ABSTRACT

HYGH, JANELLE SUZANNE. Implementing Energy Simulation as a Design Tool in Conceptual Building Design with Regression Analysis. (Under the direction of Dr. Joseph DeCarolis.)

Whole building energy simulation is generally used to validate designs; however, its use as a decision support tool during design—especially during early stages—has been limited. Challenges with energy simulation implementation during conceptual design include the difficulty of creating an energy model with many unspecified parameters and the amount of time required to create an energy model and generate results. Use of a simplified simulation building program provides a practical alternative, but produces less accurate results due to the simplification of the complex processes governing the interaction of a building with its environment.

This work describes the development of a regression model based on iteration of a highly detailed energy simulation tool, EnergyPlus. Monte Carlo simulation based on random variations in key parameters relevant to architectural design in early stages (e.g., size, form, orientation, fenestration, materials, thermal properties) is performed to develop the data used in the regression. During conceptual design when design decisions have the most impact on the energy performance of the building, the resultant model provides quick feedback to the user on the effects of changes in these parameters on whole building heating and cooling energy consumption. In addition, sensitivity analysis of the energy simulation results provides guidance for the designer to identify better solutions within the design space. The new methodology developed in this thesis provides quantitative feedback on energy performance that can be used as a design tool without prescribing solutions that limit the creative process of design.
Implementing Energy Simulation as a Design Tool in Conceptual Building Design with Regression Analysis

by
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A thesis submitted to the Graduate Faculty of North Carolina State University in partial fulfillment of the requirements for the degree of Master of Science

Civil Engineering

Raleigh, North Carolina
2011

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DEDICATION

To Seana Campbell, a wonderful person, great friend, and an inspiring Architectural-Environmental Engineer.
BIOGRAPHY

Janelle Suzanne Hygh grew up in Raleigh, North Carolina. With interest in historic architecture, math, and physics, she went to Miami, Florida to pursue a degree in Architectural Engineering. She graduated with Bachelors degrees in Architectural and Civil Engineering from the University of Miami in 2008. During that time she was very active in the American Society of Civil Engineers student chapter. Upon graduation she moved back to North Carolina and worked for a civil engineering consulting firm. In January 2010 she started her Masters studies at North Carolina State University, with an interest in buildings and energy. Her graduate coursework has focused on energy, economics, and environmental modeling; research has brought her back to Architectural Engineering, applied to energy efficiency.
ACKNOWLEDGMENTS

I would first like to thank my committee for allowing me to be a part of this project. I have been able to study something I’m passionate about, and grown as a student, teacher, and researcher in the process. Ranji, Joe, and David – you have an uncommon dedication to your students and your professions. I hope I can continue that passion and dedication in my future endeavors.

I would also like to acknowledge the other people whose discussion and contributions have added to this work: Maria Papiez, Shawna Hammon, Dennis Stallings and colleagues at PBC+L.

To my father, thanks for your countless hours of Perl programming that made this project possible. Working with you has been a joy.

To my parents and family who have stood by me, supported me, and loved me during my best and worst times. I would not be here today if it weren’t for you.

To Jacob Griffin, whose never-ending encouragement and humor were crucial to the completion of this work. Thanks for believing in me always.
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Chapter 1 Introduction

In the conceptual design phase, harmonious schemes composed of elements such as plan, form, fabric, and orientation are developed. At this stage, energy analysis can provide feedback on annual energy consumption and other performance metrics to designers considering energy efficiency. Energy simulation is a powerful tool with the unique capability to model the building as a system to capture the complex dynamic thermal interactions between a building and its outdoor and indoor environments (Morbitzer 2003). The use of energy simulation is increasingly important as performance responses become less intuitive as our buildings become more complex (Hobbs et al. 2003). Energy simulation to provide feedback at the early stages of design is not often done, even though decisions at this stage have the largest impact on energy and cost (Krygiel and Nies 2008). A survey conducted in December, 2000 of approximately 200 architects, engineers, and contractors found that the most common “tool” used to help make design decisions was prior experience and rules of thumb, which highlighted the lack of quantitative tools for decision making in

Figure 1.1: Traditional versus improved design process. In the improved, integrated design process, energy analysis provides feedback through all phases of design when design decisions have the most impact on energy performance.
building design (Jacobs and Henderson 2002). These observations, although dated, still apply to current practice. Energy simulation is primarily used to estimate energy consumption to verify designs and demonstrate code compliance at the end of the design process (Lam et al. 2004; Morbitzer 2003; Rizos 2007). The incorporation of building energy analysis to support design is shown in Figure 1.1, which compares the current approach with an improved process that enables energy analysis to inform building design throughout the design process.

The high level of detail that is fundamental to energy simulation tools limits their use in the design process. Due to the complexity and detailed input required, performing energy simulation at early stages of design requires significant time, resources, and technical expertise. Contractual arrangements normally focus resources on the detailed design stage, thereby limiting the opportunities for energy analysis early in the process. The lack of smooth interoperability between design and analysis tools also limits the automatic exchange of building information, adding to the time requirements of creating an energy model and updating it as the design progresses.

There are many ways to address the barriers to integrating energy simulation throughout the design process to take advantage of missed opportunities for energy and cost savings during early design. First, deliberate focus on the early stages by allocating resources (design fees and time in the project schedule) and requiring energy simulation at every design stage would ensure that energy simulation is performed. This alone does not ensure, however, that energy analysis results would be used as feedback to design. Alternatively, making energy simulation easier to use would lessen the burden of constructing an energy model and would allow quicker generation of results, which is amenable to the iterative nature of building design. Simplified simulation methods or a simplified user interface for a detailed simulation engine could allow energy analysis to be conducted more easily by lowering the number of inputs required and limiting them within the architectural domain. Additional improvements in interoperability between design and analysis tools could alleviate the need to manually translate the architectural model to an energy model, further reducing the user-specified energy simulation input requirements.
The methods of analysis and communication of results should also be relevant to design decisions. Point estimates of energy consumption in conceptual design are not necessarily useful due to the uncertainty stemming from future design decisions that have not yet been made. Energy simulation in early design stages is useful, however, for comparative analysis, though this presents another challenge in requiring an energy model for each design alternative. Instead, if energy simulation tools facilitate broader search of the design space (e.g., by supporting parametric analysis of a whole building or a single room, floor, or façade in isolation), then the results could relate energy performance to key design parameters being explored. Such an approach would offer more meaningful insights and feedback to designers.

The goal of this work is to develop a tool that provides quantitative feedback on energy consumption with respect to key design parameters commonly explored in conceptual design. To overcome the barriers discussed above, the tool must be easy to use and manipulate by non-technical users. As such, the objective is not to create a new simulation tool, but to develop a reduce-form model using regression of data points drawn from runs with an existing detailed building energy simulation model that serves as the information basis for the new tool. The multivariate regression model is based on a set of detailed simulations, but once developed, does not require the user to work directly with the energy simulation tool. Quantitative feedback from the regression model includes quick estimates of energy consumption for a wide range of possible designs to help deliver energy-informed design.

The remainder of this thesis will be organized as follows. Chapter 2 provides a literature review in the relevant areas, describes the overall approach taken in this research, and provides a detailed methodological description. Chapter 3 presents an illustrative study of an office building in four locations. Chapter 4 discusses how this work could be applied in practice and future steps in this research.
Chapter 2 Approach and Methodology

Approaches to increase the use of quantitative energy feedback in the early stages of design include simplifying energy simulation engines or interfaces, furthering interoperability, and using alternative methods of analysis. To lessen the inputs required by detailed simulation tools, simplified building energy simulation methods have been proposed such as the simple hourly method per ISO 13790 (Nielsen 2005) and the MIT Design Advisor (Urban and Glicksman 2007). Other tools offer extensive defaults and assumptions to simplify user input for detailed energy simulation tools such as Autodesk Green Building Studio (Autodesk 2010), which uses the DOE2.2 engine. Interoperability between architectural design and analysis tools is a focus of BuildingSmart, the organization that develops and maintains the Industry Foundation Classes (IFC), an open data schema for BIM covering interdisciplinary building information throughout a building lifecycle (BuildingSmart 2010). Green building XML (gbXML) (gbXML.org 2010) is another open data standard that (in contrast to IFC) only handles information for energy analysis purposes (Dong et al. 2007). Research efforts have produced utilities to enable data transfer from architectural design tools into energy simulation engines (Bazjanac and Maile 2004). Other efforts to encourage and enable energy simulation in design include enabling large-scale parametric analysis with EnergyPlus (Zhang 2009) and a methodology to use simulation in a limited fashion for façade design (ASHRAE 2011 pp. 211-215). Uncertainty and sensitivity analysis with building energy simulation tools have been applied to demonstrate the effect of model uncertainties on rational decision making (de Wit and Augenbroe 2002), the effect of uncertainty in usage patterns to support the detailed design of individual building systems (Burhenne et al. 2010), and the effect of uncertainties in physical properties of materials after construction to support design (Sanguinetti et al. 2009; Hopfe et al. 2007a; Struck and Hensen 2007; Struck et al. 2009).
2.1 Overall Approach

The approach starts with a generic building of a specific type (e.g., medium size office building) with the simplicity and level of detail characteristic of a project in conceptual design, but complex enough to constitute a realistic design problem. Knowledge of energy performance with respect to key design parameters in conceptual design for the generic building can be generalized and made meaningful to many design projects. To eliminate the inputs normally required for a detailed simulation tool, assumptions for inputs defined later in the design process are selected to partially define the base energy model (see Figure 2.1). Identification of key parameters relevant to conceptual design decisions and the associated ranges of possible values define the design space explored in this approach. To sample the design space, Monte Carlo analysis is used to test combinations of parameters within their defined ranges. Monte Carlo simulation results serve as a rich data set, which is used to develop the regression model and validate it against independent EnergyPlus results. Sensitivity analysis using the simulation data also provides parameter sensitivities, or relative importance, of each to energy consumption.

![Diagram](image)

**Figure 2.1:** Framework for Monte Carlo simulation, which provides a rich data set for the development of a regression model and sensitivity analysis.
2.2 Methodology

The approach in Figure 2.1 is realized through three main steps, each of which is described below.

2.2.1 Design Problem Set-Up

The first step starts with configuring the base energy model, which contains assumptions for all necessary energy simulation inputs intended to be implicit in the model developed in this work. Because the purpose of this approach is to develop a model that can be applied to similar projects, the base energy model must be sufficiently generic. Capozzoli et al. (2009) demonstrates this idea by focusing on a typical multi-storey office building, though they limited the analysis to a very simple intermediate floor. The base energy model must also be complex enough to constitute a realistic design problem to be relevant in the design process. Hopfe et al. (2007a), Struck and Hensen (2007), and Struck et al. (2009) apply uncertainty and sensitivity analysis to BESTEST cases, the benchmark energy models used to validate energy simulation programs, with simple geometry consisting of a single zone box with windows, but discuss the use of more realistic design problems. The base energy model with a set of assumed values serves as the starting point for the Monte Carlo simulation, which replaces the targeted parameter values with randomly chosen values distributed uniformly within a prescribed range. Two basic categories of information make up the building model: thermal information and geometry. Thermal information includes site location, monthly ground temperature values, internal loads and schedules, thermostat settings, construction assemblies and material properties, and other site-specific conditions. Geometry must be defined in the model and if it is not held constant, then it must be handled parametrically in the Monte Carlo analysis.

In tandem with defining the base energy model is the identification of key design parameters and their ranges. Two criteria are used to choose design parameters to vary during the Monte Carlo simulation: (1) the parameter has an effect on energy consumption, and (2) the parameter is architecturally relevant in conceptual design. In an idealized environment, the designer would have full knowledge of the effect of every design decision on energy consumption. To make the problem tractable, however, it is necessary to identify key
parameters. In this work, identification of key building parameters likely to affect building energy consumption during conceptual design were selected in consultation with David Hill, an architect on the research project and available literature (Krygiel and Nies 2008; Macdonald et al. 2005). After the parameters are chosen, continuous ranges or sets of discrete values for the parameters are assigned to be compatible with the options available in design.

2.2.2 Monte Carlo Simulation

Monte Carlo simulation explores the building energy performance space associated with the range of all identified parameters. An energy simulation tool calculates the energy performance for each sample in the Monte Carlo Simulation. EnergyPlus (Crawley et al. 1999) was chosen as the energy simulation tool in this methodology because it:

- Is the official energy analysis and thermal load simulation program of the U.S. Department of Energy
- Uses text input and output, which are easy to use in an automated workflow
- Is based on first principles, not simplified algorithms
- Is freely available (non-proprietary)
- Includes extensive documentation
- Allows for visualization and limited modification of an energy model using OpenStudio, a plug-in for Google SketchUp
- Is available for Windows, Mac, and Linux

The Monte Carlo analysis starts by sampling each parameter and substituting the sampled values into the base energy model. To complete the substitution, the values of each parameter must be inserted in the appropriate location in the energy model. EnergyPlus does have built-in parametric objects that allow users to input values corresponding to multiple runs. Tags in the energy model correspond to parametric objects. When EnergyPlus finds that tag, it substitutes the value for that run as defined in the parametric object. While this is

---

1 Google SketchUp is a 3D modeling tool that is designed for its ease of use. As such it is frequently used by architects during early design when more traditional CAD or BIM tools can be cumbersome for simple, rapidly-changing models.
useful for a limited number of parametric runs, it is quite cumbersome in a large Monte Carlo simulation. jEplus is another open source tool that enables large parametric runs using parameter trees with EnergyPlus and works with tags embedded in the EnergyPlus Input Data File (IDF) file (Zhang 2009). In this work, Perl scripts were utilized to make the substitutions in the IDF files. Instead of embedding tags, the Perl scripts use regular expressions to find EnergyPlus objects by name and type and make the appropriate substitution. This approach also makes the methodology easier to port between different energy models because it avoids the need to insert tags at every substitution location.

Though many runs of the energy simulation tool are required in the Monte Carlo analysis, a computationally expensive tool, EnergyPlus, is chosen in this framework. Lam et al. (2004) argue to avoid abstraction and rule-of-thumb approaches and use instead “first principle-based engineering algorithms” for accurate results, an approach aided by the increasing affordability of computing power. Using EnergyPlus avoids additional uncertainty introduced by simplifying algorithms, and because it is a highly configurable tool, it can be used for detailed design. This paper builds on the work described by other researchers, such as Capozzoli et al. (2009), who conducted sensitivity and regression analysis focusing on design variables with architectural significance, as the results were based on the quasi-steady simplified monthly method per ISO 13790: 2008. The importance of using detailed simulation tools is illustrated in a study using BESTEST case 600, a benchmark energy model used to validate energy simulation programs, that found significantly different uncertainties in output (e.g., up to 45% in annual cooling demand and 50% in peak cooling demand), among different simulation tools (Hopfe et al. 2007b). Inconsistent results among tools led Struck et al. (2009) to conclude that future research with sensitivity and uncertainty analysis should use sophisticated tools with simplified interfaces, not abstracted models with a corresponding interface.

2.2.3 Analysis

The data produced by the Monte Carlo analysis is a set of energy model definitions and corresponding energy consumption estimates. Regression analysis of this data set provides an approximate equation for the energy consumption as a function of the key parameters.
Validation with independent EnergyPlus results determines the efficacy of using the regression model in place of direct simulation, which is the ultimate goal of this work. This approach is similar in process to the building envelope trade-off option in ASHRAE 90.1-2007 (ASHRAE 2007): both perform regression on many energy simulations to obtain simple equations. This work differs, however, in its purpose to enable decision-making in conceptual design rather than demonstrate compliance of the final design of envelope components. Also, Capozzoli et al. (2009) perform regression on results that varied six heating and cooling variables, which yield adjusted $R^2$ between 87.9% and 95.2%, and suggest that regression could be substituted for the quasi-steady simplified monthly method per ISO 13790. The work described in this paper represents a significant advancement over prior work by using a highly detailed simulation tool to develop a multivariate regression model based on 27 geometric and non-geometric design parameters. Sensitivities can also be extracted from the data produced by the Monte Carlo analysis to help architects target the most energy-sensitive design parameters during conceptual design.

2.3 Intended Use

This approach of developing a simplified regression model based on a large set of simulation results can provide meaningful feedback and insights to designers throughout the early stages of design. The goal is to develop a generic regression model that can be applied to a range of similar projects. The regression model can give approximate predictions of heating, cooling, or total heating and cooling building energy consumption for any set of key parameter values, with a margin of error calculated during regression model validation. Additionally, sensitivity analysis provides meaningful insight into the relative importance of different design parameters. The next chapter describes an illustrative study that demonstrates the development of this approach for an office building in four locations in the U.S.
Chapter 3 Illustrative Example

The methodology is presented for a rectangular, medium-sized office building, which is analyzed in four climate zones (ASHRAE 2007): 1A- Miami, FL, 4A- Winston Salem, NC\(^2\), 4B- Albuquerque, NM, and 6A- Minneapolis, MN. Table 3.1 provides a comparison of the climate in all locations described by annual cooling and annual heating degree-days with an 18°C baseline.

Table 3.1: Annual cooling and heating degree-days for the TMY3 climate data used for each location (Wilcox and Marion 2008)

<table>
<thead>
<tr>
<th></th>
<th>Miami, FL (1A)</th>
<th>Winston-Salem (4A)</th>
<th>Albuquerque (4B)</th>
<th>Minneapolis (6A)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Annual cooling</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>degree-days</td>
<td>2442</td>
<td>724</td>
<td>724</td>
<td>454</td>
</tr>
<tr>
<td><strong>Annual heating</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>degree-days</td>
<td>67</td>
<td>1695</td>
<td>2303</td>
<td>4202</td>
</tr>
</tbody>
</table>

3.1 Set-up

In this application, changes in form are governed by total building area, aspect ratio (the ratio of building length to depth), and number of stories. The base energy model for each climate zone is identical, except the ground temperatures and weather file used for the energy simulation. Details on the base energy model are provided in Table 3.2.

\(^2\) Winston-Salem, North Carolina was chosen for analysis because it is the site of a case study in related work
### Table 3.2: Description of Energy Model Inputs

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Timestep</td>
<td>6 per hour, or 10 minutes</td>
</tr>
<tr>
<td>RunPeriod</td>
<td>From 1/1 to 12/31</td>
</tr>
<tr>
<td>Ground Temperatures</td>
<td>From DOE Medium Office Reference Building for location being tested</td>
</tr>
<tr>
<td></td>
<td>(Deru et al. 2011)</td>
</tr>
<tr>
<td>Internal Loads</td>
<td>People 150 SF/person</td>
</tr>
<tr>
<td></td>
<td>Lights 1.0 Watts/SF</td>
</tr>
<tr>
<td></td>
<td>Electric Equipment 0.93 Watts/SF</td>
</tr>
<tr>
<td></td>
<td>Schedules: According to ASHRAE 90.1</td>
</tr>
<tr>
<td>Shading</td>
<td>Horizontal overhang for each window</td>
</tr>
<tr>
<td></td>
<td>Projection Factor: depth described as fraction of window height</td>
</tr>
<tr>
<td>Thermostat</td>
<td>Heating 21C with nighttime setback to 15.6C</td>
</tr>
<tr>
<td></td>
<td>Cooling 24C with nighttime setback to 26.7C</td>
</tr>
<tr>
<td>HVAC System</td>
<td>Default Ideal Loads Air System</td>
</tr>
<tr>
<td>Infiltration</td>
<td>0.20 ACH</td>
</tr>
<tr>
<td>Ventilation</td>
<td>10 L/s/person</td>
</tr>
<tr>
<td>Exterior Wall</td>
<td>Steel Framed Wall Construction with continuous insulation applied to framing</td>
</tr>
<tr>
<td>Floor/Foundation Construction</td>
<td>4&quot; Concrete Slab</td>
</tr>
<tr>
<td>Interior Wall Construction:</td>
<td>Concrete wall with gypsum on either side</td>
</tr>
<tr>
<td>Roof Construction</td>
<td>Insulation Entirely Above Deck (IEAD):</td>
</tr>
<tr>
<td></td>
<td>Continuous Insulation below Membrane</td>
</tr>
<tr>
<td>Window Construction</td>
<td>Simple Glazing System</td>
</tr>
<tr>
<td></td>
<td>U-factor</td>
</tr>
<tr>
<td></td>
<td>SHGC</td>
</tr>
<tr>
<td>Thermal Zoning</td>
<td>Core and perimeter zoning</td>
</tr>
<tr>
<td></td>
<td>Perimeter zone width = 15’ (see Figure 3.3)</td>
</tr>
</tbody>
</table>

#### 3.1.1 Design Parameters

Analysis was performed on 27 design parameters that relate to building form, fenestration, shading, and thermal envelope properties (Table 3.3). Uniform distributions were applied to each parameter within a specified range, since all values are equally plausible design choices. Aspect ratio does not take on a uniform distribution due to a minimum depth constraint of 40 ft, which is discussed later. All parameter distributions are continuous except for the number
of stories, which can only take on integer values. Minimum and maximum values were chosen to allow for exploration of plausible design values; the ranges assigned for each parameter can be found in Table 3.3.

Table 3.3: Design Parameters and Ranges of Sampling

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit Description</th>
<th>Minimum</th>
<th>Maximum</th>
</tr>
</thead>
<tbody>
<tr>
<td>1  Total Building Area</td>
<td>Area (SF)</td>
<td>20,000</td>
<td>100,000</td>
</tr>
<tr>
<td>2  Number of Stories</td>
<td>-</td>
<td>3</td>
<td>6</td>
</tr>
<tr>
<td>3  Depth</td>
<td>Ft</td>
<td>40 ft min; range governed by aspect ratio range</td>
<td></td>
</tr>
<tr>
<td>4  Orientation (rotation)</td>
<td>Degrees</td>
<td>0</td>
<td>180</td>
</tr>
<tr>
<td>5  Roof Insulation</td>
<td>R-value(h-ft2·°F/BTU)</td>
<td>15</td>
<td>50</td>
</tr>
<tr>
<td>6  Roof Color</td>
<td>Solar Absorptance</td>
<td>0.19</td>
<td>0.97</td>
</tr>
<tr>
<td>7  Roof Emissivity</td>
<td>Emissivity</td>
<td>0.86</td>
<td>0.95</td>
</tr>
<tr>
<td>8-11 Window R-value (N,S,E,W)</td>
<td>R-value(h-ft2·°F/BTU)</td>
<td>1.1</td>
<td>4.3</td>
</tr>
<tr>
<td>12-15 Window SHGC (N,S,E,W)</td>
<td>SHGC</td>
<td>0.2</td>
<td>0.6</td>
</tr>
<tr>
<td>16-19 Wall Insulation (N,S,E,W)</td>
<td>R-value(h-ft2·°F/BTU)</td>
<td>R-8</td>
<td>R-40</td>
</tr>
<tr>
<td>20-23 Shading Projection Factor (N,S,E,W)</td>
<td>Percentage of Window Height</td>
<td>5</td>
<td>100</td>
</tr>
<tr>
<td>24-27 Window to Wall Ratio (N,S,E,W)</td>
<td>%</td>
<td>2</td>
<td>90</td>
</tr>
</tbody>
</table>

Two examples of allowable building geometry in this sampling scheme are shown in Figure 3.1. These examples represent the maximum and minimum limits in aspect ratio.

Aspect Ratio = 10; 6 stories  
Aspect Ratio = 1; 3 stories

Figure 3.1: Example building geometries with maximum aspect ratio (left) and minimum aspect ratio (right). Buildings shown have the same floor area.
Window-to-wall ratio, window R-value, window solar heat gain coefficient (SHGC), wall insulation R-value, and shading projection factor were considered independently on each face of the building. Windows were represented as horizontal ribbons on each wall surface. The vertical center of the window defaults to seventy percent of the wall height, until the window is large enough to reach the top of the wall. Windows are offset 0.01 m from the wall edges to satisfy the geometry conventions of EnergyPlus. Window R-value and wall insulation R-value were input to the energy model as an equivalent U-value, the reciprocal of R-value. Orientation, in degrees, was defined as the rotation of the north axis with respect to the building north axis. Insulation of the wall, roof, and slab was represented by varying the insulation thickness with a constant thermal conductivity and converted into an equivalent R-value. Roof emissivity and roof color were represented by the thermal absorptance and solar absorptance, respectively, of the outermost layer of the roof construction. Thermal zones were defined on the bottom, middle, and top floors, with a multiplier applied to the middle floor to represent additional floors. The floor-to-floor height for all stories was 15 feet. The elevation of the thermal zones on the top floor was set at the true height of the building, which is dependent on the randomly sampled number of stories. Elevation of the middle floor was set at the midpoint between the top and bottom floors. The building floor area and number of stories were randomly sampled, and the range of sampling for building depth was conditionally sampled based on the total floor area and number of stories to satisfy two conditions: (1) a depth cannot be less than 40 feet to allow for perimeter and core zoning and (2) the aspect ratio must be between 1 and 10. The minimum and maximum for the depth for sample $i$ was determined by

$$\begin{align*}
\text{Depth}_{\text{min},i} &= 40 \text{ ft if } \left( \frac{\text{Building Area}_i}{\text{Stories}_i} \right) \left( \frac{40 \text{ ft}}{2} \right)^2 < 10 \\
\text{else} & \left( \frac{\text{Building Area}_i}{\text{Stories}_i} \right) \frac{10}{10}
\end{align*}$$

(3.1)

Aspect ratio of 10 would yield a depth less than 40'; therefore set the minimum at 40';

Aspect ratio of 10 would yield a depth greater than 40'; therefore set the minimum at the depth corresponding to an aspect ratio of 10.
The building depth is always less than or equal to the length, thus the maximum depth for all samples is the square root of the footprint, yielding a square form:

\[
Depth_{\text{max},i} = \sqrt{\frac{\text{Building Area}_i}{\text{Stories}_i}}
\]  

(3.2)

A diagram in plan and 3D view with the relevant geometry parameters is shown in Figure 3.2.

![Diagram showing building dimensions and relevant geometry parameters](image)

**Figure 3.2: Rectangular building with relevant geometry parameters. Aspect Ratio is length divided by depth.**

Monte Carlo sampling for the four geometric parameters (building area, number of stories, aspect ratio, and window-to-wall ratio) was done in MATLAB. Coordinates in three dimensions \((x, y, z)\) of every building surface and fenestration surface were calculated for each sample corresponding to the sampled values. The coordinates were exported as comma-separated values (CSV) files for substitution into the base energy model. Random samples for Parameters 4 through 23 were generated with a Perl script that exports a separate file for each parameter with the sampled value and EnergyPlus object type, name, and field number. Another Perl script took as input the original CSV files with geometric coordinates, the Perl-generated files with the sampled values, and the base energy model, and made the appropriate substitution for each set of sampled values to create an Input Data File (IDF) file. The EnergyPlus input was stored in an IDF (text) file. The result was a group of IDFs equal to the number of samples.
3.1.2 Simulation in EnergyPlus

The number of samples, each representing a unique combination of random draws, must be large enough to adequately cover the decision space created by variations in all parameters. The number of Monte Carlo samples was set at 20,000 to be sufficiently large enough to cover the decision space without detailed analysis to determine the minimum sample size. Simulation of 20,000 energy models in EnergyPlus was run in parallel on a 11-node Linux cluster. Nine of the eleven nodes were available, each with two quad-core processors, which allowed 72 simultaneous EnergyPlus runs, significantly decreasing the model run time. A full annual simulation was run for each energy model. Results for annual heating and cooling load for each sample were compiled and analyzed in MATLAB.

3.1.3 Data Processing

Heating and cooling loads were calculated by EnergyPlus and extracted from the output. These loads represent the amount of energy that must be added to or extracted from the conditioned space to meet the thermostat settings. The heating and cooling loads were adjusted by the efficiency or coefficient of performance (COP) to obtain estimates of end-use energy consumption by typical equipment. Average values of efficiency and COP of 0.80 and 3.23, respectively, for the Medium Office Building type as defined for the DOE Commercial Reference Building based on ASHRAE 90.1-2004, were applied to the loads. In addition, the heating and cooling energy consumption estimates were summed to obtain total energy use.

\[
Total\ Energy = \frac{\text{Cooling Load}}{\text{COP}} + \frac{\text{Heating Load}}{\text{efficiency}} \tag{3.3}
\]

The sampled input data also must be processed to represent parameters that can be logically grouped for regression. For example, the orientation parameter allows rotation of 180 degrees, which covers the full range of possible orientations of a rectangular building. With a rotation of 90 degrees, however, the original East face would then face South. Hence, processing allows the conversion of all parameters considered independently on each side to the appropriate cardinal direction, which is dependent on the randomly sampled orientation.
parameter for that run. The angle of the outward facing normal for each external surface determines its orientation.

![Diagram that describes the building orientation by cardinal direction.](image)

**Figure 3.3:** Diagram that describes the building orientation by cardinal direction.

At the base rotation of 0 degrees, the West, South, East, and North orientations were assigned to sides 1, 2, 3, and 4, respectively, as shown in Figure 3.3. Randomly sampled orientation values were used to assign sides to their correct cardinal direction during post processing according to Table 3.4.

<table>
<thead>
<tr>
<th>Building Orientation</th>
<th>West</th>
<th>South</th>
<th>East</th>
<th>North</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 to 45°</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>45 to 135°</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td>135 to 180°</td>
<td>3</td>
<td>4</td>
<td>1</td>
<td>2</td>
</tr>
</tbody>
</table>

**Table 3.4:** Equivalent cardinal direction for properties assigned to Sides 1-4 in energy model input. This data is used for transformation to cardinal direction based on each orientation sample.

### 3.2 Regression Analysis

Multivariate linear regression was performed on results for heating, cooling, and total energy with respect to each of the 27 independent parameters. Of the 20,000 samples, eighty percent of the runs were used to estimate the regression equation. The remaining twenty
percent of runs were used to test the accuracy of the regression equation to predict actual simulation results. The regression produces linear regression coefficients, which were proportional to each parameter’s sensitivity to energy use. The form of the regression equation to predict heating, cooling and total energy is:

\[ y(x_1, x_2, \ldots, x_n) = \beta_0 + \sum_{j=1}^{n} \beta_j x_j \]  

(3.4)

where \( y \) is the predicted heating, cooling, or total energy, \( x_j \) are the parameters and \( \beta_j \) are the corresponding coefficients. It is important to note that each regression model is implicitly based on the fixed inputs in the energy model as well as the location and weather data used for simulation. When a linear regression is performed for heating, cooling and total energy with respect to the 27 design parameters, there is unexplained variance in the models that limits the certainty of any predictions generated with the regression model. The accuracy of the regression models were improved by adding additional terms to the model. Additional terms considered for inclusion in the regression are each a function of one or more of the 27 parameters included in the original sensitivity analysis. For instance:

\[ x_{new} = x_1 x_2 \]  

(3.5)

The form of the regression model stays the same, but the revised multivariate linear regression includes cross product terms. Non-linearities exist due to interactions among parameters in the building model; for example, window SHGC and window area. A unit change in SHGC depends on the amount of window area to which the SHGC change is applied. Another example is a unit change in window to wall ratio having a larger impact on a wall with a large versus a small surface area. The parameters associated with the fenestration objects are especially important in this regard because they play a large role in heat transfer through the building envelope. Additional variables considered for inclusion to capture the interaction between window to wall ratio and other parameters were window area, the product of window-to-wall ratio and wall area as well as U-value and SHGC weighted by the appropriate window area.

Processing of energy model inputs allows parameters to be defined by cardinal direction, but does not account for variation within the defined range of a given cardinal
direction, which represents a range of 90 degrees. Therefore, interaction between orientation and thermal properties of external walls and fenestration were considered to improve the regression. Orientation was sampled on a uniform distribution between 0 and 180 degrees, but is expected to have a non-linear interaction with energy performance: rotation of 0 and 180 degrees should have similar outcomes, with 90 degrees being the most divergent. Therefore, trigonometric functions of the orientation parameter alone and multiplied by other parameters, including aspect ratio, window area, SHGC, window U-value, and shading were investigated as additional variables in the regression model.

Shading projection factor (the ratio of shading projection to window depth) was also found to cause non-linearities in the model. Shading was converted to projection length by multiplying the projection factor by the window-to-wall ratio, which is linearly proportional to window depth due to the constant width of the windows.

3.2.1 Refining the Regression

Forward stepwise regression and standardized regression coefficients were used to determine which variables are most sensitive and are linearly proportional to energy consumption to therefore explain the most variability in the models. Stepwise regression is a method that adds or removes variables one at a time to maximize the improvement in fit of the model according to the $R^2$ value (Morgan and Henrion 1990). The order of a stepwise regression indicates which variables explain a portion of the remaining error as well as the relative importance of the included variables. The stepwise regression and magnitude of parameter sensitivities given by regression coefficients informs which variables should be included in the regression model to minimize the error that cannot be explained by the 27 original design parameters. The original 27 parameters were manually added to the heating regression for Winston-Salem. Then, stepwise regression was performed in MATLAB to determine which variables to add to the model to improve the fit. The results of the stepwise regression, displayed as the remaining root mean square error (RMSE) as a function of included variables, are in Figure 3.4 and Table 3.5.
Figure 3.4: Remaining RMSE as a function of the additional included parameters for the heating regression model in Winston-Salem location. Note that the RMSE plotted on the vertical axis is the remaining error after the original 27 design parameters are added to the regression.

Table 3.5: Variables added to heating regression model for Winston-Salem.

<table>
<thead>
<tr>
<th>Added Term</th>
<th>Variable Name</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>North U-value * Window Area</td>
</tr>
<tr>
<td>2</td>
<td>West Window Area</td>
</tr>
<tr>
<td>3</td>
<td>East Window Area</td>
</tr>
<tr>
<td>4</td>
<td>South Window Area</td>
</tr>
<tr>
<td>5</td>
<td>West U-value * Window Area</td>
</tr>
<tr>
<td>6</td>
<td>South U-value * Window Area</td>
</tr>
<tr>
<td>7</td>
<td>East U-value * Window Area</td>
</tr>
<tr>
<td>8</td>
<td>West SHGC * Window Area</td>
</tr>
<tr>
<td>9</td>
<td>East SHGC * Window Area</td>
</tr>
<tr>
<td>10</td>
<td>South SHGC * Window Area</td>
</tr>
<tr>
<td>11</td>
<td>North SHGC * Window Area</td>
</tr>
</tbody>
</table>

Adding these eleven terms in this example lowered the RMSE of the model by more than a factor of two. In all, forty-five variables were used for the heating regression model and thirty-seven in the cooling regression model. The regression model representing total energy used the union of the two sets, resulting in fifty-one variables. For simplicity, the same set of variables was used for each predictor in all locations. RMSE, average percent error, and $R^2$
are reported for the final regression models tested against the validation set in Table 3.6. For the Miami location, approximately four percent of the validation set had zero annual heating load, which will give infinite percent error for those samples.

Table 3.6: Validation results for refined regression model using additional terms to capture interactions between parameters and non-linear contributions of parameters

<table>
<thead>
<tr>
<th>Location</th>
<th>Miami</th>
<th>Winston-Salem</th>
<th>Albuquerque</th>
<th>Minneapolis</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Heating</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Climate Zone</td>
<td>1A</td>
<td>4A</td>
<td>4B</td>
<td>6A</td>
</tr>
<tr>
<td>RMSE (GJ)</td>
<td>0.8</td>
<td>20.8</td>
<td>30.3</td>
<td>61.3</td>
</tr>
<tr>
<td>R²</td>
<td>0.803</td>
<td>0.976</td>
<td>0.967</td>
<td>0.986</td>
</tr>
<tr>
<td>Average % Error</td>
<td>n/a</td>
<td>6.15%</td>
<td>7.99%</td>
<td>3.58%</td>
</tr>
<tr>
<td><strong>Cooling</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Climate Zone</td>
<td>1A</td>
<td>4A</td>
<td>4B</td>
<td>6A</td>
</tr>
<tr>
<td>RMSE (GJ)</td>
<td>26.2</td>
<td>22.1</td>
<td>26.9</td>
<td>16.2</td>
</tr>
<tr>
<td>R²</td>
<td>0.995</td>
<td>0.986</td>
<td>0.973</td>
<td>0.982</td>
</tr>
<tr>
<td>Average % Error</td>
<td>1.93%</td>
<td>3.43%</td>
<td>4.91%</td>
<td>3.98%</td>
</tr>
<tr>
<td><strong>Total Energy</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Climate Zone</td>
<td>1A</td>
<td>4A</td>
<td>4B</td>
<td>6A</td>
</tr>
<tr>
<td>RMSE (GJ)</td>
<td>25.6</td>
<td>24.4</td>
<td>34.5</td>
<td>56.2</td>
</tr>
<tr>
<td>R²</td>
<td>0.995</td>
<td>0.992</td>
<td>0.984</td>
<td>0.991</td>
</tr>
<tr>
<td>Average % Error</td>
<td>1.88%</td>
<td>2.45%</td>
<td>3.61%</td>
<td>2.67%</td>
</tr>
</tbody>
</table>

Overall, the refined regression models show good fit. The heating, cooling, and total energy regression models, when tested with the independent validation set, yielded an R² greater than 0.96, except for heating in Miami. Interestingly, out of the four locations tested, the R² for total energy consumption is highest for Miami.

The goodness of fit for the regression on total energy, measured by R², RMSE, and average percent error, is better or equal than heating and cooling regressions for all locations (see Table 3.6). In particular, the RMSE for the regression to predict total energy consumption is well below the sum of RMSE in the heating and cooling models for each
location as shown in Figure 3.5. Therefore, the regression model for total energy consumption is a better predictor of actual total energy than the sum of the heating and cooling model predictions. There are several plausible explanations for this behavior which can be explored. First, the better fit could be explained by the larger number of explanatory variables in the total energy regression model (51) versus the heating model (45) and cooling model (37). However, the variables for the heating and cooling regression model were added by stepwise regression from a master set of potential variables until no additional variable would increase model fit. Therefore, the RMSE in the heating and cooling models would not decrease with more variables, so this explanation cannot fully account for the observed behavior. Secondly, if the heating regression model was over or under biased, and the cooling regression model had opposite bias, then this would result in a lower RMSE of total energy than the sum of heating and cooling. Each model is estimated with a least squares regression so validation of the resulting heating and cooling models should not be consistently biased. This lack of systematic bias across all samples can also be seen by inspection of Figure 3.7. However, bias could exist that is not observable in aggregate, e.g. with respect to individual or groups of parameters. Lastly, it follows logically that estimation of an aggregate value would be easier than estimation of its individual components. For example, predicting the hourly heating load every hour for an entire year and summing those predictions would result in much greater error than trying to predict the aggregate annual heating load. Similarly, for the basic regression model used here, it could be expected that the aggregate total energy could be predicted with less error than if heating and cooling were predicted individually and then summed. Further investigation and analysis of the results at finer resolutions of time and parameter values is required to fully understand this behavior.
The cooling regression function has a better fit than the heating regression function in all locations except Minneapolis, where the heating is slightly better. Average percent error for the validation set is lowest at 1.88% in Miami, and highest at 3.61% in Albuquerque. The final regression models for total energy for all four locations yield an $R^2$ value that is above 0.98. Figure 3.6 compares the predictions obtained via multivariate regression and the EnergyPlus simulation results for each sample in the validation set for cooling energy in Albuquerque. Figure 3.7 shows the same plots for heating, cooling, and total energy consumption for all four locations. The strong linear fit obtained in all cases suggests the potential use of the refined regression models in lieu of energy simulation during early design stages. The regression equations give the user approximate estimates of heating and cooling energy consumption values as a function of the 27 key parameters (Table 3.3). Use of the regression models enables easy exploration of the decision space by estimating almost instantaneously the energy consumption.
Figure 3.6: Validation of the cooling regression model for the Albuquerque location.
Figure 3.7: Validation of the heating, cooling, and total energy regression models. Lines represent perfect agreement between the result from EnergyPlus (vertical axis) and prediction by the regression models (horizontal axis).
3.3 Parameter Sensitivity

Monte Carlo simulation is also used for sensitivity analysis, and within the regression framework the regression coefficients can be used to provide a relative and quantitative measure of parameter sensitivity. To compare sensitivity of parameters between locations, first an examination of the distribution of EnergyPlus results for each location is discussed. The following section examines the sensitivity analysis results and reports the observations for the four climate locations tested.

3.3.1 EnergyPlus Results

All locations had identical sampling of parameters, but the range and variability of total energy are unique between locations, as shown in Figure 3.8. Heating values also tended to have more outliers. This holds true at all four locations, though the number of outliers is highest in Minneapolis where the 10% to 90% quantile makes up less than half of the range between the minimum and maximum observed (see Figure 3.9b). Interaction effects among parameters is a key contributor to the outliers for heating and cooling. Interactions between parameters and regression model adjustments are discussed in subsequent sections.
Figure 3.8: Distribution of total heating and cooling energy for the four locations tested. The 25% and 75% quartiles (a) chart and 10% and 90% quantiles (b) are shown. Error bars represent the minimum and maximum observed.
3.3.2 Parameter Sensitivity Methodology

The regression models with only the 27 independent parameters include a coefficient for each parameter, which indicates the relative sensitivity to the heating, cooling, or total energy predictors. Sensitivity to orientation is represented as the sine of orientation, and window and wall R-value is represented as U-value in the model. These modifications are done to
improve model fit, while still keeping each term independent of one another. The units of coefficient $\beta_j$ depend on the units of $x_j$, all of which do not have the same order of magnitude (e.g., building area of 30,000 SF and window solar heat gain coefficient of 0.5). Standardized regression coefficients (SRCs) can be used to compare coefficients with different units. Linear regression coefficients are normalized into SRCs to permit comparison. SRCs are obtained by multiplying each coefficient by the ratio of the estimated standard deviations of $x_j$ to $y$ (Morgan and Henrion 1990 p. 208), as shown in Equation 3.6.

$$U_{SRC}(x_j, y) = \frac{\beta_j \times s_j}{s_y} \quad (3.6)$$

Normalized values are shown in Table 3.7 for three parameters with respect to Minneapolis heating energy consumption.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Parameter Range [min, max]</th>
<th>$\beta_j$ Regression Coefficient</th>
<th>$s_j$ Input Std Dev</th>
<th>SRC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Area (SF)</td>
<td>[20000, 100000]</td>
<td>1.20E+07 J/SF</td>
<td>23094 SF</td>
<td>0.541</td>
</tr>
<tr>
<td>Window-to-Wall Ratio N</td>
<td>[0.02, 0.90]</td>
<td>6.19E+11 J/% Window</td>
<td>0.254 % Window</td>
<td>0.306</td>
</tr>
<tr>
<td>Shading Projection Factor S</td>
<td>[0.05, 1.00]</td>
<td>8.17E+10 J/Shading PF</td>
<td>0.274 Shading PF</td>
<td>0.044</td>
</tr>
</tbody>
</table>

In the Minneapolis results, the building area regression coefficient is relatively small, but the parameter values themselves are large. The opposite can be observed for the window-to-wall ratio and shading projection factor. By normalizing the regression coefficients by the standard deviation of the sampled parameter values, the effects due to the scale of the parameters are eliminated. When comparing the SRCs in Table 3.7, building area is the most sensitive with an SRC of 0.541, followed by window-to-wall ratio with an SRC of 0.306, and only a relatively small contribution by shading projection factor. Note that the standard deviation of a variable that is uniformly distributed is directly proportional to the difference between its minimum and maximum values. Results for the SRCs for heating, cooling, and
total energy for the four locations are shown in Figure 3.10, Figure 3.11, Figure 3.12, and Figure 3.13.

**Figure 3.10:** Parameter sensitivity based on the Miami regression model. Parameters are ordered from top to bottom based on their influence on total building energy consumption (labeled ‘Total’).
Figure 3.11: Parameter sensitivity based on the Winston-Salem regression model. Parameters are ordered from top to bottom based on their influence on total building energy consumption (labeled ‘Total’).
Figure 3.12: Parameter sensitivity based on the Albuquerque regression model. Parameters are ordered from top to bottom based on their influence on total building energy consumption (labeled ‘Total’).
Figure 3.13: Parameter sensitivity based on the Minneapolis regression model. Parameters are ordered from top to bottom based on their influence on total building energy consumption (labeled ‘Total’).

3.3.3 Results

Parameter ranking determined by their influence on heating and cooling loads is largely similar across the four locations, with total energy sensitivity depending on the relative influence of heating and cooling. Building floor area is the most sensitive parameter for cooling, and one of the most sensitive for heating; as a result, it is also the most sensitive parameter for total energy. In decreasing levels of sensitivity to total energy, the number of stories, window-to-wall ratio, and aspect ratio all follow building area, though in slightly different order depending on the location. As larger aspect ratio (i.e., more rectangular than square) and larger heights increase the amount of surface area for the same building area,
they both increase the heating and cooling loads for all locations. In Minneapolis, Albuquerque and Winston-Salem, the ranking of window-to-wall ratio by cardinal direction was the same, with North, West, East, and then South in descending order. In Miami, the East, West and South had similar sensitivities, with North being much less sensitive. This is consistent with the trends for cooling in the other locations, which is logical because the total energy in Miami is mostly cooling load. After the shape parameters and the window-to-wall ratio, window properties are the next most sensitive to total heating and cooling energy use. Again sensitivities in Miami differ; SHGC comes next in Miami, while U-value is more significant than SHGC for the other locations. Orientation, or rotation of the building, is generally the next most sensitive parameter following window properties, and in locations with heating (i.e., all but Miami), wall U-value on the north face and roof R-value tend to follow. The results for Miami are somewhat anomalous compared to the other locations, where sensitivities to shading are much higher than window or wall U-value. For Miami, roof color was the sixteenth most sensitive parameter out of 25 parameters, while it had very little effect in the other locations.

The signs of the SRCs indicate the direction of sensitivity. An input parameter increase with a positive SRC will result in increased energy use, while an input parameter increase with a negative SRC will result in decreased energy use. Some parameters affect heating and cooling in the same direction, such as window-to-wall ratio, aspect ratio, and the number of stories. Both window SHGC and shading have opposite effects on heating and cooling, which causes their sensitivity to total energy use to be much lower because the heating and cooling effects are offset by one another. This highlights the importance of performing annual simulation, because the relative weight of heating and cooling will determine the optimal parameter value. SHGC, for example, is not as intuitive as other parameters like window area, which are known only to increase energy use. Roof emissivity (e.g., application of low-e paint applied to a roof surface) showed very low sensitivity in all locations, which could be partly due to the small range of values in the sampling for this parameter.
Grouping the results for standardized regression coefficients by heating, cooling, and total energy, it is possible to see the trends between climate locations (see Figure 3.14, Figure 3.15, and Figure 3.16 for plots of the most sensitive parameters). With respect to the heating load, SRC results for Minneapolis, Winston-Salem, and Albuquerque are consecutively ordered by either ascending or descending sensitivity for almost all parameters. For example, in Minneapolis greater sensitivity to heating load is observed for building area, aspect ratio, and number of stories. The Winston-Salem location, followed by Albuquerque, has descending sensitivity to these parameters. These parameters all contribute to the heating load, whose effects are exaggerated in colder climates. Window-to-wall ratio and window U-value on the North side have the opposite trend, with Albuquerque being the most sensitive, followed by Winston-Salem and then Minneapolis. This result indicates that the parameters governing the fenestration on the North make a greater contribution to the variability in the heating load in Albuquerque than in Minneapolis.

Figure 3.14: Standardized regression coefficients for heating load at all four locations. Parameters are ordered from top to bottom based on their influence on energy consumption in Winston-Salem.
The standardized regression coefficients are more consistent between locations for the cooling load, as shown in Figure 3.15. Building area dominates the sensitivity of all parameters in all locations. The building area parameter in Albuquerque contributes less to total variability in the cooling load in comparison to other locations. Therefore, sensitivities in the other parameters are higher in Albuquerque, including window-to-wall ratio, shading, and window U-value and SHGC. More detailed analysis of the energy model results are required to understand the contributing factors to this result, but it is worth noting that Albuquerque is the only dry climate tested, and presumably has lower latent cooling load due to ventilation and infiltration at the same outside dry bulb temperature.

![Figure 3.15: Standardized regression coefficients for cooling load at all four locations. Parameters are ordered from top to bottom based on their influence on energy consumption in Winston-Salem.](image)

Figure 3.16 shows the SRCs for total energy in the four climate locations and illustrates the relative influence of heating and cooling. For example, the Miami location shows high sensitivity to building area and relatively low sensitivity to other parameters, similar to the observed trends for cooling. Likewise, the Minneapolis location shows high sensitivity to
aspect ratio, the number of stories, and the north window-to-wall ratio, similar to the trends for heating.

![Graph showing standardized regression coefficients for total energy consumption at four locations.](image)

**Figure 3.16:** Standardized regression coefficients for total energy consumption (for both heating and cooling) at all four locations. Parameters are ordered from top to bottom based on their influence on energy consumption in Winston-Salem.

While the raw coefficients will have different units and cannot be compared against one another (e.g., window-to-wall ratio and wall R-value), the raw coefficients of the same parameter can be a useful comparison between locations. For example, while the SRC for window U-value on the North side is greatest in Albuquerque, the absolute value of change in heating load in gigajoules per unit change in U-value is not necessarily greatest in Albuquerque because the SRCs are normalized by the standard deviation of the heating load, which is much greater in Minneapolis (see Figure 3.9b). Comparisons of raw coefficients for window U-value, window-to-wall ratio, building area, and aspect ratio are shown in Figure 3.17 and Figure 3.18.
Building Area

Aspect Ratio

(a)

Heating

Cooling

Total

GJ Heating Energy / Building Area in square meters

GJ Heating Energy / Aspect Ratio

GJ Cooling Energy / Building Area in square meters

GJ Cooling Energy / Aspect Ratio

GJ Total Energy / Building Area in square meters

GJ Total Energy / Aspect Ratio

Minneapolis  Winston-Salem  Albuquerque  Miami

Figure 3.17: Comparison of raw linear regression coefficients showing sensitivity of building area and aspect ratio at all four locations. Coefficients are presented for heating (a), cooling (b), and total energy consumption (c).

The absolute differences in sensitivity are shown without normalizing the coefficient by the standard deviation of the output (heating, cooling, or total energy). Aspect ratio and total building area are sensitive in all climates as shown earlier, but they also are much more pronounced in warm climates like Miami and cool climates like Minneapolis (see Figure 3.17). There is also a large difference in sensitivities for the same parameter facing different cardinal directions. In each location, the differences between cardinal directions are the same. For example, the window-to-wall ratio on the East and West facing walls exhibit the greatest sensitivities, followed by South and then North walls, to cooling (see Figure 3.18b).
Figure 3.18: Comparison of raw linear regression coefficients for window U-value and window-to-wall ratio at all four locations. Coefficients are presented for heating (a), cooling (b), and total energy consumption (c).
3.3.4 Validation

The validation set made up of approximately 20% of the 20,000 samples is used to calculate the error observed by the regression predictions. Error metrics utilized in this analysis include the root mean square error (RMSE), $R^2$, and average percent error for each location. Plots for heating, cooling, and total energy that compare the EnergyPlus simulation result to the value predicted by the multivariate linear regression are shown in Figure 3.19. The various error metrics are reported in Table 3.8.

Table 3.8: Validation results for the multivariate linear regression on heating, cooling, and total energy consumption to obtain SRCs, which measure relative parameter sensitivity.

<table>
<thead>
<tr>
<th>Location</th>
<th>Miami</th>
<th>Winston-Salem</th>
<th>Albuquerque</th>
<th>Minneapolis</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Heating</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Climate Zone</td>
<td>1A</td>
<td>4A</td>
<td>4B</td>
<td>6A</td>
</tr>
<tr>
<td>RMSE (GJ)</td>
<td>1.2</td>
<td>65.4</td>
<td>85.1</td>
<td>222.9</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.498</td>
<td>0.762</td>
<td>0.743</td>
<td>0.816</td>
</tr>
<tr>
<td>Average % Error</td>
<td>n/a</td>
<td>19.38%</td>
<td>22.80%</td>
<td>12.58%</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Location</th>
<th>Miami</th>
<th>Winston-Salem</th>
<th>Albuquerque</th>
<th>Minneapolis</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Cooling</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Climate Zone</td>
<td>1A</td>
<td>4A</td>
<td>4B</td>
<td>6A</td>
</tr>
<tr>
<td>RMSE (GJ)</td>
<td>55.0</td>
<td>38.1</td>
<td>46.8</td>
<td>29.0</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.977</td>
<td>0.959</td>
<td>0.917</td>
<td>0.941</td>
</tr>
<tr>
<td>Average % Error</td>
<td>4.25%</td>
<td>6.26%</td>
<td>9.23%</td>
<td>7.44%</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Location</th>
<th>Miami</th>
<th>Winston-Salem</th>
<th>Albuquerque</th>
<th>Minneapolis</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Total Energy</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Climate Zone</td>
<td>1A</td>
<td>4A</td>
<td>4B</td>
<td>6A</td>
</tr>
<tr>
<td>RMSE (GJ)</td>
<td>55.1</td>
<td>71.0</td>
<td>91.9</td>
<td>223.2</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.977</td>
<td>0.932</td>
<td>0.886</td>
<td>0.859</td>
</tr>
<tr>
<td>Average % Error</td>
<td>4.24%</td>
<td>7.18%</td>
<td>9.86%</td>
<td>10.23%</td>
</tr>
</tbody>
</table>

The regression fits for heating are worse than cooling in all locations. $R^2$ ranged from 0.498 to 0.816 for the heating regression, and from 0.917 to 0.977 for the cooling regression. The regression for total energy yielded an $R^2$ from 0.859 to 0.977. The goodness of fit for the
regression on total energy, measured by $R^2$, RMSE, and average percent error, is better than the average of heating and cooling for all locations. In locations where heating or cooling dominated the total energy load, the regression on the dominant load was better in that location than all others. For example, Miami is dominated by the cooling load, and the cooling regression yielded the highest $R^2$ of 0.977. Likewise, the heating regression for Minneapolis was the best with an $R^2$ of 0.816. Additionally, there is less unexplained variability in the total load regression than the sum of heating and cooling. This trend was also seen in the refined regression models; discussion on this observation and potential explanations can be found in section 3.2.1. The fit of the regression models with only the 27 parameters used in Monte Carlo analysis is worse than the models with additional terms to capture interactions between parameters and non-linearities. However, they allow the user to examine the sensitivity of each parameter independently of one another.
Figure 3.19: Validation of linear regression to predict energy consumption compared to EnergyPlus results. The lines represent perfect agreement between the EnergyPlus result on the vertical axis and the predicted value by the regression on the horizontal axis.
3.4 Number of Samples

In this analysis, the 20,000 simulation runs are executed to provide adequate coverage of the decision space. Such a large number of runs are enabled by the available parallel computing capability, which was used to execute 72 simulations simultaneously. This allowed completion of all runs in approximately 13 hours. When conducting the Monte Carlo analysis, the number of samples is typically decided by balancing computational effort with a measure of variability, such as the variance in the mean results (Morgan and Henrion 1990). Past studies using Monte Carlo analysis with building simulation tools have limited the number of runs to a couple hundred or up to 1000 (Burhenne et al. 2010), though many have used very simplified simulation tools. A final step in the analysis involved analyzing the incremental benefit of additional model runs.

The generalized regression equation for the rectangular form in the preceding example is based on a multivariate regression on 80% of 20,000 total samples, or approximately 16,000; the remaining 4,000 samples were used during the validation exercise. The breakdown of total runs into the estimation and validation sets was varied to observe the change in error with fewer samples. Samples were randomly assigned to either the validation or estimation set based on specified probabilities. The probability of being assigned to the estimation set was gradually increased to demonstrate how the error changes as a function of the number of runs used to build the regression model. A Monte Carlo simulation was conducted for Winston-Salem and the results for average error and standard deviation of average error are shown in Table 3.9. In addition, the change in average error versus sample size is shown in Figure 3.20. In each case, the validation set consisted of the remaining samples, or 20,000 minus the number of estimation samples.

The regression equations for heating, cooling, and total energy have 45, 37 and 51 variables, respectively. Figure 3.20 shows a sharp decrease in prediction error between 50 and 200 samples and a leveling off between 500 and 1000 samples. To formulate a relatively accurate regression equation, much fewer samples than 20,000 are needed for a problem similar to the generalized rectangular problem discussed in the previous section.
Table 3.9: Average and standard deviation of percent error for heating, cooling, and total energy regression models for various sample sizes. Multivariate regression performed with different numbers of samples in the estimation set. Average error and standard deviation of average error based on comparison to the validation set are shown for heating, cooling and total energy load.

<table>
<thead>
<tr>
<th>Number of Estimation Samples</th>
<th>Average Percent Error</th>
<th>Standard Deviation of Average % Error</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Heating</td>
<td>Cooling</td>
</tr>
<tr>
<td>62</td>
<td>18.33%</td>
<td>5.87%</td>
</tr>
<tr>
<td>78</td>
<td>9.91%</td>
<td>4.73%</td>
</tr>
<tr>
<td>107</td>
<td>9.15%</td>
<td>4.55%</td>
</tr>
<tr>
<td>210</td>
<td>7.33%</td>
<td>3.78%</td>
</tr>
<tr>
<td>402</td>
<td>7.00%</td>
<td>3.57%</td>
</tr>
<tr>
<td>602</td>
<td>6.76%</td>
<td>3.56%</td>
</tr>
<tr>
<td>802</td>
<td>6.51%</td>
<td>3.50%</td>
</tr>
<tr>
<td>998</td>
<td>6.53%</td>
<td>3.48%</td>
</tr>
<tr>
<td>1967</td>
<td>6.34%</td>
<td>3.44%</td>
</tr>
<tr>
<td>2979</td>
<td>6.32%</td>
<td>3.44%</td>
</tr>
<tr>
<td>16025</td>
<td>6.15%</td>
<td>3.43%</td>
</tr>
</tbody>
</table>

Figure 3.20: Average prediction error of the validation set versus the number of estimation samples used to generate the multivariate regression, with error bars representing one standard deviation. Results are drawn from the simulation presented in the previous section for total energy in Winston-Salem.
Chapter 4 Discussion

This work was motivated by the lack of building energy information available during early stages of building design. To fill the gap, a simple regression model with predictive capability and a rigorous sensitivity analysis of key building design parameters have been developed. The analysis is based on a generic office building located in four locations: Miami, Winston-Salem, Albuquerque, and Minneapolis. Remaining questions pertain to how one would use the results in the design process, and what further research could be done to build on this work.

4.1 Use as a Design Tool

The standardized regression coefficients are an indication of sensitivity across the range of each input while varying all other variables simultaneously. All buildings are not perfect rectangles, though many buildings, especially commercial ones are variations of a box. In more complex design situations, approximating a design as a single or multiple rectangular forms could further the usefulness of the regression model, with an appropriate understanding of the effects of the approximations. It is worth pursuing whether such a model based on a specific building type in a given climate location would be useful and insightful to designers. Rank order sensitivities of key parameters could inform design strategy. Such information can yield energy-related insight before starting design or during early design stages. Knowledge of parameter sensitivity can inform design by quantifying tradeoffs between parameters, and focusing attention on the parameters that are most likely to affect the energy goals of the project. The regression model can be used as a quick way to get feedback on early design decisions pertaining to the modeled parameters. With a simple regression equation, different design schemes can be compared against one another.

At a smaller scale, variations in individual and groups of parameters could be isolated and their result on energy loads estimated within a margin of error. Such capability could have immense value for designers in early stages looking for rapid feedback on energy performance without building or modifying a full-scale energy model. As stated previously, point estimates of heating and cooling load are by themselves can be ambiguous during
conceptual design. However, the regression model can quickly show an increase or decrease in energy consumption over a wide range of scenarios and offers a robust technique to analyze tradeoffs between parameters and changes to their values. Parametric analysis could be conducted easily using the regression model to examine one-at-a-time sensitivity. For example, the regression model can be used to examine the effect of increasing the R-value (or decreasing the U-value) of the windows. Two scenarios, one with 30% windows and another with 15% windows computed with the regression model are shown in Figure 4.1.

![Graph of Total Heating and Cooling Energy vs. Window R-value for two scenarios](image)

**Figure 4.1:** Parametric Analysis of window R-value for total heating and cooling energy in Albuquerque for two scenarios based on the regression model.

Using the tools developed in this research, early design in mixed climates can provide useful insights. For example, measures commonly considered to be energy efficient (e.g., additional insulation) have mixed effects on heating and cooling. As a result, the effect on annual energy consumption is not always intuitive.
4.2 Further Work

To implement the regression model in the design process, an interface that allows exploration of potential designs and their impact on energy consumption needs to be developed. Formal search techniques can be applied to the regression model to find optimal combinations of parameter values, or to explore multiple near-optimal solutions using the method of modeling to generate alternatives (Brill et al. 1982). Methods to communicate the results and facilitate utilization within design teams needs to be explored. Sensitivity analysis using the regression model can be tailored to specific design questions. For example, if only a few parameters are of interest, sensitivity analysis can be applied to a subset of parameters. Another application is to impose constraints on the ranges of the design parameters and rerun the Monte Carlo simulation to explore the sensitivity within the design decision space available to a specific project. This could be especially valuable because the SRCs can be dependent on the initial range given (Capozzoli et al. 2009), so further refinement of the sensitivities for the portion of design decision space available to a specific project would give better feedback than the generalized sensitivities based on wider ranges.

4.3 Conclusion

In this application, sensitivity analysis and regression analysis are applied to model a rectangular building. Parameters considered include the size and shape, as well as rotation, roof and wall insulation, window R-value, SHGC and shading. Standardized regression coefficients (SRCs) can provide valuable information to designers regarding the relative impact each parameter will have on heating and cooling loads. In the four locations tested—covering some of the extremes of climate in the continental U.S.—SRCs for the same design parameters varied widely from one another. This result highlights the need for climate-sensitive design. Also, the sensitivity of the same parameter on different building faces is different, which can also inform design prioritization. Monte Carlo simulation also provides rich data for the creation of a multivariate regression model that can be used to quantify energy savings and effects without running more simulations. The methods developed in this research allow designers in the early design stages to have access to quantitative energy data,
but without the high level of technical expertise often needed to create and run a building simulation model. This framework can be applied to other performance indicators such as peak heating and cooling loads or daylighting in a very similar manner. Additionally, the sampling and substitution of values through Perl scripts has the flexibility to include many other parameters. Finally, only 500 to 1000 runs are required to conduct sensitivity and regression analysis, which does not require the use of high performance parallel computing. The quantitative feedback generated by the regression and sensitivity analysis enables designers at an early stage, when changes are easier to make and when more energy savings are available, to support decision-making for energy efficiency.
REFERENCES


