogical planner and handles conversational pragmatics (e.g., grounding, adjacency pairs, and so on). The student model represents the student’s knowledge and emotional state, is usually based on the system’s underlying educational and affective theory and incorporates the domain knowledge. The pedagogical planning (PP) module monitors the student’s cognitive and affective state and determines the next most suitable tutorial action. Finally, the natural language generation (NLG) module generates tutor responses or queries and is often template-driven. This work will focus on the development and evaluation of the action tracking module which, for a programming ITS, is the code understanding system.
A programming ITS’s code understanding system must provide sufficiently detailed information to allow effective tracking of and response to student actions. In solving this problem, code understanding systems have generally varied with respect to four main parameters: the range of accepted input (i.e., how much variability in the student solution is allowed), the level of interactivity (i.e., token-by-token vs. sub-routine at a time), the implementation complexity and the granularity of the information provided to the student model. For example, the PROUST system (Johnson, 1986) supported a wide range of input in the form of a compileable subroutine but used a complex plan-based recognition system. LISP Tutor (Anderson & Reiser, 1985), on the other hand, greatly constrained the student’s input but performed a token-by-token tracking of student actions. It, too, used a very complex plan-based recognition system, but performed some pre-compilation to accelerate tracking. Both systems supported a very fine-grained model of the student’s programming knowledge. From prior observation of human tutors (Boyer, Phillips, Wallis, Vouk, & Lester, 2008), it appears a desirable code understanding system should accept a wide range of input (i.e., partial, buggy and un-compileable code), and provide incremental real-time token-by-
token tracking of student actions. Ideally, the code understanding system should also be
reasonable to implement and support a fine-grained student model.

As a motivating example, consider the code in Figure 2—a composite of student
errors seen in our training set. Here the student has used a “while” keyword instead of a “for”
and replaced the semi-colons with commas. To match human tutoring behavior, a code
understanding system must be able to accept such buggy and incomplete input even though it
isn’t compileable. In the “while” for “for” case, the human tutor often intervened early once
the student began coding the test clause of the for loop. For an ITS to replicate this behavior,
the code understanding system cannot wait until the code is compileable. For the “,” for “;”
bug the human tutor would often wait until the student attempted to compile the code before
intervening. To mimic this behavior the code understanding system must be able to ignore
some errors while still providing the most probable interpretation at any given step (e.g.,
allowing the system to remediate the hard coded loop limit).
To meet the desired requirements of a programming ITS’ code understanding system (i.e., accept a wide range of input, provide token-by-token tracking, be reasonable to implement and support a fine-grained student model), this thesis explores the use of Dynamically Constructed Bayes Nets (DCBNs) (Alvarado, 2004). In this approach, as evidence (i.e., a token) is added, the code understanding system heuristically alters a Bayes net representing the student’s program. The heuristic construction focuses the recognition/understanding problem on hypotheses for which there is reasonable evidence (vs. just trying all hypotheses) while Bayes net inference allows competing hypotheses to influence each other. This approach promises to support a wide range of input due to the flexibility of Bayes nets, while permitting real-time token-by-token tracking due to
aggressive pruning of the Bayes net. Additionally, the implementation time and complexity should be similar to other code understanding systems (e.g., PROUST and LISP Tutor), while higher-level Bayes net hypotheses and the linking of each Bayes net fragment to a portion of the student’s knowledge should enable a fine-grained student model.

The next section (Chapter 2) will describe the proposed code understanding system. Chapter 3 will then provide a quantitative and qualitative evaluation of its performance, while Chapter 4 will cover related work in programming ITSs, code understanding, graphical models, and compilers. A discussion of the results will follow in Chapter 5 with Chapter 6 providing a conclusion.
CHAPTER 2

DCBNs for Code Understanding

This thesis documents the development and implementation of a Java™ code understanding system to evaluate the applicability of DCBNs. The developed system repurposes Alvarado and Davis’ DCBN architecture (Alvarado & Davis, 2005) to support code understanding instead of sketch recognition. The following discussion will present the implemented system and point out how it differs from Alvarado and Davis’ approach.

Example

To better illustrate the operation of the DCBN-based code understanding system, the running example of the student typing the code “a=0;” will be used. The Bayes nets resulting from each stage in this process are shown in Figure 4 through Figure 11.

Figure 3 provides a key for interpreting the Bayes nets. Each ellipse represents a Bayes net node, with the associated label being either the rule name or token it represents. Below and to the right of each node is listed the probability of the node followed by a colon, and then if the node is parentless, its prior probability, but if the node is a child, then the leak probability. This leak probability is used to represent the likelihood that some hypothesis not present in the Bayes net could have caused the associated node. Each child arrow out of a node is labeled with the causal strength (i.e., the probability that the parent could cause the child independent of all other possible causes). Note that the Bayes nets used by the DCBN system exclusively employ Noisy OR nodes. These canonical causal relations only require the causal strengths of the parents rather than a full conditional probability table – greatly
reducing the number of probabilities required to fully specify the joint distribution. Finally, each node is color coded by its probability. Strongly believed nodes are fully saturated green, while low probability nodes are black.

Figure 3. Explanation of Bayes net figures.

Figure 4 shows the Bayes net after the initial “a” identifier has been added but before pruning. The “a” token (lower-left corner) has spawned a parent Identifier hypothesis. Although the Identifier hypothesis has two parents, there are other possible causes that have not been added to the Bayes net. To compensate for this probabilistically, a leak probability (0.03) has been added to the Identifier hypothesis. Of the Identifier hypothesis’ two parents, one is strongly believed (i.e., the idOrClassRef hypothesis with a belief of .71), while the other is very weak (i.e., the variableDeclaratorId with a belief of .031). In this case, the weaker hypothesis will be pruned away since it is below a threshold of the stronger hypothesis’ belief. When the variableDeclaratorId node is pruned away, so too will its parent and both of their children, since without the variableDeclaratorId node they will all lack any supporting evidence. By way of comparison, the primary node in the upper right
quadrant also has two parents, but since the probabilities are so similar (i.e., .078 and 0.11) neither one can be pruned away. This likelihood-based pruning can be seen as a harsher form of the Bayes nets’ explaining away phenomena. If one hypothesis is obviously not a viable candidate, it is just removed from the net. Figure 5 shows the initial Bayes net after pruning. The leak probability of the Identifier node does not change since (as will be discussed more later) parents that are pruned away are not allowed to add their causal strength in absentia.

Figure 4. Bayes net after the student types the initial “a” identifier but before pruning.
Figure 5. Bayes net after the student types the initial “a” identifier and after pruning.

Figure 6 shows the state of the Bayes net after the “=“ operator has been added but before pruning has occurred. In this Bayes net, the “=“ token has spawned an assignmentOperator hypothesis and a hypothesis that it is part of the optional initialization portion of a variable declaration (i.e., the “R75_sub0 node). The assignmentOperator hypothesis has recursively created an sExpression1Rest hypothesis (i.e., that the assignment operator is part of an assignment expression). This sExpression1Rest hypothesis is prevented from recursively generating more hypotheses because one of its required children (sExpression2) is not supported by any evidence. As in Figure 4, the R75_sub0 hypothesis will be pruned because its likelihood is far less than its competing parent (i.e., the assignmentOperator hypothesis). Figure 7 shows the Bayes net after this pruning step.
Figure 6. Bayes net after the student types the “a” identifier and “=” operator but before pruning.
Figure 7. Bayes net after the student types the “a” identifier and “=” operator and after pruning.

Figure 8 shows the Bayes net after the student has added the “0” integer literal but before pruning. In this case, the integer literal has completed the sExpression2 hypothesis, allowing the sExpression1Rest hypothesis to recursively generate parent hypotheses. One of these parents incorporates the idOrClassRef hypothesis and then continues recursively generating up to the R159_sub0 level. This hypothesis represents a collection of blockStatements. Note that while the causal strength for the first blockStatement is 1.0, the second blockStatement’s causal strength is only .25. This results from the fact that blocks usually consist of only one or two statements for the selected problem. The causal strengths are computed from the development portion of the corpus and thus reflect the quick drop off in probability for multiple blockStatements.
Figure 8. Bayes net after the student types the “a” identifier, “=” operator and “0” integer literal but before pruning.

Figure 9 shows the Bayes net for “a = 0” after pruning. The node labeled “; - 0” is a proposed evidence node. Such nodes represent tokens the system believes the student will type in the future. When the actual semi-colon token is added in Figure 10, it greedily replaces the proposed evidence, orphaning it. It is pruned away in Figure 11, leaving the final Bayes net interpretation. In this case, due to the simplicity of the problem and lack of ambiguity, only the correct abstract syntax tree remains. For a non-toy example, the Bayes net would be much more complicated.
Figure 9. Bayes net after the student types the “a” identifier, “==” operator and “0” integer literal and after pruning.
Figure 10. Bayes net after the student types the “a” identifier, “=” operator, “0” integer literal and “;” but before pruning.
DCBNs for Code Understanding

Reapplying SketchREAD’s DCBN-based architecture to code understanding required many modifications. For their sketch recognition domain, Alvarado and Davis used a hierarchical description of the shapes for their knowledge base, which needed to be changed to address Java™ programming. The low-level constraints had to be changed, from the geometric ones used for sketch recognition to ones more suited to code understanding (e.g., distance between tokens). Heuristics had to be added to support the modification of an
existing artifact (since students frequently return and alter earlier written code) and to deal
with evidence of varying importance (i.e., the “;” and “)” tokens are less informative than the
“for” and “if” tokens). Finally, SketchREAD’s limitation that shapes cannot be recursive had
to be removed since many programming language grammars require recursion.

**Knowledge base.** The knowledge base used for the implemented code understanding
system is a simplified grammar for the Java™ language. This grammar was derived from
Java™ grammar. The simplified grammar was created by removing productions not required
to parse the development corpus, followed by a reduction of the grammar’s hierarchical
structure (especially with regard to expressions) to reduce the depth of the generated Bayes
net. This simplification step was taken to simplify development of the DCBN algorithm and
reduce its execution time.

The grammatical rules allow the DCBN system to “understand” the student’s code at
the grammatical level. Were this work taken further, PROUST-like intent recognition rules
(e.g., a running-count iterator pattern) would be added to form an additional layer of
hypotheses on top of the grammar-derived ones. Additionally, a layer of student knowledge
rules could be added to map from both the grammatical and intent recognition levels to the
student model. Finally, rules or knowledge derived from the specific problem the students
were solving could then help guide the system’s understanding of the individual problem’s
code.

**Constraints.** To evaluate the suitability of different shape arrangements,
SketchREAD employed several geometric constraints. For code understanding, these
geometric constraints have been replaced with lexical order and lexical distance constraints. When new evidence or hypotheses are added to the Bayes net, a topological sort (Cormen, Leiserson, Rivest, & Stein, 2001) is applied, using the parent-child relations and order of the tokens in the student’s code as constraints. This yields a consistent numbering of all the nodes in the Bayes net. The numbers from the evidentiary nodes (i.e., tokens) are then propagated throughout the graph, updating each node’s range of evidentiary support. This evidentiary support range is used in several ways to reduce the number of combinations considered in the Bayes net construction process.

**Bayes net construction heuristics.** Although the core of Alvarado and Davis’ Bayes net construction process remains the same, updating it to the code understanding domain required several new heuristics to both deal with the new domain and address limitations in Alvarado and Davis’ approach.

**Slot filling.** A first alteration in the Bayes net construction process was the use of the evidence numbering and evidentiary support system to constrain hypothesis generation.

When filling slots in a grammar rule’s hypothesis, the selected slot fillers were required to have a consistent left to right ordering. This greatly reduced the number of combinations the Bayes net system needed to consider. It did not eliminate consideration of the cases where a student transposed two tokens, but instead caused the system to generate two hypotheses to explain the error—each considering its transposed token to be in the correct location but with the other token not incorporated.

One issue with the original DCBN system was that whenever the student created an identifier the system would use the “public” keyword at the beginning of the method to
create a new method declaration hypothesis regardless of the separation between the two tokens. To limit the generation of such implausible hypotheses, the maximum evidence range of a hypothesis (captured by the number of tokens supporting the hypothesis) was used to limit the range from which a given parent hypothesis could draw its children. The maximum range of used evidence was determined for each rule using the development portion of the corpus. This maximum range was then bloated to allow for some random student insertion errors (e.g., allowing two additional tokens to the left and right). At run-time, when some parent hypothesis was being considered for instantiation, the evidence index of the motivating evidence (i.e., the child node that was driving the parent’s instantiation) was used to center the parent’s maximum range. Potential candidates to become children of the parent hypothesis were then selected from only within that range. This heuristic prevented the parent hypothesis from selecting children an arbitrary distance away in the student’s code. This was not as restrictive as it seems, since, if ever a hypothesis did require evidence outside of its range, multiple hypotheses would be created to explain portions of the evidence—a situation that could be detected and explicitly handled in a more complete system.

**Editing existing code.** The evidentiary support range and maximum evidence range were also used to deal with student modifications to existing code. Deletions are well handled by the existing system, but student insertions can lead to a case where a hypothesis is no longer plausible because the child nodes have incrementally become too far apart (e.g., the student starts with “a=0;” but changes it to “a=1; b=0;”). Without some means to remove the original hypothesis, the Bayes net construction process can get stuck, since the original tokens (i.e, “a=0;”) are fully explained and unlikely to get unseated by a competitor. The
code understanding DCBN system explicitly checks for hypotheses that have grown beyond their maximum range and removes them from the Bayes net. This too is not as restrictive as it sounds, since the top-down step can re-instantiate reasonable hypotheses to explain the data.

Evidence importance heuristic. In both of SketchREAD’s domains, the informational value of each primitive stroke was relatively constant. For Java™ this is not true, with many tokens (e.g., “;”, “(“, “)”) being particularly non-informative. An importance-weighting system was used to prevent all tokens from always generating all their parents.

The development portion of the corpus was used to calculate $P(\text{rule} \mid \text{token})$ for all rules and tokens. These distributions were then rescaled and thresholded for each rule, so that only the most determinative of a rule’s children would cause its generation. This correspondingly means that some tokens (i.e., “;” and “)”) never instantiate parent hypotheses but merely slot into existing hypotheses.

Recursion. Recursion is handled by an explicit check to limit infinite recursion when the Bayes net is being constructed. The maximum recursion level for each rule is computed using the development portion of the corpus. That limit is then used to cap the recursion at run-time. As was mentioned earlier, the grammar was altered (particularly the expression portion) to reduce the grammar’s reliance on recursion.

The inner loop. The basic algorithm for assembling Bayes nets (see Figure 12) is a four-step process that occurs as each new piece of evidence is received. Each step is geared towards controlling the potential for combinatorial growth of the Bayes net, while maintaining its correctness and utility.
I) Bottom Up Processing
   Take new input and incorporate into the Bayes net
II) Top Down Processing
   Use Bayes net state to flesh out net
III) Pruning
   Heuristically remove hypotheses
IV) Choose Most Likely Interpretation

Figure 12: Code Understanding system’s inner loop.

In Step I, for each key press, the DCBN algorithm spawns a token-level minimum edit distance pass over the student’s code to find the inserted and deleted tokens. Deleted tokens simply lose their evidentiary status in the Bayes net and are usually pruned away on the next pass. For new tokens, the existing proposed evidence (e.g., the “; - 0” node in Figure 9) is examined to find any that are consistent with regard to their lexical constraints. If a match is found, the new token greedily replaces the proposed evidence in the Bayes net (e.g., the real “;” replacing the “; - 0” node). If no match is found, then the new token is simply added to the Bayes net. In either case, every rule that contains the new token in its right hand side is considered as an explanatory hypothesis. At this point, the P(rule | token) information is used to skip hypothesis instantiation for non-discriminative tokens. Also at this point, the maximum evidence range of each proposed hypothesis is computed by expanding the evidentiary basis of the driving Bayes net node using the proposed rule, token and the token’s slot in the rule to look up the typical left and right extent. The maximum evidence range and
rule definition are then used to find all the possible slot fillers for the rule (reserving the
driving Bayes net node’s slot solely for it). Except for the driving Bayes net node’s slot,
instantiating new proposed evidence is also considered. Each possible combination of the slot
fillers is then generated and evaluated based on several criteria.

First, the proposed rule must have sufficient evidence to be instantiated (i.e., taking
into account optional portions of the rule, are there enough evidence-supported children to
warrant the hypothesis’ instantiation). This evidential support test is different from the one
used in SketchREAD. For the parsing domain, a hypothesis is required to have pre-existing
nodes for each slot to the left of the driving Bayes net node (i.e., no proposed evidence is
allowed). This acts to reduce the amount of proposed evidence that is created overlaying the
code the student has already completed. Second, all the children’s evidence constraints must
be consistent and must form a valid left-to-right ordering with no duplication. Third, the
hypothesis cannot cause improper recursion, and finally the hypothesis cannot duplicate an
existing hypothesis. If all these tests are satisfied, then the hypothesis is instantiated.

Care is taken during instantiation to greedily reuse any existing incomplete rule nodes
that are consistent with the child nodes. Additionally, existing Bayes net nodes (particularly
the proposed evidence) are reused as much as possible. These two steps serve to greedily
minimize the Bayes net size.

If, upon instantiation, a rule is completely supported by its children (vs. having
several proposed evidentiary children), the bottom up Bayes net creation process is repeated
on the newly completed node (e.g., the sExpression1Rest node in Figure 8). Because the code
understanding system often simply replaces an existing node with another (e.g., in the top-
down pass, when a proposed evidentiary node is replaced with real evidence), the code understanding DCBN system must also sometimes make a special traversal up the Bayes net, firing off recursion on Bayes net nodes that have become complete through other means. This approach to controlling the combinatorial growth of hypotheses is similar to SketchREAD’s constraint based system (although a bit more rigid). Each hypothesis is evaluated with regard to the constraints it must satisfy prior to its instantiation. In no case is a hypothesis added to the Bayes net if it would cause a cycle in the graph.

For Step II of the inner loop of the code understanding domain, the top down step performs two actions. It attempts to complete any incomplete hypotheses, and tries to replace proposed evidence with real evidence. The first action operates by finding all the rules for which an incomplete node is a left hand side. Each candidate is then evaluated in exactly the same way as in the bottom up step. The second action operates by scanning through the proposed evidence and the real evidence, checking for a pair whose constraints are consistent. If such a match is found, the proposed evidence is greedily replaced with the real evidence.

In SketchREAD, Alvarado and Davis included a re-interpretation pass in their Step II. This pass would consider alternate interpretations of the user’s strokes given the context provided by higher-level hypotheses (e.g., could this “line” actually be a poorly drawn ellipse). This step made sense in the sketch recognition domain where low-level input noise was common, but was not found useful in the code understanding domain (i.e., it was not productive to question the tokenizer’s categorization).
For the pruning step (Step III), the code understanding DCBN system implements SketchREAD’s likelihood and redundancy-based pruning. For the first, all the parents of a node are compared and those below a threshold of the most likely are removed (as seen in Figure 4 and Figure 5). Care is taken during the pruning process to ensure that all nodes that are going to remain keep all of their children, preventing holes from opening up in a hypothesis. Redundancy-based pruning is implemented via a garbage collection step that eliminates duplicate hypotheses and merges proposed evidence. This step greatly reduces clutter in the Bayes net.

In SketchREAD, Alvarado and Davis also implemented an age-based pruning step where the age of each incomplete hypothesis was compared against some tolerance and those that were too old were removed. The intuition here was that if the user had not completed a figure after some time limit, they did not ever intend to do so. Age-based pruning was found to be inappropriate for the code understanding domain since students would frequently partially complete a portion of the code and then return to it much later (e.g., begin a for loop then work on the loop contents then return to fix bugs in the for loop.)

Finally, for the interpretation selection step (Step IV), the code understanding DCBN selects the single most-likely top-level hypothesis (e.g., a method declaration). This is a bit stricter than SketchREAD’s system of collecting a set of hypotheses that together cover the available evidence, but allows direct comparison of the chosen hypothesis with the top-down recursive-descent compiler’s abstract syntax tree.

**Bayes net evaluation.** The described process constructs the Bayes net, however several additional steps need to be completed before inference can be used. In particular, the
appropriate probability distributions must be provided, missing/pruned parents need to be handled and the actual inference method must be selected.

Whereas SketchREAD used a combination of empirically and manually determined probabilities, all of the code-understanding system’s probabilities were empirically determined. Both the prior probabilities for each rule and the causal strengths for the Noisy OR nodes were computed from the development portion of the corpus. In SketchREAD, Alvarado and Davis set $P(\text{child}=t \mid \text{parent}=t)$ to 1.0, if the child were a required portion of the parent, or to 0.5, if the child were an optional portion of the parent. Although the empirical method is more accurate, in practice it made a difference in only a few cases (e.g., for non-uniformly distributed optional nodes – since required children were also empirically always 1.0).

Because the DCBN algorithm only generates a portion of the full Bayes net, it is necessary to account for the influence of parent nodes that are either not instantiated or have been pruned away. The code understanding system assumes that parents that have been pruned away are no longer viable and will not have any influence on their orphaned children. It constructs a leak probability for each node that takes into account the likelihood that that node could have been caused as a result of a parent that was not currently in the Bayes net (and had not been previously pruned away). SketchREAD accounted for missing hypotheses in the exact same manner.

Finally, to actually perform the Bayes net inference, the code understanding system used the University of Pittsburg’s Decision Systems Laboratory’s SMILE (SMILE) reasoning engine. Relevance-based decomposition inference was used in place of
SketchREAD’s use of loopy belief propagation. It was found that, for the smaller Bayes nets in the code understanding domain, the relevance-based decomposition was fast enough and more reliable than loopy belief propagation (please see the evaluation section for more discussion of this topic). Unlike SketchREAD, the code understanding DCBN system did not arbitrarily limit the maximum number of parents to eight. It was hoped that this would allow an improved recognition rate without too great a performance impact.
CHAPTER 3

Evaluation

Overview

In order to mimic the observed behavior of human tutors, an ITS must be able to recognize a student’s intent, even when confronted by partial, buggy and un-compileable code, and it should be able to perform this recognition in real-time. Additionally, the code understanding system should be reasonable to implement and maintain and support a fine-grained student model.

The evaluation of the implemented system will use the above four criteria to assess DCBN’s suitability for ITS code understanding. Recognition capability will be assessed through comparison against a recursive descent top-down parser and a minimum edit distance baseline. For the minimum edit distance comparison, the fraction of available evidence explained will be used as a metric. The code understanding system’s performance will be assessed by its processing time per student input character. Code complexity will be assessed via lines of code and development time. Finally, student model support will be assessed qualitatively.

Corpus

The corpus used for the evaluation was derived from a series of human-tutor novice-programmer tutoring sessions. For each session, the tutor and student were only allowed to communicate via a chat interface and the tutor could see but not alter the student’s coding window (Boyer, Dwight, Fondren, Vouk, & Lester, 2008). Each student key stroke was
logged to a database yielding a detailed corpus of student actions and tutor interventions. This corpus was divided 2/3-1/3 into development and testing portions with 20 sessions selected for development and 10 for testing.

For development and evaluation purposes only a portion of the tutored problem was used. Figure 2 shows the method the students had to complete. All students used a for loop to accomplish the task, but varied in the usage of variables, declarations of the variables and use of brackets.

Figure 13 and Figure 14 show the number of student programming actions in the development and testing sessions respectively. The development portion had a mean of 139.0 programming actions (i.e., keystrokes) per session, with a standard deviation of 55.68 while the testing portion had a mean of 152.7 programming actions per session with a standard deviation of 56.03. The development portion was compileable 11.4% of the time (i.e., the student code could be compiled only 1/10 of the time), while the testing portion was compileable 8.6% of the time. All sessions (both development and testing) ended in a compileable state.

![Figure 13. Development set Programming Action Histogram.](image1)

![Figure 14. Test set Programming Action Histogram.](image2)
Baselines.

**Compiler.** To assess the code understanding system’s grasp of the student code, whenever the code is compileable the compiler’s abstract syntax tree is compared to the Bayes net’s interpretation. In this case, the compiler’s abstract syntax tree represented the ground truth and comparing the Bayes net’s answer to it assesses whether the Bayes net is correctly interpreting the student’s code. To make this feasible, the compiler and Bayes net employ the same grammar.

**Minimum Edit Distance.** Minimum edit distance was used as the second baseline for the DCBN code understanding system’s evaluation. Minimum edit distance is a simple and widely used method for student response evaluation, in which the system matches the student solution against a set of answers and selects the one that is closest as measured in insertions and deletions. For the code understanding system’s evaluation, a minimum edit distance system was implemented that operates at the token level (i.e., it finds token insertions and deletions rather than character insertions and deletions). The answer key was also specified in tokens. An identifier in the answer key needed only be matched by another identifier-typed token in the student’s code to be considered a match. All other tokens (e.g., keywords) must have matched in both type and contents. This permissive matching scheme corresponds to the DCBN’s operation (i.e., constraints on identifier values were not added to the Bayes net) permitting a valid comparison between the two.
Results

**Quantitative.**

**Development set results.** The development set was used to implement the DCBN-based code understanding system. Since every student plan in the development set was taken into account during implementation, the development set performed very well. In particular, whenever the student’s code was compileable, the most likely interpretation selected by the Bayes net always matched the recursive descent top-down compiler’s abstract syntax tree. For the minimum edit distance system, only five “answers” were required to cover all 20 development tutoring sessions (i.e., each session converged on one of the five correct answers by the end with no evidence left unexplained). Although it is best case due to the development of the system to match the available data, the development set’s results still demonstrate the workings of the DCBN-based code understanding system and provide baseline expectations for the test set’s results.

Figure 15 shows the average amount of evidence (in tokens) as a function of progress through a tutoring session (Note: the figures presented in the body of this work stretch each session to align their start and end. Matching figures that do not time scale the student actions are presented in Appendix A. The time-scaled figures are easier to understand and discuss and do not vary substantively from the figures in Appendix A). As expected, on average the amount of evidence grew almost monotonically throughout the session. The variance in the amount of evidence grew in the body of the session as the students got into the problem and their solutions diverged. The slight tapering of the variance near the session end was
probably a result of the tutors wrapping up the session with some variance remaining due to the different solutions.

Figure 15. Time-scaled Development Data: Mean and standard deviation of evidence.

Figure 16 compares the minimum edit and DCBN-based systems’ fraction of evidence explained throughout a tutoring session. Both systems behaved as expected. The minimum edit distance approach accounted for each token as quickly as it could, while the DCBN system had to wait until sufficient evidence accumulated before it could instantiate a higher level hypothesis and have the student’s tokens incorporated into the top-level hypothesis. The double dip nature of the DCBN curve matched the usual session’s progression from the outer “for” loop to the loop contents.
Figure 16. Time-scaled Development Data: Comparison of minimum edit and DCBN by fraction of evidence explained.

The dip in the DCBN’s fraction of evidence explained at the end of the session was a result of two outlier sessions. Figure 17 shows that the majority of the sessions followed the average path but there were two sessions that lost traction on the problem right at the end. Note that the lower fraction of evidence explained does not mean that the evidence was not explained somewhere in the Bayes net; it merely means that the evidence and its parent hypotheses were not incorporated into the dominant top-level hypothesis.
Figure 17. Time-scaled Development Data: Fraction of evidence explained for all DCBN sessions.

Figure 18 and Figure 19 show the mean and standard deviation of the evidence explained fraction for the minimum edit distance and DCBN systems (providing more detail than in Figure 16).

As can be seen in Figure 18, the minimum edit distance method behaved as expected. It had a somewhat constant mean and standard deviation (compared to the DCBN) and converged to the correct answer at the end of the session. The variance decreased a bit at the end of the session as the tutors consolidated the students’ answers.
In Figure 19 it can be seen that the DCBN system also behaved as expected and converged to the correct answer by session end. The variance grew substantially as the students got into the body of the problem and (ignoring the effect of the outliers) it tapered off towards the end of the session.
Figure 19. Time-scaled Development Data: DCBN mean and standard deviation of evidence explained fraction.

Figure 20 shows the number of Bayes net nodes both before and after pruning. The pruning process behaved as expected, with fewer nodes existing after the pruning step and both curves increasing with the amount of evidence. The pre-pruning curve had a .986 correlation with the amount of evidence (Figure 15), while the post-pruning curve had a .996 correlation. This behavior matches Alvarado’s results, although SketchREAD had substantially larger Bayes nets.
Figure 20. Time-scaled Development Data: Number of Bayes net nodes before and after pruning.

Figure 21 shows that the variance in the pre-pruned number of nodes is very high. This is a result of different student actions incurring different numbers of generated hypotheses. Figure 22 shows that the number of post-pruned Bayes net nodes is far more stable than the pre-pruned number.
Figure 21. Time-scaled Development Data: Mean and standard deviation of pre-prune number of Bayes net nodes.

Figure 22. Time-scaled Development Data: Mean and standard deviation of post-prune number of Bayes net nodes.
Besides the number of nodes, the interconnectedness of the Bayes net is another metric for its complexity. Figure 23 shows the average maximum number of parents in the Bayes net both before and after pruning. As expected, the pruning reduced the interconnectedness of the Bayes net in addition to shrinking its size. The average maximum number of parents did increase slightly within the body of the session as more hypotheses competed to explain the observed data.

![Figure 23. Time-scaled Development Data: Pre- vs. Post-pruning maximum number of parents.](image)

Figure 24 shows the mean and standard deviation for the pre-pruning maximum number of parents. The maximum number of parents was highly variable due to the wide range of hypotheses that could have been competing. Figure 25 shows the mean and standard
deviation for the post-pruning maximum number of parents. The pruning process greatly reduced the variability in the interconnectedness of the Bayes net.

![Graph showing time-scaled development data: mean and standard deviation of pre-pruning maximum number of parents.](image)

**Figure 24.** Time-scaled Development Data: Mean and standard deviation of pre-pruning maximum number of parents.

Finally, Figure 26 shows the mean and maximum of the per student input character running time. The overall mean was .37s, while the overall standard deviation was 6.11. The variability in the execution time was driven by the pre-pruned Bayes net size and maximum number of parents. This extreme variability makes it difficult to incorporate DCBN-based code understanding into an ITS. These timings results were faster than those reported by Alvarado, resulting from the smaller Bayes net size.
Figure 25. Time-scaled Development Data: Mean and standard deviation of post-pruning maximum number of parents.

Figure 26. Time-scaled Development Data: Mean and maximum of running time per student character stroke.
**Test set results.** The test set consisted of 10 sessions not seen during development. The DCBN system was able to process 9 of the sessions but failed on one because of runaway combinatorial hypothesis generation. Omitting the failed session, the DCBN system failed to match the top-down recursive descent parser’s abstract syntax tree in five cases out of the 155 times the student code was compileable (yielding a failure rate of 3.2%). This matching failure never occurred at the session’s end so the DCBN was able to get back on track.

The minimum edit distance method failed to find an answer that explained all the data by session’s end twice. In the first case only one token was unexplained (a “≤” instead of a “<” in a “for” loop). In the second case, 12 tokens were left unaccounted for. Creating the missing answer would require only a minor modification to an existing answer — which the minimum edit algorithm did correctly identify (i.e., the minimum edit system matched the semantically closest of the five available patterns). The session on which the minimum edit system failed was also the one on which the DCBN system diverged.

Figure 27 shows the average amount of evidence in the test set. Taking into account noise due to the smaller sample size, it closely matches the development set (Figure 15). (Note: all of the test set figures omit the failed session—it is treated separately later). Figure 28 compares the minimum edit and DCBN fraction of evidence throughout the session. These results also closely match the development set’s results (Figure 16). Figure 29 shows all of the DCBN fraction of evidence paths throughout the session. The test set had fewer outliers than the development set. Figure 30 and Figure 31 show the mean and standard deviation for the minimum edit and DCBN fraction of evidence explained respectively. They
reveal that in both cases the variance was greater for the test set due to unseen student sessions (and smaller sample size).

Figure 27. Time-scaled Test Data: Mean and standard deviation of evidence.
Figure 28. Time-scaled Test Data: Comparison of minimum edit and DCBN by fraction of evidence explained.

Figure 29. Time-scaled Test Data: Fraction of evidence explained for all DCBN sessions.
Figure 30. Time-scaled Test Data: Minimum edit distance mean and standard deviation of evidence explained fraction.

Figure 31. Time-scaled Test Data: DCBN mean and standard deviation of evidence explained fraction.
Figure 32 through Figure 34 show the relation between the pre-pruning and post-pruning number of Bayes net nodes. The test set had a slightly greater variability than the development set, particularly in the pre-pruning number of nodes. The pre-pruning curve had a correlation of .968 with the evidence curve (down from .986 in the development set), while the post-pruning curve had a correlation of .995 (matching the development set’s .996).

Similarly, the pre-pruning and post-pruning maximum number of parents (Figure 35 through Figure 37) matched the development set curves but with greater variability (particularly in the pre-pruning numbers).

Figure 32. Time-scaled Development Data: Number of Bayes net nodes before and after pruning.
Figure 33. Time-scaled Test Data: Mean and standard deviation of pre-prune number of Bayes net nodes.

Figure 34. Time-scaled Test Data: Mean and standard deviation of post-prune number of Bayes net nodes.
Figure 35. Time-scaled Test Data: Pre- vs. Post-pruning maximum number of parents.

Figure 36. Time-scaled Test Data: Mean and standard deviation of pre-pruning maximum number of parents.
Figure 37. Time-scaled Test Data: Mean and standard deviation of post-pruning maximum number of parents.

Figure 38 shows the average and maximum running time through a student session for the test set. The mean was .53s with a standard deviation of 7.3. The test set’s times were more variable than the development set’s (Figure 26). This is consistent with the greater variability in the number of nodes and interconnectedness of the Bayes net.
Failed Session. The DCBN-based code understanding system failed to complete on one of the test sessions. It ran out of memory within the SMILE library (SMILE) 65% of the way through a session attempting to convert the causal strengths to a CPT. One limitation of SMILE is that it does not fully exploit Noisy OR nodes and converts them to regular CPTs prior to inference. The exponential growth of the CPT with the number of parents resulted in SMILE attempting to allocate a 1GB block of memory.

Figure 39 shows that the amount of evidence provided by the student was not unusual. Figure 40 also reveals that the DCBN system was behaving as usual with regard to the amount evidence for which it could account, showing the normal lag for the “for” loop. Figure 41 and Figure 42 however show that on the 123rd student action both the size of the Bayes net and its interconnectedness sky-rocketed. This increase occurred because the
DCBN system got trapped in the combinatorial explosion of trying to reorganize statements into blocks.

Note in Figure 40 that the minimum edit solution was also not able to deal with this student’s solution. The minimum edit system was not able to explain the entirety of the solution and did not converge to 1.0 at session end. The minimum edit system did, however, select the answer key that was semantically closest to the student’s solution (i.e., the student’s solution was a minor variation of the selected answer).

![Failed Session: Amount of Evidence](image)

**Figure 39. Failed Session: Amount of evidence**
Figure 40. Failed Session: Fraction of evidence explained.

Figure 41. Failed Session: Pre- vs. Post-Pruned Number of Bayes net nodes.
Maximum Number of Parents

Programming Action Number
Failed Session: Pre vs. Post-Pruned Max Number of Parents

Figure 42. Failed Session: Pre- vs. Post-Pruned maximum Number of Parents.

**Development Time.** The core Bayes net construction portion of the DCBN system took substantially greater than 30 man days to implement and debug. In contrast, it took only 1 man day to implement the minimum edit distance system and create the five answer patterns required for the development set. The core DCBN system consists of 7962 lines of code (omitting comments and blank lines), while the minimum edit distance system only requires 319 lines of code (25x less). The minimum edit distance system is clearly a far simpler system.

**Qualitative.** In general, the Bayes net generation and inference system behaved as expected. The Bayes net nicely handled ambiguity in the student’s code by creating multiple hypotheses to explain the same data. The lag in hypothesis creation was a bit counter-
intuitive, but usually worked appropriately. In some cases, however, the Bayes net hypothesis generation lagged far behind what a human tutor would know (i.e., a human tutor would know the student was trying for a “for” loop quite early in the “while(i = 0, i < 50, i++)” example, but the DCBN would have to wait for extra evidence to formulate such a hypothesis). This would be a potential problem for an ITS attempting to exactly emulate a human tutor by delaying mitigation until later than a human could do so. Overall, however, the hypothesis creation yielded a conceptually pleasing progression.

Although the quantitative analysis captures some aspects of the DCBN and minimum edit distance performance, it is not entirely accurate. While the minimum edit solution appears to uniformly account for student actions, it is blindly matching tokens without considering their intent. Some of this intent is “compiled” into the answers (i.e., the minimum edit system cannot go too far astray since it has to cleave closely to the structure of the provided answers), but the “intelligence” behind the minimum edit matching is minimal (also “precompiled” into the answers). The DCBN system, at least, uses structured knowledge of the domain to better account for student actions.

Since the actual knowledge of the student intent is “compiled” into the minimum edit answers, it is difficult to operationalize it to drive a student model. In the cases where the minimum edit answers are compileable, an abstract syntax tree could be built for each answer and, as tokens are matched, the explained abstract syntax tree nodes could update a student model. This approach, however, would be difficult to extend to higher-level PROUST-like plans and goals. DCBNs, on the other hand, could clearly be extended to support such higher-level knowledge. The PROUST-like Bayes net fragments would be used to generate
competing hypotheses with the most likely explanation updating the student model. Thus, while minimum edit could be enhanced to support a fine grained student model, the DCBN architecture supports it in a natural manner.
CHAPTER 4

Related Work

This work rests at the intersection of several active research areas. Prior programming ITSs provide other sample points in the code understanding system design space. Program understanding directly speaks to some of the requirements of the code understanding system. Plan recognition, and particularly DCBN-based plan recognition, provides the inspiration for the proposed approach. DCBNs are a form of knowledge-based model construction and rely on the field of graphical models. Finally, code understanding is closely related to parsing and compilation and relies on much of the framework and tools of that discipline.

ITSs for Programming

LISP tutor. LISP Tutor was an early cognitive tutor (Anderson & Reiser, 1985; Corbett, Anderson, and Patterson, 1988) based on Anderson’s ACT* theory of learning and cognition. LISP Tutor’s programming knowledge was encoded as a set of about one thousand if-then productions. Given a problem description, LISP Tutor used planning to determine a set of acceptable solutions. Early versions of the system then monitored student actions and immediately corrected them if they deviated from an acceptable path, using “buggy” productions to both detect the bad action and drive the correction. Later versions of the system precompiled the acceptable solutions and allowed the student to buffer their actions for evaluation (granting greater input flexibility).

Despite its generality, LISP Tutor was actually quite restrictive. By employing a top-down, left-to-right editor with no ability to alter prior code and immediately correcting
student errors, initial versions of LISP Tutor greatly limited the range of student input. Although better, later LISP Tutor versions were still very restrictive. While the student was allowed to code ahead, the evaluation system would still proceed top to bottom left-to-right—only characterizing the first student error and discarding “incorrect” later sections. Early LISP Tutor versions also explicitly queried the student regarding their next goal thereby further limiting the scope of the student-action understanding problem.

LISP Tutor was evaluated through its use in a LISP mini-course and in a more standard classroom setting. In the mini-course, students using LISP Tutor were 30% faster at finishing the exercises and performed one standard deviation (43%) better than students working on their own. In the standard classroom, the LISP Tutor students were 60% faster and performed 30% better than the control students.

With regard to where it lies in the code understanding design space, LISP Tutor greatly restricted the variability of student solutions but provided token-by-token updates. The technology supporting LISP Tutor was complex but it was able to drive a very detailed student model (i.e., each production could be mapped to some piece of student knowledge).

**Java™ intelligent tutoring system.** The Java™ Intelligent Tutoring System (JITS) (Sykes & Franek, 2003; Sykes & Franek, 2004) is a more recent tutoring system focused on Java™. JITS uses a hybrid approach to code understanding: if an answer key is provided, it uses a simple minimum edit distance algorithm, but otherwise it uses an error-correcting parsing approach loosely based on Aho and Peterson (1972). In the error-correcting parsing approach, minimum edit distance is used to transform tokens into plausible inputs (i.e., reserved words, keywords and the symbol table contents). If no match is found, the scanner is
then forced to add plausible tokens (e.g., generate a missing “;”). The changes found by the minimum edit distance or error-correcting parsing systems are then used to drive system interaction.

JITS represents a very different set of design decisions than LISP Tutor. The input is very unconstrained but the student must manually press a “parse” button to have JITS evaluate their code. The technology needed for JITS is far less than that required for LISP Tutor and correspondingly does lose some ability to model student knowledge (particularly for the pure minimum edit distance path).

PROUST. PROUST (Johnson & Soloway, 1985; Johnson, 1986) was a planning-based program understanding/debugging system based on Soloway et al.’s theory of programming (Soloway & Ehrlich, 1984; Soloway, 1986; Spohrer & Soloway, 1985). PROUST’s programming knowledge was encoded as a set of goals and plans which, given a description of the problem and a compileable student solution, were used to determine a probable student implementation path. Heuristics were used to constrain the search space to the more probable goal-plan decompositions (e.g., goal A is usually implemented via plan B) and to decide amongst competing alternatives (e.g., if two goal-plan decompositions explain the same data, select the one that has the less serious error). Matching between the generated and student code was used to evaluate the proposed paths. PROUST’s matching system could resolve near misses (and thus account for additional variability) by altering the code via common transformations. Problem areas in the student code were identified by the appearance of “buggy” plans in the decomposition and mismatches between the generated and student solutions.
For its evaluation, PROUST was run on 206 student solutions to a simple programming problem. PROUST was able to completely explain 72% (149) of the programs and partially explain 22% (45) of the programs. It was unable to explain 6% (12) of the programs. Of the 72% completely explained, 95% of them were correct explanations.

While both PROUST and Lisp Tutor used planning to discover student intent, they mainly differed in the flexibility of their understanding systems. PROUST implemented a more flexible algorithm that allowed it to accept a complete student solution rather than tracking the student step-by-step. This more flexible input mechanism exposed PROUST to a wider range of possible solutions (i.e., the student could get further off track in PROUST than in LISP Tutor). Even the later versions of LISP Tutor still evaluated the student solution top-down left-to-right only allowing some skipping within the solution tree.

In terms of the code understanding design space, PROUST was designed to accept a wide range of student solutions but did require that they be compileable. Solutions were only evaluated when the student successfully compiled their solution. The planning-based recognition was complex but, like LISP Tutor, PROUST could drive a very fine-grained student model.

All the presented code understanding systems are highly relevant to the current work. The DCBN bottom-up creation of Bayes net hypotheses is a reversal of LISP Tutor and PROUST’s top-down planning approach. LISP Tutor and PROUST’s goal/plan knowledge base (including buggy productions) is transformed in the proposed system into Bayes net fragments that are added as supporting evidence appears. JITS uses minimum editing distance extensively. Minimum edit distance is a simple and widely used method of assessing
student answers and forms one of the baselines against which the DCBN-based system was compared.

**Code Understanding**

**Programmer’s apprentice.** The Programmer’s Apprentice project was a large effort at MIT to codify programming knowledge and develop a programming assistant to handle the more mundane portions of coding (Rich & Waters, 1987; Rich & Sidner, 2006). For a knowledge representation, they developed a plan calculus that could capture both knowledge about programming and knowledge of a specific program. This plan calculus was used in their KBEMACS tool, which could create a program from a concise specification and allow editing of the program’s structure to effect implementation changes.

As part of the Programmer’s Apprentice project, Rich and Wills (1987) created a LISP program recognition system (the Recognizer) using the plan calculus knowledge base. This system converted the plan calculus into flow graphs, and then used a flow-graph parser to explain small programs in terms of the program calculus clichés it employed. This process allowed the Recognizer to identify semantically equivalent programs in the face of different implementations.

The Programmer’s Apprentice and the Recognizer are very relevant to the current work. As in LISP Tutor and PROUST, the Programmer’s Apprentice’s conceptualization of programming and programs as a product of hierarchical plans and goals forms the basic theory behind the DCBN’s operation. Like PROUST, the Recognizer handled many of the understanding problems faced by the DCBN system (e.g., divergent implementations). The
Recognizer, however, was limited in its handling of unrecognized code (i.e., it provided a means of skipping it and restarting its search) so would not be suitable for the buggy and incomplete programs encountered by an ITS’ code understanding system.

**Plan Recognition**

Using DCBNs for plan/intent recognition is not new. Alvarado and Davis (2005) employed such a system to recognize sketches while Goldman (1990) used them to recognize plans in short stories. Common to both methods (and to the current work) is the assembly of Bayes net fragments to effect intent recognition, the use of Noisy OR gates to reduce the complexity of the required probability distributions, the use of two construction passes (an upward & downward step) and the inclusion of multiple explanatory hypotheses within a single Bayes net allowing them to compete to explain the available evidence.

**Wimp3.** In Wimp3 (Goldman, 1990; Charniak & Goldman, 1991; Charniak & Goldman, 1993) Charniak and Goldman explored the use of DCBNs to recognize plans in short stories. In Wimp3, plan knowledge was stored in a predicate calculus-like notation which, given the available evidence, was converted to Bayes net fragments and assembled into an explanatory Bayes net. Wimp3 then performed inference on the Bayes net to determine the most likely intent of the story. Wimp3 incrementally generated and evaluated the Bayes net as words were parsed, allowing the system to change its interpretation as more evidence became available.

To both limit the possibility of a combinatorial explosion and determine which Bayes net fragments to assemble, Wimp3 used a separate marker passing system. This system used
the provided evidence to propagate flags through the plan hierarchy. When multiple flags intersected (e.g., buying and driving-to plans intersecting at a parent shopping plan), Wimp3 would consider the new fragment as a candidate for instantiation. Probabilities were incorporated into this search to eliminate very unlikely possibilities (e.g., a holding-up-the-store plan would be rejected because of its low prior).

Wimp3 was evaluated on a 24 story test set after development on a matching 24 story training set. With some modifications to deal with new words and knowledge, Wimp3 was able to recognize 23 out of the 24 test stories. Wimp3 failed on the 24th story because its BN became too large to evaluate.

**SketchREAD.** In SketchREAD, Alvarado and Davis (2005) (Alvarado, 2004) employed DCBNs to recognize sketches in multiple domains. They used the Bayes net to combine low-level stroke data and higher-level domain-specific knowledge to combat noise in their input. As each stroke was processed, it spawned the generation of Boolean shape hypotheses. Higher-level hypotheses were then heuristically created to explain the basic shapes. Each shape could be explained by multiple higher-level hypotheses that were combined via a Noisy OR model. This system allowed incremental updating and interpretation of sketches and the incorporation of multiple knowledge sources (i.e., low-level stroke data and higher-level domain-specific knowledge) into the same formalism. Alvarado and Davis found that the higher-level contextual information allowed the Bayes net to compensate for errors in the low-level shape recognition.

To evaluate their system, Alvarado and Davis collected ten family tree sketches containing between 24 and 102 strokes and 16 to 60 symbols, and 80 circuit diagrams
containing 23 to 110 strokes and 10 to 63 symbols. SketchREAD was able to recognize 77% of the shapes in the family tree domain but only 62% in the more difficult circuit diagram domain. Their baseline system achieved a 50% recognition rate in the family tree domain and 54% in the circuit diagram domain showing the benefit of incorporating the contextual information.

SketchREAD’s intent recognition system is the direct inspiration for the DCBN approach used in this work. Although its approach is not used in this work, Wimp3 is highly relevant as a second reference point for the capabilities and limitations of DCBN-based recognition systems.

Knowledge Based Model Construction

OOBNs and SPOOK. In their OOBN and SPOOK systems (Koller & Pfeffer, 1997; Pfeffer, Koller, Milch, & Takusagawa, 1999) Koller and Pfeffer created object-oriented Bayes net construction languages to model complex domains. In OOBNs, they allowed the definition of Bayes fragments as classes (i.e., instantiable probabilistic models) that supported inheritance (i.e., sub-classes could reuse parent models) and composition. The OOBN language supported the construction of efficient BN inference models by improving the selection of cliques for a junction tree (via localization) and reuse (i.e., derived classes could leverage base class calculations). SPOOK extended OOBNs by adding a quantifier attribute, number uncertainty and reference uncertainty, and allowed inference directly on the SPOOK network rather than converting it to a Bayes net.
Although very similar to DCBNs, the OOBN and SPOOK languages were focused on simplifying the construction of Bayes nets for complex domains rather than incrementally creating a partial Bayes net model of an incomplete system. Correspondingly, the OOBN/SPOOK fragment size was substantially larger than that used in DCBN systems (e.g., a complex car or battalion model vs. a single grammar rule). OOBNs did support refinement of the Bayes net (i.e., a base class object could be replaced with a sub-class object and vice-versa) but this process was user driven.

Plan to Bayes net conversion. Huber, Durfee, and Wellman (1994) developed a constructive algorithm for mapping from plans to Bayes nets. For the simplest case, the system transformed each rule’s left hand side into a Bayes net variable, with the right-hand-side variables becoming its children. Huber et al. provided additional mappings for AND/OR branches and multiple goal plans as well as accounting for temporal dependence and context. Each goal node had the states inactive, active and achieved, while the primitive-action (i.e., leaf nodes) had the states performed and not-performed. Once the Bayes net was complete, the observations would be fed into the leaves and inference would be used to determine the most likely goal.

Huber et al.’s work is closely related to the DCBN methods. Its straightforward conversion of a plan database to a single monolithic Bayes net could obviously yield too large a Bayes net. The DCBN methods developed by Alvarado and Goldman heuristically solve this problem by focusing on the relevant portion of the Bayes net.
Graphical Models

DCBNs are a knowledge-based model construction method that relies on a graphical model (i.e., partial Bayes nets). There are several other formalisms within the field of graphical models that could also form a viable basis for a code understanding system. This section reviews several of these systems and discusses the rationale underlying the selection of DCBNs.

Bayes nets and decision networks. A Bayes net (Charniak, 1991; Pearl, 1988) is a graphical formalism that specifies the dependencies between random variables. It is made up of a directed acyclic graph (DAG) with probabilities. Each root node must have a suitable prior probability and all other nodes must have a Conditional Probability Table (CPT) specifying the conditional probabilities of its states given all combinations of its parents’ states. The Bayes net in Figure 43 depicts a causal model in which an ulcer can cause both anemia and stomach pain while a spicy chili dinner can also cause stomach pain. To use a Bayes net, the observed nodes are set to their known states (e.g., stomach pain but no anemia) and Bayesian inference can then determine the most probable cause.
Beyond merely performing inference, Bayes nets possess several desirable properties when reasoning under uncertainty. Primary among these is the fact that Bayes nets are firmly grounded in probability theory, avoiding the ill-effects of ad hoc weighting systems. By specifying the dependence relations between the random variables, Bayes nets also reduce the number of probability values required to completely specify the joint distribution—a benefit that can be taken further if canonical causality relations (i.e., Noisy-ORs) are exploited. Noisy OR nodes capture the case when each parent can independently cause the child reducing the number of required probabilities to one for each parent rather than one for each parent state combination. Finally, Bayes nets possess the powerful capability to explain away alternate hypotheses. If one hypothesis gains strength over another regarding the same evidence, the weaker hypothesis will become less likely since it is not needed to explain the observed data. For example, if it is known that someone has stomach pain but also that he ate a spicy chili dinner earlier, then it should become less likely that they have an ulcer.
Bayes nets and decision networks (i.e., Bayes nets augmented with actions and rewards) are widely used to model known probabilistic systems where only some of the variables are observable and the problem is to infer information from or make decisions based on the known variables. Bayes nets and decision networks are ill suited for code understanding since the whole Bayes net would be too large and the structure of the student’s solution is not known *a priori* (i.e., the Bayes net cannot be constructed until the student is done). Waiting until the student’s solution is complete would prevent the ITS from responding to the student’s incremental changes.

**Dynamic Bayes nets and dynamic decision networks.** Dynamic Bayes nets (DBNs) and dynamic decision networks are other widely used graphical models (e.g., Murray & VanLehn, 2000). They are used to represent temporally driven changes in state (i.e., a single Bayes net time slice is replicated and temporal links are used to connect the slices). These graphical models are unsuitable for code understanding because the unrolled Bayes net would be even larger than a single Bayes net (which was already too large) and it is unclear what additional information the temporal links would provide. To be specific, if the individual Bayes nets for two time slices were aligned and linked together the temporal links would reveal the changes between the two Bayes nets but that information is more easily modeled by other means. Additionally, in DBNs the time slices are usually exactly the same so deriving the temporal cross links for the potentially very different code understanding time slices would be problematic.

**Hidden Markov models.** Hidden Markov models (Rabiner, 1989) are usually used to determine state transitions within a temporal stream of evidence. Although the code
understanding problem could be characterized as such (i.e., the stream of student generated tokens forms the temporal evidence stream) there are two problems. First, the students often go back and alter prior evidence. By itself this difficulty is surmountable, but code understanding also requires a more complex model of the student’s code than a single layer of hidden states allows. Hierarchical hidden Markov models (Fine, Singer, & Tishby, 1998) could be used to compensate for this but would be cumbersome.

**Markov logic networks.** Markov logic networks (MLNs) (Richardson & Domingos, 2004) combine first order predicate logic with graphical models (i.e., they add a weight to each clause in the knowledge base) to reason in domains where the first order predicate logic statements are not rigidly true or false (e.g., social network modeling). MLNs operate by creating a Markov network for the problem (i.e., by constructing all possible groundings) and then using Markov chain Monte Carlo or belief propagation to perform inference. Although the code understanding problem can certainly be cast into the MLN framework, doing so would create an unduly large network and given the reported performance numbers (measured in minutes rather than seconds) could not satisfy an ITS’ real-time feedback requirement.

**DCBNs.** Of the available graphical models, DCBNs are the only solution likely to be able to meet all the requirements of the code understanding task. The dynamically constructed Bayes net inherits all the benefits of Bayes nets (i.e., firm probabilistic grounding, inference, and explaining away) but only the portion of the Bayes net relevant to the observed evidence is instantiated. The DCBN approach supports the modification of
previous evidence and supports a very detailed and hierarchical representation of the system’s state.

DCBNs do incur some additional costs however. Care must be taken to maintain the probabilistic validity of the Bayes net, since portions of it are not instantiated or are pruned away. Additionally, since heuristics are used in its construction, the resulting Bayes net will not necessarily consider all the hypotheses of the hypothetical full Bayes net and may therefore not always arrive at the correct answer.

**Parsing**

**Error correcting compilers.** Error correcting compilers are a specialty within compilers that augment the parser to compensate for programmer error.

For their error correcting parser, Aho and Peterson (1972) handled symbol insertions, deletions and replacements. In their approach, they augmented the original grammar with additional error production rules and altered an Earley parser to track the number of error productions used in the parse. The minimum edit distance parse could then be selected from the alternatives. The running time of their approach was $O(N^3)$ with $N$ being the number of symbols.

As another example, in his error correcting parser Thompson (1976) used a probabilistic context free grammar (i.e., a context free grammar with a probability attached to each production.) In this formalism, a given parse’s probability is the sum over all the different derivations of the product of the rule probabilities used in each derivation. Thompson formulated the error correcting parse problem as error correction on a noisy
channel model. He proposed a parsing mechanism that selected the most likely parse by amplifying the original grammar with error rules for replacement errors (whose probabilities incorporated the channel’s likelihood of causing that error) but accounting for deletion, insertion and transposition errors in the parser’s processing. In his combined solution, Thompson used a minimum probability threshold to reduce the required bookkeeping, but his approach was still exponential with regard to the number of tokens.

Although well-defined and able to leverage much of the machinery of compilers, the error correcting parsing approaches are still limited. Primary among these limitations is their assumption of only insertion, deletion, replacement and transposition errors. The buggy rules in LISP Tutor and PROUST provide a much higher-level understanding of why the student is writing incorrect code and allow for appropriate remediation. It is unclear what remediations the error correcting parsers could drive other than syntax correction.
CHAPTER 5

Discussion

Results

The results presented in the Chapter 3 are consistent with those in the literature. Just as the DCBN code understanding system failed on one if the coding sessions, Charniak and Goldman’s Wimp3 failed on one out its 24 test set stories. In both cases, the combinatorial possibilities swamped the systems. Charniak & Goldman went on to identify combinatorial issues as the central challenge for their system. The DCBN performance against the top-down parser was quite good, failing to match the abstract syntax tree only 3.2% of the time. This is roughly comparable to PROUST’s 6% failure rate, but one has to take into account the different scopes (i.e., PROUST does much more), approach (i.e., PROUST uses planning) and evaluation methods (the DCBNs were continuous through a session while PROUST only assessed snapshots). The execution speeds are consistent with Alvardo’s findings where she also observed great variability.

The minimum edit system performed better than expected. It aggressively consumed/explained tokens and did well even when there was no exactly matching answer. In particular, for the session on which the DCBN failed, the minimum edit system at least retained some traction on the problem. This is particularly problematic, since the DCBN-based and all intent-based systems (e.g., LISPTutor and PROUST) are advertised as being more robust for unseen data.
Suitability for ITS Code Recognition

With respect to the evaluation criteria (i.e., ability to process buggy, incomplete and un-compileable code, quick response, easy to implement and maintain and support for a fine-grained student model), DCBN’s get mixed scores. DCBNs usually do well capturing the student’s intent, but sometimes fail spectacularly. The large variability in execution time makes DCBNs problematic for programming ITSs where a real-time response is needed. DCBNs are very complex to implement and maintain. In particular, modifying the system tends to percolate changes throughout its behavior making regression testing critical. Debugging DCBNs is also very difficult, especially with bugs late in a session when the Bayes net is very complex. DCBNs could easily support a very fine grained student model where belief in a given node could translate to belief in the student’s knowledge of a rule. Despite its complexity, DCBNs also possess an architectural elegance lacking in the minimum edit system.

The minimum edit distance system also receives mixed scores for the evaluation criteria. It performed as well, if not better, than the DCBN system at accounting for student actions. It was far faster than DCBNs, and could easily support real-time interactions. Minimum edit distance was easy to implement (i.e., 1 day vs. DCBNs 30+ days) and debug. The only area in which minimum edit distance had difficulty was in the student model where it was unclear how effective and easy it would be to bootstrap from the match information to a student model.

Overall, it is recommended that DCBNs should be avoided as a code understanding system for an ITS. Their variable execution speed, unpredictable behavior (e.g., the failed
session) and high maintenance/debugging cost make them a poor choice. Additionally, in the one case where a truly new solution was seen (i.e., the failed session did not have an answer in the minimum edit answer key), minimum edit actually performed better than the DCBNs, despite intent recognition systems supposedly being better able to deal with unseen solutions. It is true that given a completely different problem (e.g., bubble sort), DCBNs would at least be able to get traction on the student’s code while minimum edit would be at a complete loss. However, the 2-3 hours required to generate a suitable answer key for minimum edit distance is a fraction of the time that would probably be required to get the DCBN-based system debugged and fully working.

**Future Work**

Although DCBNs are perhaps not the best approach to take, minimum edit distance is also far from ideal. A promising alternative is using finite state transducers (as in FASTUS (Hobbs, Appelt, Bear, Israel, Kameyama, Stickel, & Tyson, 1996)) to capture portions of the solution and common bugs. This approach would maintain the simplicity of the minimum edit approach, but better support a fine-grained student model (i.e., each triggered finite state transducer could increase belief in some portion of the student’s knowledge).
CHAPTER 6

Conclusion

Summary

This thesis investigated the adaptation of Alvarado & Davis’ DCBN intent recognition system to the task of code understanding for an ITS. The DCBN approach used heuristics to assemble only the portion of a Bayes net relevant to the observed evidence. Adapting Alvarado & Davis’ DCBN approach from its original sketch understanding domain required the development of new lexically-based constraints, new heuristics to handle student editing of old data and construction heuristics to deal with the non-uniform distribution of token importance. The implemented DCBN-based code understanding system was evaluated through comparison with a top-down recursive descent parser and a minimum edit distance baseline. The DCBN system was able to process 90% of the test set, but ran out of memory on one session due to a combinatorial explosion of hypotheses. The minimum edit distance system did not have an answer pattern for the problematic session but still matched the closest solution. The DCBN-based code understanding system was deemed unsuitable for integration into an ITS due to its unpredictable behavior, wide variability in execution speed and extreme cost to extend and debug.

Concluding Remarks

Just as bigrams are a difficult technique to beat in natural language processing, minimum edit distance appears difficult to beat for student input analysis. In both cases, the
simplicity, predictable behavior and reasonable performance of the simpler system provides a better engineering solution than a more complex and time intensive solution.
REFERENCES


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APPENDICES
Appendix A: Non-time-scaled Figures

Figure 44. Development Data: Mean and standard deviation of evidence. Non-time-scaled correlate of Figure 15.
Figure 45. Development Data: Comparison of minimum edit and DCBN by fraction of evidence explained. Non-time-scaled correlate of Figure 16.

Figure 46. Development Data: Minimum edit distance mean and standard deviation of evidence explained fraction. Non-time-scaled correlate of Figure 18.
Figure 47. Development Data: DCBN mean and standard deviation of evidence explained fraction. Non-time-scaled correlate of Figure 19.

Figure 48. Development Data: Number of Bayes net nodes before and after pruning. Non-time-scaled correlate of Figure 20.
Figure 49. Development Data: Mean and standard deviation of pre-prune number of Bayes net nodes. Non-time-scaled correlate of Figure 21.
Figure 50. Development Data: Mean and standard deviation of post-prune number of Bayes net nodes. Non-time-scaled correlate of Figure 22.

Figure 51. Development Data: Pre- vs. Post-pruning maximum number of parents. Non-time-scaled correlate of Figure 23.
Figure 52. Development Data: Mean and standard deviation of pre-pruning maximum number of parents. Non-time-scaled correlate of Figure 24.

Figure 53. Development Data: Mean and standard deviation of post-pruning maximum number of parents. Non-time-scaled correlate of Figure 25.
Figure 54. Development Data: Mean and maximum of running time per student character stroke. Non-time-scaled correlate of Figure 26.

Figure 55. Test Data: Mean and standard deviation of evidence. Non-time-scaled correlate of Figure 27.
Figure 56. Test Data: Comparison of minimum edit and DCBN by fraction of evidence explained. Non-time-scaled correlate of Figure 28.

Figure 57. Test Data: Minimum edit distance mean and standard deviation of evidence explained fraction. Non-time-scaled correlate of Figure 30.
Figure 58. Test Data: DCBN mean and standard deviation of evidence explained fraction. Non-time-scaled correlate of Figure 31.

Figure 59. Test Data: Number of Bayes net nodes before and after pruning. Non-time-scaled correlate of Figure 32.
Figure 60. Test Data: Mean and standard deviation of pre-prune number of Bayes net nodes. Non-time-scaled correlate of Figure 33.
Figure 61. Test Data: Mean and standard deviation of post-prune number of Bayes net nodes. Non-time-scaled correlate of Figure 34.

Figure 62. Test Data: Pre- vs. Post-pruning maximum number of parents. Non-time-scaled correlate of Figure 35.
Figure 63. Test Data: Mean and standard deviation of pre-pruning maximum number of parents. Non-time-scaled correlate of Figure 36.

Figure 64. Test Data: Mean and standard deviation of post-pruning maximum number of parents. Non-time-scaled correlate of Figure 37.
Figure 65. Test Data: Mean and maximum of running time per student character stroke. Non-time-scaled correlate of Figure 38.