

## ABSTRACT

AVR, AZHAGAN. Characterizing Driving Behavior by using LIDAR and GPS through Traffic Stream Models. (Under the direction of Drs. Rachana Gupta and Nagui Roupail).

This research consists of two parts, the first part proposes a low-cost system to capture spatial gap between vehicles and a method to process the raw data by filtering the outliers using a novel filtering procedure. Multiple sensors and modules are integrated to form the system. The sensors used are compact, lightweight, low-cost and have low power consumption. A single beam 1-Dimensional Light Detection and Ranging (LIDAR) was used for capturing the gap between vehicles, a Global Positioning System (GPS) to map each data point with a timestamp and positional data, and a camera to capture video data with an overlay of date, time, distance and speed in real-time. The combined data frequency of LIDAR and GPS is around 3Hz and the camera records at 30 frames per second. The filtering procedure performs a 2-stage process comprising of the Autoregressive Integrated Moving Average (ARIMA) prediction modeling in stage one and mean-filtering in stage two. The captured data is stored in a Raspberry Pi module, which is later processed by using the filtering technique to obtain the data with the least outliers. The overall system has enabled to capture gap between vehicles and speed of the vehicle at a very low cost. The other part of the thesis concentrates on the usage of dynamically collected local density data and using it to characterize driving behavior. The motivation for this research was to overcome the lack of longitudinal evolution of density data while using fixed position sensors. Throughout this research, only dynamically collected naturalistic data was used, free of any controlled experiment biases. Data were collected on arterial and freeway segments, of 2 and 4 miles long respectively. The second part of the thesis describes three important analyses, the first involving using gap between vehicles to estimate the local density and using local density to identify the density of a specific location in a corridor, by just driving through that corridor. The second considers the relationship between instantaneous speed - local density under different regimes of the Wiedemann car-following model, to characterize driving behavior. Finally, two well-known macroscopic traffic flow models like Greenshields and Modified Greenberg are used to investigate the characteristics of the dynamically collected instantaneous speed - local density data to standard models generated using steady-state aggregated speed flow density values, which is also used to characterize the driving behavior based on the metrics of HCM-6 and HCM2000 model.

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Characterizing Driving Behavior by using LIDAR and GPS through Traffic Stream Models

by  
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North Carolina State University  
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requirements for the degree of  
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## **DEDICATION**

I dedicate this work to my parents Manjari Avr and Raviraj Jambulingam, and my sister Anjana Avr and my friends from LICET and NCSU for their never-ending support and belief in me.

## **BIOGRAPHY**

Azhagan Avr was born and brought up in Chennai, India. He did his schooling in St. Michael's Academy, Chennai, India. In the year 2016 he graduated with an undergraduate degree in Electronics and Communication from Loyola ICAM – College of Engineering and Technology (LICET) affiliated to Anna University, Chennai, India. His interests in projects and excellence in academics earned him an opportunity to be an exchange student at Comillas Pontifical University, Madrid, Spain in June 2015. As a research scholar, he performed a month-long research in amplifier stability. In February 2016, he was given an opportunity to perform his final year project in Hochschule Heilbronn, Heilbronn, Germany. He worked on integrating an industrial Laser scanner in an autonomous farming vehicle.

During his undergraduate studies, he served as the Vice President and President of the national level symposium conducted by the ECE department in the year 2014 and 2015 respectively. After graduating in 2016 he joined Department of Transportation in Indian Institute of Technology Madras (IITM), Chennai, India as a Project Associate. There, he was bridging the gap between Civil and Electrical engineering through his product development and coding skills. In Fall of 2017, Azhagan enrolled as a master's student in North Carolina State University (NCSU), Raleigh, USA. Since then he has been working in Institute for Transportation Research and Education (ITRE), Raleigh, USA as a Graduate Research Assistant on a variety of state funded projects that involve inter-disciplinary fields of Transportation and Electrical engineering.

## ACKNOWLEDGMENTS

This thesis presents my contribution in **Characterizing Driving Behavior by using LIDAR and GPS through Traffic Stream Models**. This research was an extension of the ARPA-E project carried out at ITRE.

I would like to thank **Dr. Nagui Roupail and Thomas Chase** for trusting me and giving me the opportunity to work on the ARPA-E project. Dr. Roupail has been a constant guidance throughout my research and I would like to express my gratitude for his patience, enthusiasm and for sharing his immense knowledge. **Dr. Shams Tanvir** has played a vital role in my entire thesis and has always been available to answer any questions that I have had and has always made time for me and been patient in explaining the technical nuances.

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# 1 INTRODUCTION

## 1.1 Problem Definition and Motivation

In the 1970s, ropes were used to measure the spatial gap between vehicles. But, nowadays with advances in technologies, these are collected through a variety of state-of-the-art techniques. Researchers have used video data to identify the gap between vehicles [1]. Some researchers have used GPS data for speed capturing but also for estimating the gap between vehicles using positional data [2]. But in the techniques mentioned above, the spatial gap between vehicles is being estimated and not captured; hence there is always scope for inaccuracy in such techniques.

Hence a probable solution to collect the gap between vehicles would be using sensors like Light Detection and Ranging (LIDAR) or Radio Detection and Ranging (RADAR). At present, almost all new vehicles are equipped with sensors like LIDAR or RADAR for Advanced Driver Assistance Systems (ADAS). But data from these sensors are not accessible to users through the On-Board Diagnostics (OBD) port. Hence this research would be useful for future studies that use vehicles to collect spatial gap between vehicles like car-following data for various research practices.

One of the common methods of collecting traffic flow and vehicle volume data in a segment is through static or stationary infrastructure sensors. Some of the commonly used methods of data collection are stationary video cameras or vehicle counting sensors like the Remote Traffic Microwave Sensor (RTMS) [3]. These methods, however, lack variation in space over the segment as the sensors are fixed to a location and the collected data is usually averaged out to estimate the information about the entire segment. That is often the reason macroscopic models use average speed and average density. Also, Installations and reinstallations of these stationary sensors in different locations are expensive and difficult to maintain [4].

An alternative solution to collect data in a cost-effective way would be through a dynamic method where the sensor is in motion. Some researchers have used devices that collect vehicular speed data from the On-Board Diagnostics (OBD) port [5], and some have used Global Positioning System (GPS) devices to log vehicular speed and positional data from probe vehicles [6]. But these dynamic methods of data collection cannot report vehicle volume or occupancy information.

A promising method would be to combine one of the above-mentioned approaches i.e. using GPS or OBD data to collect vehicular speed along with a sensor that collects spatial gap

between vehicles from a moving vehicle. This can be achieved by using LIDAR or RADAR. Similar setups are found on commercially available autonomous vehicles (AV). Nowadays vehicles are equipped with different sensors to provide different information to the driver, like LIDARs are used to detect and measure the distance of objects or vehicles from an AV [7] and GPS modules are used in the in-built navigations systems for positional data. LIDAR and RADAR can be expensive, but this study uses a low-cost way to collect spatial gap between vehicles using LIDAR. From the instantaneous spatial gap between vehicles captured, “local density” can be calculated, along with the characterization of the entire lead vehicle trajectory while that vehicle is in range.

The local density is generated based on the driver’s reactions to the leading vehicle, that is, the dynamic data collected pertaining to the driver of the following (equipped) vehicle across the corridor. The advantage of the naturalistic approach is that information is collected without any bias or any controlled conditions. One purpose of this research is to demonstrate the effectiveness of this approach.

The motivation for this research is to develop a low-cost, dynamic and a prototype with good accuracy that would capture spatial gap between vehicles, unlike the traditional stationary devices that capture gap between vehicles information from stationary positions. The main motivation of this research was to capture data in an independent, naturalistic and dynamic way and characterize the driving behavior with the captured gap between vehicles and vehicular speed. Some of the questions that motivated me to pursue my research on this topic are listed below;

- a) Can a low-cost LIDAR capture accurate reading while in motion?
- b) Is the chosen ARIMA model the most appropriate to the application?
- c) Are the results of the 2-stage filtering process promising?
- d) What is the need for local density data through dynamic data collection?
- e) How does classifying speed-density data into regimes help in characterizing driving behavior?
- f) Can some of the existing macroscopic models represent the dynamic data?

A brief on some existing techniques used to collect spatial gap between vehicles and a review of past studies related to static and dynamic sensors are discussed in the following section.

## 1.2 Literature Review

As mentioned in the previous section, various techniques have been used to estimate the spatial gap between vehicles. An image processing tool used to classify vehicles in a mixed traffic scenario is used to estimate the spatial gap between vehicles [1]. But the disadvantage of using cameras for measuring the gap between vehicles is that the camera needs to be calibrated for every location the camera is being installed, the following study shows a method that can be used to calibrate the camera [8], which is an added challenge. Apart from calibration, there are other challenges faced when stationary sensors are used like restrictions on installations, environmental factors and cost of installations and reinstallations [4]. Hence dynamic data-driven methods are the way to move forward [9].

An alternative solution to stationary sensors could be using GPS devices to estimate the spatial gap between vehicles. The research proposes that positional and speed data obtained from GPS traces are cost-effective and accurate [10]. Using the positional data of two known vehicles the gap between vehicles is estimated [2]. This method of dynamic data collection brings in the factor of dependency on the data from the leading vehicle which rules out collecting data from different commercial users independently, as at any given time 2 vehicles are needed for data collection.

In the methods mentioned above the spatial gap between vehicles, are not captured directly but they are estimated. Hence the methodology used in this research involves a naturalistic approach of data collection that is independent of other vehicles for the data.

RADAR and LIDAR both have a similar functionality except that LIDAR uses light waves and RADAR uses radio waves to measure distance. Both these devices have their set of advantages and disadvantages, but both the sensors are widely used in the latest vehicles [11] for ADAS. This research uses a LIDAR device for measuring the distance.

Two different types of LIDAR such as 1-Dimensional (1D) and 2-Dimensional (2D) LIDAR were tested. The 3-Dimensional (3D) LIDAR was not tested as mapping the environment into a 3D plane was not the scope of this research and they are very expensive. The 2D sensor can map an entire 2D plane by rotating 360 degrees, but the major drawback is that the 2D sensor has a very low sample rate because the object that the sensor was tracking has moved significantly before the sensor completes the rotation and the accuracy decreases with the object in motion, but the 2D sensor works best for mapping a stationary 2D plane. Due to the lack of compatibility of

the 2D sensor with the intended application, the 1D sensors were later considered. 1D sensors do not map the environment, nor rotate 360 degrees, but they produce a singular light beam at a frequency between 500 – 1000 Hz which is then bounced off the surface of the leading vehicle and the reflected beams are captured and distance is measured. They are less expensive compared to the other LIDAR devices, the LIDAR used here is priced at \$125 and the device is small, low power and compact.

ARIMA is a prediction model that is used for time series forecasting [12]. The model can predict a value based on the selected range of values. ARIMA is used to predict the spatial distance between cars. The mean filter also known as an averaging filter is used to filter the data that is rejected by the ARIMA prediction.

Various methods have been employed to collect microscopic information like speed and headways and macroscopic information like vehicle occupancy, vehicle flows, and so on with static sensors. One such method was to use an offline image processing tool to classify vehicles in a mixed traffic scenario and gather microscopic information like speed and headway and macroscopic characteristics like vehicle trajectories, vehicle occupancy, and so on [3]. The drawbacks of similar systems are that the area covered by these sensors is only hundreds of feet wide i.e. they lack spatial variation over the segment and the installation and maintenance cost would be expensive as well.

One of the alternative solutions for static data collection was the data logging from the OBD port, and the OBD port provides a lot of vehicular information like speed, acceleration, engine RPM and so on. Various researches have been performed using OBD data to study driving behavior [13], remote logging of vehicular data [14] and so on. Like the speed data from the OBD port, the GPS devices are used to capture vehicular speed through satellites. GPS data has been used to model low-speed urban roads based on operating speed [15]. Alternatively, apart from collecting speed data, researchers have used positional data from the GPS to calculate the gap between vehicles [2], but the disadvantage of this system is that it depends on the leading vehicle to have the GPS device as well. But by using a LIDAR/RADAR along with the GPS will remove the dependency of every vehicle to have the GPS device. LIDAR and RADAR have their own set of pros and cons, but they are the two most widely used devices to measure spatial gap between vehicles [11].



The car is assumed to be following when the driver is unable to drive at the desired speed and is constrained by the leading vehicle [16]. The car-following model being used is a psychophysical model designed by VISIM also called a Wiedemann model. The enhanced version of the 1974 model, proposed by Wiedemann and Reiter in 1992 [17]. Wiedemann model being a microscopic car-following model that is entitled to a single driver's behavior makes use of dynamic information such as headway, speed of the follower and speed of the leader vehicle. In Wiedemann car-following model, the thresholds are defined for every speed, so it helps to identify the driving behavior at different speeds [18]. Through this model, each data point is categorized into a regime.

Various macroscopic models like Greenshields, Modified Greenberg, etc. are used for investigating the quality and closeness of the dynamic speed-density data. These models are usually fitted to data that are collected using static sensors over time at a given location with temporal variation but lacking variation in space over the segment. This research explores how the models would represent dynamic data.

Hence from the literature mentioned above, some systems that capture speed and vehicle occupancy from static locations lack the evolution of density in space. Some dynamic systems with GPS or OBD devices capture speed data but do not capture density data. But methods used to collect speed and density data from the GPS requires a controlled environment and are dependent on other vehicles to house similar data capturing devices to obtain speed and density data. Hence this research proposes to use LIDAR and GPS to capture the gap between vehicle and speed of the equipped vehicle, respectively.

### **1.3 Methodology**

This research discusses a cost-effective method to collect the distance between two vehicles using LIDAR, and a method to process and filter the outliers from the raw data. A 2-stage process which involves ARIMA prediction modeling in stage 1 and mean-filtering in stage 2 to filter out the noise in the raw data from the sensor. When the manufacturers make the raw sensor data available to users through the OBD port, the same method of noise removal can be implemented, but due to its unavailability, an external sensor is used.

This research discusses three methods of investigation using the data collected: (a) a numerical analysis of the local density data, (b) classification of the differential speed-local density

domain into different car-following regimes and (c) a comparison of various traditional macroscopic models with the collected speed-local density data. In fact the data streams generated in this work resemble those likely to be produced by autonomous and connected vehicles, thus providing a preview of possible applications of such data for enhanced mobility and safety purposes.

#### **1.4 Structure of the Thesis**

Following the introduction in Chapter 1, the system integration and data collection procedures are explained in Chapter 2. Then, in Chapter 3 the data filtering process is explained in detail. Chapter 4 comprises the theory of various traffic flow models, like microscopic and macroscopic models. Chapter 5 explains the three methods of data investigation through analysis and results. In the last chapter, findings and future work are discussed.

## 2 SYSTEM INTEGRATION AND DATA COLLECTION

### 2.1 Introduction

In this chapter, the components that were used to develop the device are discussed in detail with their usage and specifications. Then the data collection process and routes are explained. Finally, the different data sets obtained through this process are briefed.

### 2.2 System Components

In this section, the component specifications and the device architecture are explained.

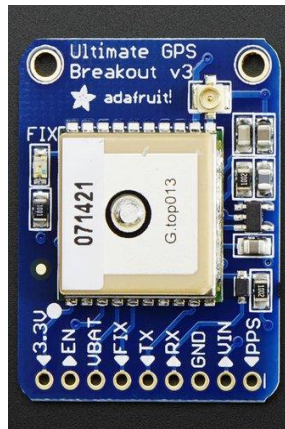
#### 2.2.1 Light Detection and Ranging (LIDAR)



**Figure 2.1:** LIDAR-Lite v3

LIDAR-Lite v3 is an optical distance measurement sensor. Compact, lightweight with low power consumption. User-configurable allows adjustment between accuracy, operating range, and measurement time. Communication via I2C and PWM. It requires a power source and an external micro-controller running an application . It has an output frequency of 500Hz and a range of 40m.

## 2.2.2 Global Positioning System (GPS)



**Figure 2.2:** Adafruit Ultimate GPS

The breakout board is built around the MTK3339 chipset, with a high-quality GPS module that can track up to 22 satellites on 66 channels, has an excellent high-sensitivity receiver (-165 dB tracking), and a built-in antenna. It can do up to 10 location updates a second (10Hz) for high speed, high sensitivity logging, or tracking. Power usage is incredibly low, only 20 mA during navigation. The Breadboard Breakout board comes with an ultra-low dropout 3.3V regulator. A footprint for optional CR1220 coin cell to keep the RTC running and allow warm starts and a tiny bright red LED. The LED blinks at about 1Hz while it's searching for satellites and blinks once every 15 seconds when a fix is found to conserve power .

## 2.2.3 Real Time Clock (RTC)

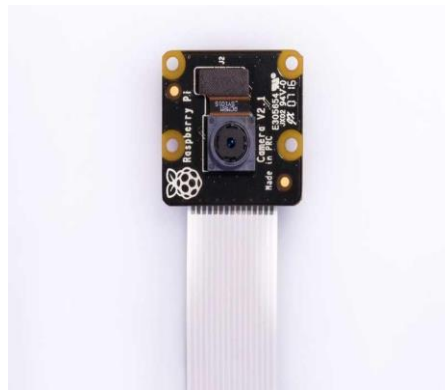


**Figure 2.3:** DS3231 Real-Time Clock

The DS3231 is a low-cost, extremely accurate I2C real-time clock (RTC) with an integrated temperature-compensated crystal oscillator (TCXO) and crystal. The device incorporates a battery

input and maintains accurate timekeeping when the main power to the device is interrupted, in this case, it maintains the time when the Raspberry pi is switched off. The integration of the crystal resonator enhances the long-term accuracy of the device as well as reduces the piece-part count in a manufacturing line. The RTC maintains seconds, minutes, hours, day, date, month, and year information. The date at the end of the month is automatically adjusted for months with fewer than 31 days, including corrections for leap year. The clock operates in either the 24-hour or 12-hour format with an AM/PM indicator .

#### 2.2.4 Camera



**Figure 2.4:** Raspberry Pi Camera

The infrared Camera Module v2 (Pi NoIR) replaced the original PiNoIR Camera Module in April 2016. The v2 Pi NoIR has a Sony IMX219 8-megapixel sensor (compared to the 5-megapixel OmniVision OV5647 sensor of the original camera). The Pi NoIR gives everything the regular Camera Module offers, with one difference: it does not employ an infrared filter. (NoIR = No Infrared.) This means that pictures taken in daylight will look decidedly curious, but it gives the ability to see in the dark with infrared lighting .

## 2.2.5 Laser Pointer



**Figure 2.5:** Laser Pointer

A laser pointer was used during the research while installing the external LIDAR sensor on the hood of the vehicle.

## 2.2.6 Arduino

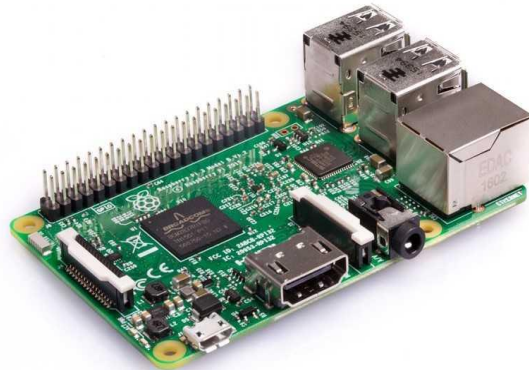


**Figure 2.6:** Arduino Uno Microcontroller

The UNO is the most used and documented board of the whole Arduino family. Arduino Uno is a microcontroller board based on the ATmega328P (datasheet). It has 14 digital input/output pins (of which 6 can be used as PWM outputs), 6 analog inputs, a 16 MHz quartz crystal, a USB connection, a power jack, an ICSP header, and a reset button. It contains everything needed to

support the microcontroller; simply connect it to a computer with a USB cable or power it with an AC-to-DC adapter or battery to get started. The Uno board is the first in a series of USB Arduino boards and the reference model for the Arduino platform .

### 2.2.7 Raspberry Pi



**Figure 2.7:** Raspberry Pi 3 Model B

The Raspberry Pi 3 Model B is the earliest model of the third-generation Raspberry Pi. It replaced the Raspberry Pi 2 Model B in February 2016. Quad-Core 1.2GHz Broadcom BCM2837 64bit CPU, 1GB RAM, BCM43438 wireless LAN and Bluetooth Low Energy (BLE) on board, 100 Base Ethernet, 40-pin extended GPIO, 4 USB 2 ports, 4 Pole stereo output and composite video port, Full size HDMI, CSI camera port for connecting a Raspberry Pi camera, DSI display port for connecting a Raspberry Pi touchscreen display, Micro SD port for loading the operating system and storing data and an Upgraded switched Micro USB power source up to 2.5A .

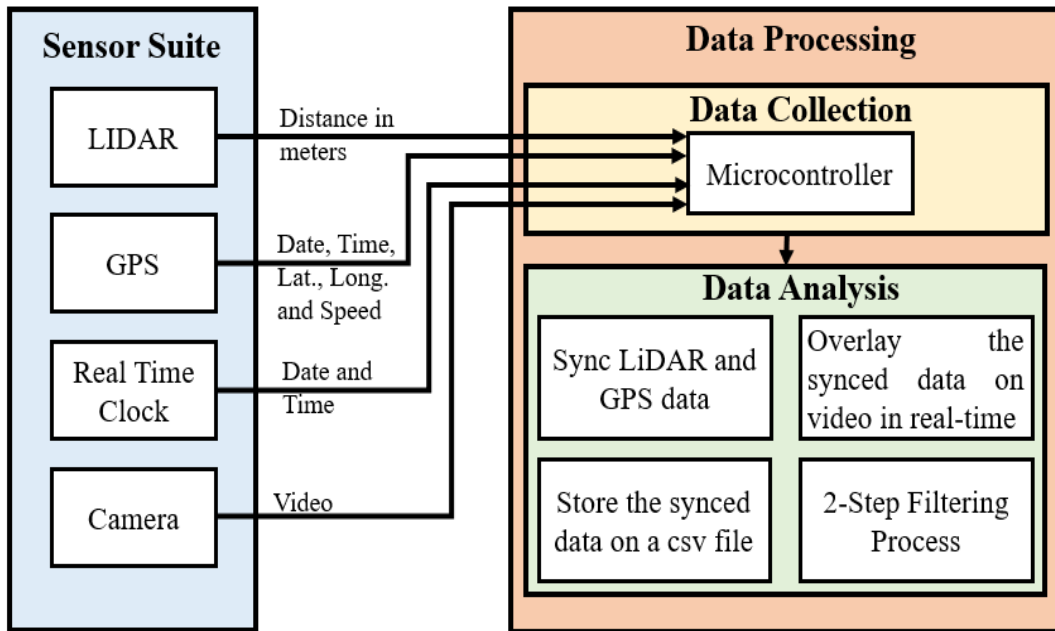
## 2.2.8 Mount



**Figure 2.8:** Delkin Fat Gecko Suction Mount

A Delkin Fat Gecko mount with dual suction cups was used to temporarily fix the LIDAR on to the hood of the vehicle during data collection.

## 2.2.9 System Architecture



**Figure 2.9:** System Architecture

In the system architecture, as shown in Figure 2.9, the sensor suite consists of the LIDAR, GPS, real-time clock and a camera. The LIDAR is used for distance measurement; GPS is used to collect



timestamps, speed, and positional data. The real-time clock is for updating the system time in the Raspberry pi and the video data from the camera is used as a reference to verify the data. The data output from the different devices is sent to the Data Processing unit which is a combination of an Arduino and Raspberry Pi. The Arduino receives the data captured from the GPS and LIDAR modules, organizes and syncs them together. The LIDAR has a range of 40 m and the output from the LIDAR module is in the form of pulses, whose width is converted to distance. The pulse width is expressed in the unit  $\mu\text{s}$ ,  $10 \mu\text{s} = 1 \text{ cm}$ . The distance of the object in meters is,

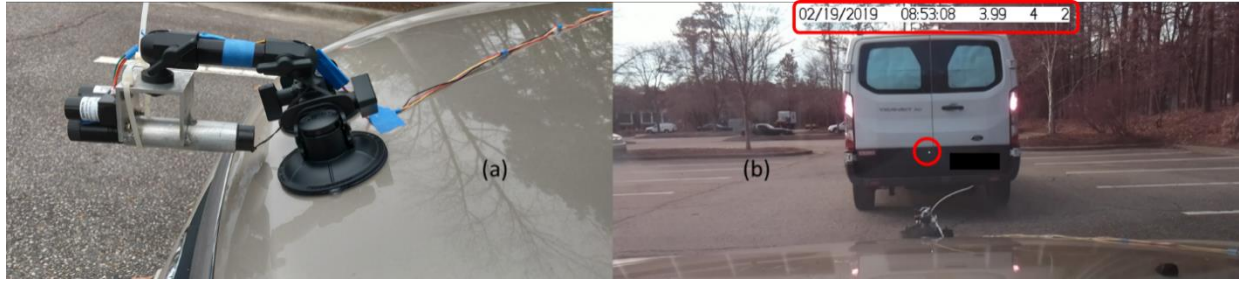
$$\text{Distance, } d = \frac{\text{Pulse width}}{1000} \text{ meters} \quad (1)$$

The Raspberry Pi performs the overlay of the GPS and LIDAR data on the video and stores the captured data in the CSV file. The 2-step filtering process can also be performed on the Raspberry Pi, but for convenience, visualization and efficiency of processing a large amount of data a separate laptop was used. The total cost of the entire setup would round up to \$300.

### **2.3 Data Collection**

During data collection, the LIDAR is mounted on the hood of the car using a specially made mount, which helps in the installation process. The mount consists of 2 suction pads, a shaft, and an aluminum panel with a laser pen holder.

As shown in Figure 2.10a, the two suction pads enable the mount to be affixed to the hood, the LIDAR is screwed to the aluminum panel and the laser pen is slid inside the holder. There are two knobs to adjust the angle of the mount. The light waves from the LIDAR cannot be seen by the naked eye, so the Laser pen helps to make the final adjustments. As shown in Figure 2.10b, the image is a snapshot from a real-time video, which gives an idea about where the LIDAR is pointed (red circle).

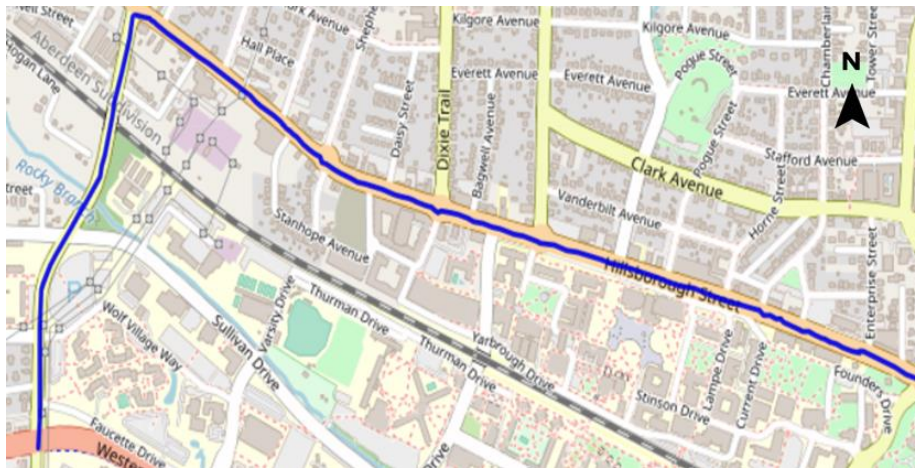


**Figure 2.10:** (a). LIDAR affixed on the hood of the car (b). Snapshot from the video.

As seen in Figure 2.10a, the LIDAR is connected to the in-vehicle unit through wiring, which consists of components like Arduino, Raspberry Pi, Real-time clock, GPS and Camera. The in-vehicle unit is powered through the 12V cigarette lighter port. Data is collected by following random vehicles in different traffic conditions like congested and free flow driving situations on freeways and arterial roads.

### 2.3.1 Route Details

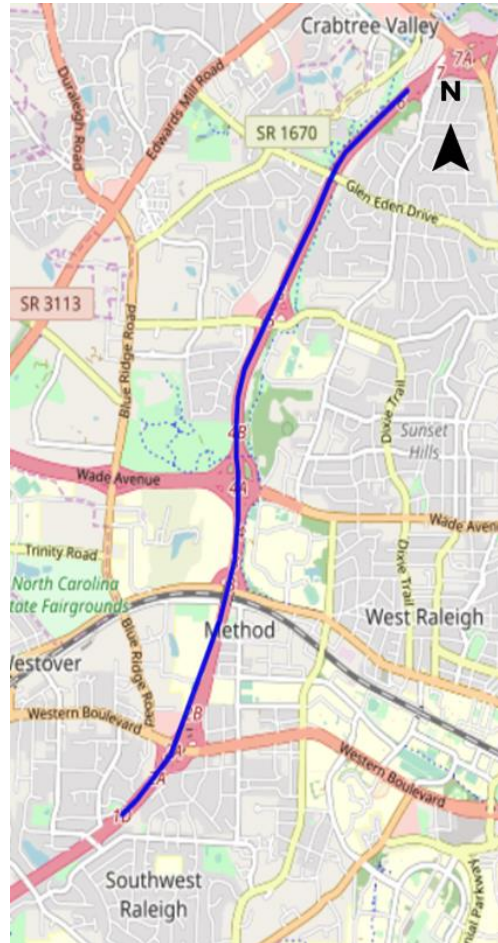
The data was collected by naturalistic driving in two routes. The chosen routes consist of one arterial segment and one freeway segment.



**Figure 2.11:** Arterial Route

The arterial route, as shown in Figure 2.11 was a 2-mile segment Northbound on Gorman Street followed by eastbound on Hillsborough Street in Raleigh, NC. Gorman Street had a varying speed limit of 35 – 40 miles/hour (MPH) and Hillsborough street has a speed limit of 25 - 30 MPH.

There are totally 8 signalized intersections with 2 on Gorman and 6 on Hillsborough street. Hillsborough Street has 4 roundabouts across the segment.



**Figure 2.12:** Freeway Route

The freeway route, as shown in Figure 2.12 was Southbound on Interstate-440 from Exit 7 to exit 1D. The speed limit across the 5-mile stretch varies between 55 – 65 MPH. In both routes two sets of data were collected, one in the AM off-peak (10 – 11 AM) and one in the PM peak (4 to 5 PM), resulting in four scenarios in total. The collected data consisted of timestamps, speed (mile per hour), the gap between vehicles (in meters) and subject vehicle positional data such as latitude and longitude. The time, speed and gap between vehicles were overlaid on the video, which was used as a reference to understand and confirm the results.

### 2.3.2 Data

Through the developed low-cost system two forms of data were captured and stored, which are explained in the following sections.

#### 2.3.2.1 Video Data with Overlay

The other data form stored in the Raspberry Pi is the video overlaid with the date (GPS), time (GPS), the spatial gap between vehicles (LIDAR), follower speed (GPS), and trip id. These variables are displayed on the video for reference which is highlighted in Figure 2.10b.

#### 2.3.2.2 GPS – LIDAR Data

The GPS and LIDAR data captured from the respective modules are synced within the Arduino and then sent to the Raspberry Pi where data is stored in a CSV file. A sample of the data is shown below.

**Table 2.1:** Sample Dataset

Date	Time	Latitude	Longitude	Speed (MPH)	Distance (meter)	Trip Id
2/19/2019	08:53:08 AM	35.770103	-78.682135	4	3.91	2
2/19/2019	08:53:08 AM	35.770103	-78.682135	4	3.95	2
2/19/2019	08:53:08 AM	35.770103	-78.682135	4	3.99	2
2/19/2019	08:53:08 AM	35.770103	-78.682135	4	0.14	2
2/19/2019	08:53:09 AM	35.770103	-78.682135	4	3.92	2
2/19/2019	08:53:09 AM	35.770103	-78.682135	4	3.98	2

The first and second column of Table 2.1 consists of the date and time, the third and fourth column consists of the vehicle's latitude and longitude, 5<sup>th</sup> column is the speed of the vehicle in miles per hour and all the above-mentioned data are obtained from the GPS module. The 6<sup>th</sup> column is the distance data from the LIDAR module in meters. The final column is the trip-id used as an identification number to identify each trip individually.

## 3 DATA FILTERING AND ERROR ANALYSIS

### 3.1 Introduction

This chapter discusses the types of noises in the data and methods to remove the noises. Also, error analysis is performed to highlight the performance of the prediction modeling used for filtering and the accuracy of the LIDAR sensor. Finally, stagewise results of the filtering process are explained.

### 3.2 Simple Exponential Smoothing (SES)

The exponential smoothing window is used to smoothen the time series data. The past values are given equal weight in a moving average window, but in simple exponential smoothing, weights are exponentially increased over time [19]. The exponentially increasing weights help in providing less weight to the values away from the data point of interest [20]. Exponential smoothing is given by equation [19]:

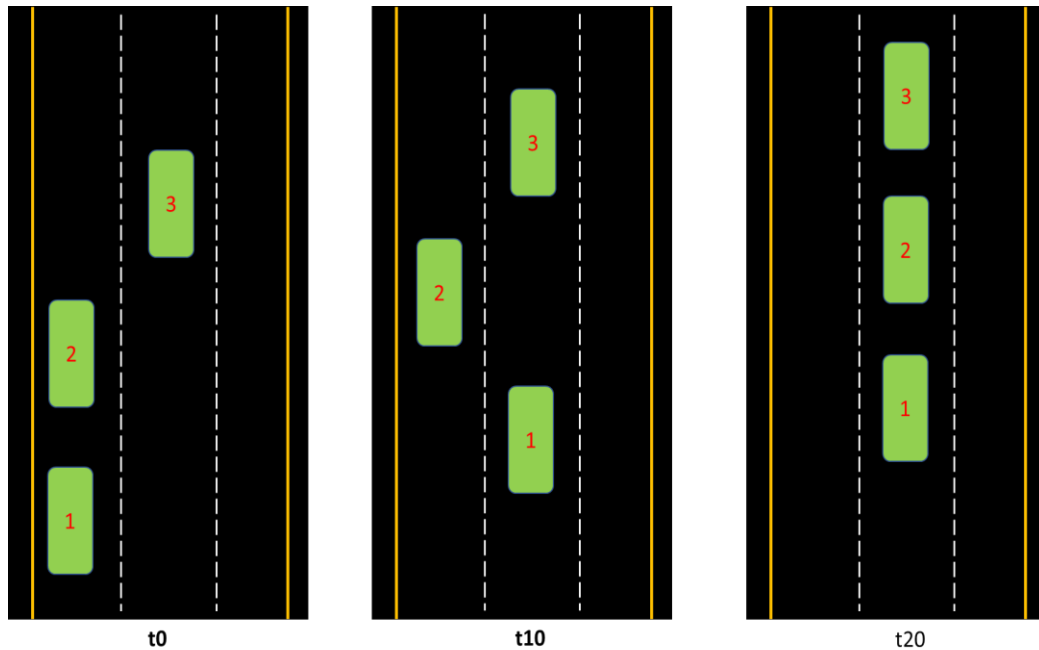
$$S_t = \alpha \cdot x_t + (1 - \alpha) \cdot s_{t-1} = s_{t-1} + \alpha \cdot (x_t - s_{t-1}) \quad (2)$$

where  $\alpha$  is the smoothing factor with values from  $0 < \alpha < 1$ .  $S_t$  is the weighted average of the most recent observation  $x_t$  and  $s_{t-1}$  is the previously smoothed data. Large values of  $\alpha$  provide greater weight to recent changes in the data, while small values of  $\alpha$  are less responsive to recent changes. Hence the value of  $\alpha$  depends on the data and the application. In this research, the simple exponential smoothing model is responsive to recent changes because each measured reading is independent of the previous readings i.e. the past values do not have an impact on present reading.

### 3.3 Auto Regressive Integrated Moving Average (ARIMA)

ARIMA (0,1,1) prediction modeling performs simple exponential smoothing [21]. The model performs incremental exponential smoothing by gradually discounting the past values i.e. lesser weights are given to values away from the current observation [22], by which less smoothing and more response to recent changes are achieved [19]. This prediction helps in filtering out the noise in the raw data. When the difference between the predicted value and the measured value is less than 2m (threshold 1: TH1) then the reading is a valid data point; otherwise, the measured value

is considered as a noisy reading and sent to the next stage for filtering. Noises are of three types, namely, system noise that is caused by weak signals received after reflection from the vehicle, noise due to objects in the environment like trees, bushes, lamp posts, and noise due to change in car-following events, etc.

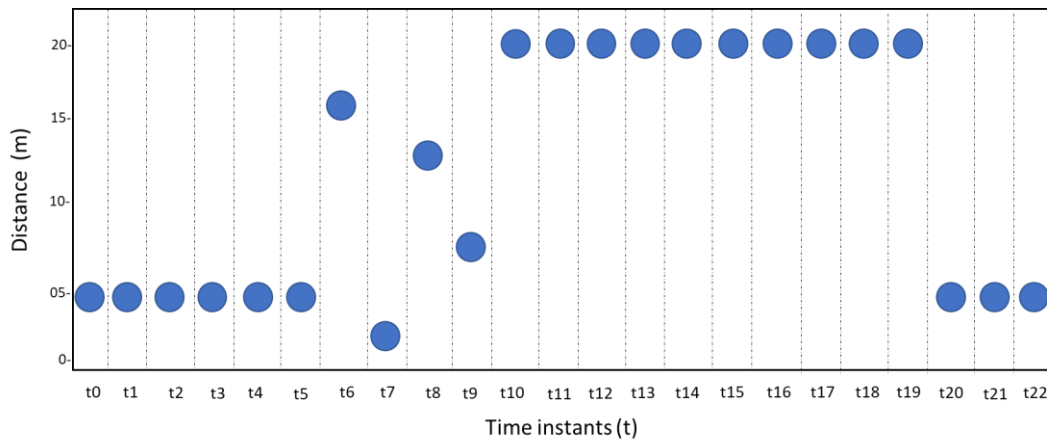


**Figure 3.1:** Illustrates the change in car-following events.

But some valid readings resemble noise. For example, as illustrated in Figure 3.1, assuming at instant ' $t_0$ ' the distance between any two vehicles is 5 m and the length of each vehicle is 10 m. So, at instant  $t_0$ , vehicle 1 (equipped) is following vehicle 2 at 5 m and after 10 instants of time vehicle 1 changes lane to follow vehicle 3 at 20 m approximately. So, this sudden change in value from 5 m to 20 m is called a change in the car-following event (good noise). Similarly, at instant  $t_{20}$  vehicle 2 moves between vehicle 1 and vehicle 3, hence now the distance measured changes from 20 m to 5 m. Hence these changes in car-following events are like the noise values with sudden upward or downward spike in readings. To avoid throwing out such values mean filtering is performed.

### 3.4 Mean Filter

As mentioned earlier, a sudden change in the spatial gap between vehicles can be due to weak signals or random objects or due to change in the car-following events. These types of readings are filtered out by ARIMA prediction modeling. Hence through mean filtering, the three types of readings are differentiated, and the change in car-following event readings (good noise) are retained, and the noise from random objects and system noise (bad noise) are discarded. The method of differentiating the readings is explained below;



**Figure 3.2:** Illustrates the raw data from the LIDAR for the scenarios shown in Figure 3.1.

With reference to Figure 3.1, Figure 3.2 illustrates the raw readings from the LIDAR module. The readings at t6, t8, and t9 are due to random objects, and reading at t7 is due to a weak reflected signal from the objects. The remaining data points are the reading of the vehicles. Readings captured from instant t0 to t5 are retained as valid data points by ARIMA prediction modeling. At t6 there is a sudden spike in data which is rejected by the ARIMA model, once rejected by the ARIMA model, mean filtering is performed, by averaging the values from t6 to t10. So, if the actual value at t6 is 17m but the average of the values from t6 to t10 is around 11.8 m, the difference between the actual value at t6 and averaged value is 5.2 m, so only when the difference between the actual value and the averaged value is less than 1m (threshold 2 as TH2) the value is retained. So, in this case, the value at t6 is discarded as a noisy value. Similarly, corresponding values from t7 to t9 are also discarded.

The next change in the event occurs from t9 to t10 as mentioned before ARIMA rejects the value of 20 m at t10 due to the sudden change in value. As performed earlier, the average from

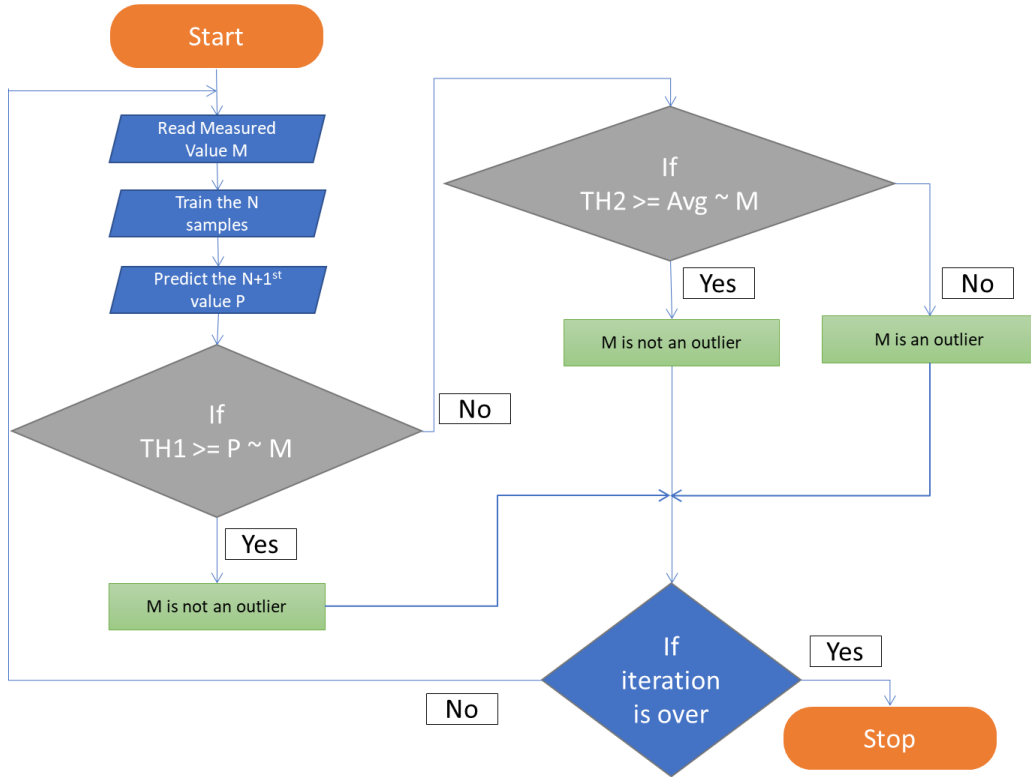
t10 to t14 is 20 m, and the difference between t10 and the average is less than 1m, so the sudden change in value is accepted as a valid data point. Similar processing happens in the transition from t19 to t20.

Hence through a combination of ARIMA prediction and mean filtering valid data points are retained, and invalid data points are discarded. The algorithm for this process is explained in detail below.

### **3.5 Data Filtering Algorithm**

There are two levels of filtering. In the first level, a window size (N) of 30 values is considered and the 31st value (N+1th value which is, P) is predicted through ARIMA forecasting if the difference between P and the measured value M is less than TH1 then the reading is a valid data point. But if the difference between P and M is greater than TH1 then the value is sent to the next level of filtering. In the second stage of filtering, the measured value M is assumed to be the starting of a new car-following event or noise. So, the average of M and the next 4 readings are considered and if the difference between the M and the average is less than TH2, then the measured value M is a valid data point or else M is a noisy reading. The discarded values are not considered for populating the sampling window which is used for predicting the value P. The sampling window of size N is a moving window. The two threshold values TH1 and TH2, are identified through trial and error to achieve the best-filtered data output.





**Figure 3.3:** Shows a Flowchart of the 2 step-filtering process

### 3.6 Error Analysis

The main reason for choosing ARIMA (0,1,1) was its exponential smoothing model. Table 3.1 shows the error analysis between the different ARIMA models [22] commonly used for time series forecasting. To perform the error analysis, ground truth data were collected by physical measurements in a controlled environment.

A test vehicle parked at 100 m from the starting point, the equipped vehicle was driven towards the stationary vehicle at a constant speed of 10 MPH, the LIDAR started recording from a stipulated distance of 26 m from the stationary vehicle, and the equipped vehicle was stopped at 10 m before the parked vehicle. Since the equipped vehicle was driven at a constant speed, and the initial LIDAR recording distance is known, the ground truth value is calculated for every instant a LIDAR reading was available in that range. In Table 3.1, Mean Square Error (MSE) is calculated to verify the accuracy of the prediction model and the accuracy of the final output. MSE is given by the formula,

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 \quad (3)$$

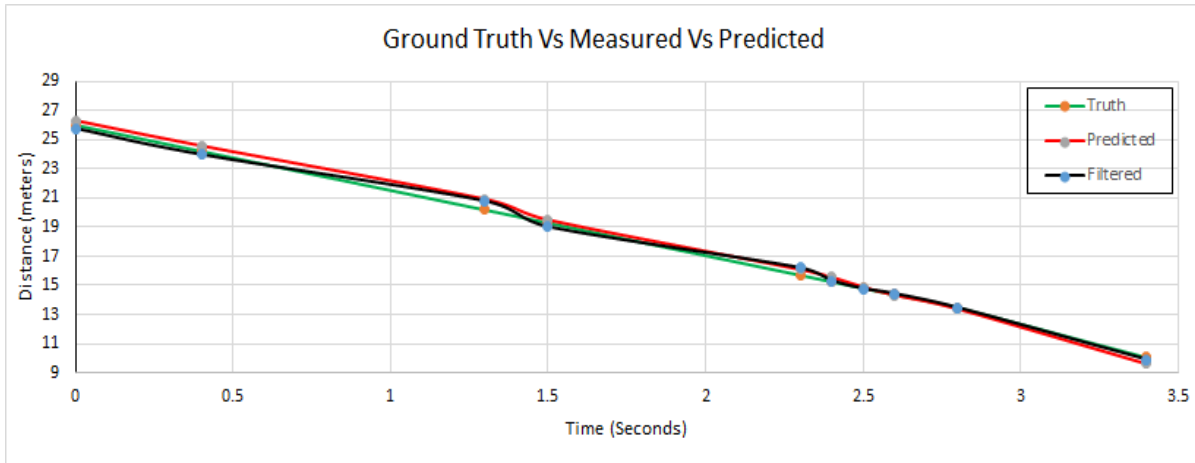
Where n is the number of data points,  $y_i$  is the observed value and  $\hat{y}_i$  is the predicted value.

The error analysis between ground truth and predicted value proves the accuracy of the ARIMA prediction with respect to the ground truth and the error analysis between the ground truth and the filtered data (final valid data points) proves the accuracy of the sensor with respect to the ground truth.

**Table 3.1:** Mean Square Error Analysis

<b>ARIMA Model</b>	<b>Ground Truth Vs Prediction</b>	<b>Ground Truth Vs Filtered Data</b>
White Noise- (0,0,0)	17.28 meters	1.38 meters
Random Walk- (0,1,0)	1.49 meters	0.98 meters
<b>SES- (0,1,1)</b>	<b>0.13 meters</b>	<b>0.08 meters</b>
1 <sup>st</sup> order AR model- (1,0,0)	1.01 meters	0.96 meters
Differenced 1 <sup>st</sup> order AR model- (1,1,0)	1.08 meters	0.96 meters
LES- (0,2,1)	2.61 meters	1.39 meters

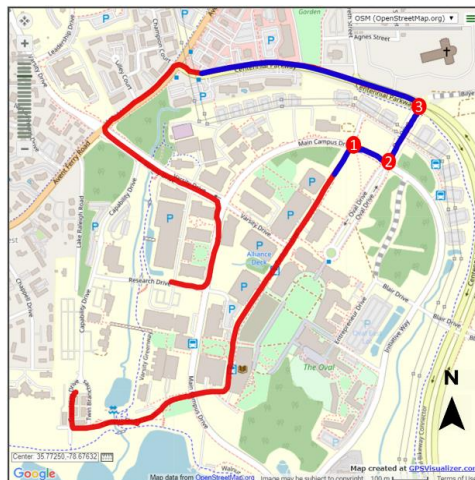
Table 3.1 highlights the MSE values of different ARIMA models. ARIMA (0,1,1) has the least MSE value when compared with the other ARIMA models. Figure 3.4 shows the comparison between ARIMA (0,1,1) predicted data, filtered data, and ground truth values.



**Figure 3.4:** Compares ground truth values with predicted and filtered data.

In Figure 3.4, the blue dots denote the values captured by the LIDAR in real-time, the grey dots are the values predicted by ARIMA (0,1,1), and the orange dots are the actual ground truth values measured physically using measurement tools. Figure 3.4 verifies that the grey dots and the orange dots lie very close to each other, which proves the accuracy of the ARIMA (0,1,1) prediction model and similarly the orange and blue dots also lie close to each other, which proves the accuracy of the LIDAR.

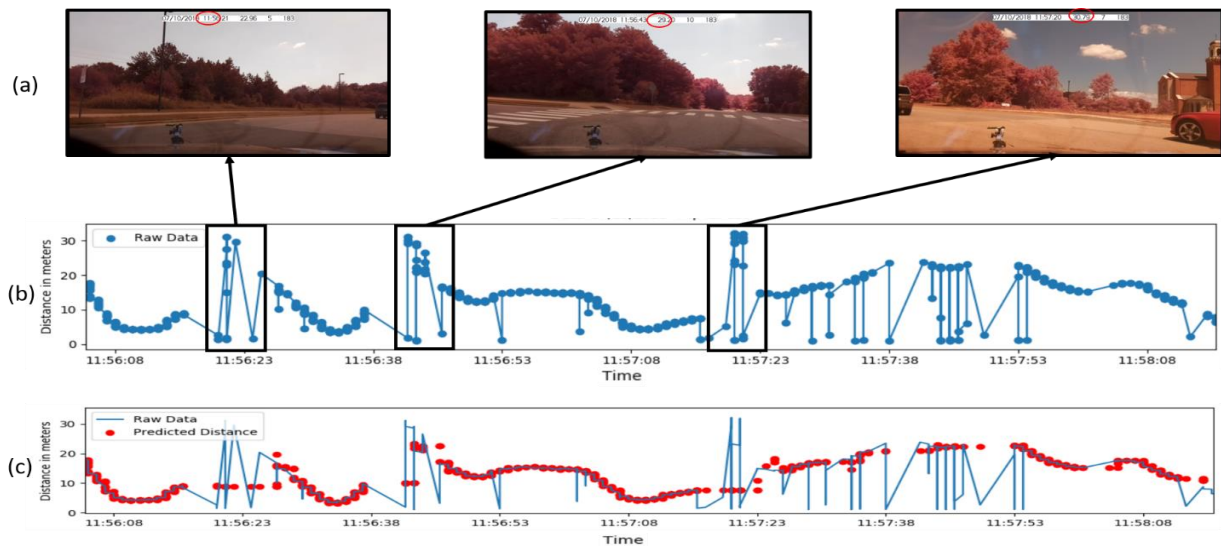
### 3.7 Data Filtering Results



**Figure 3.5:** Route traveled for collecting the data

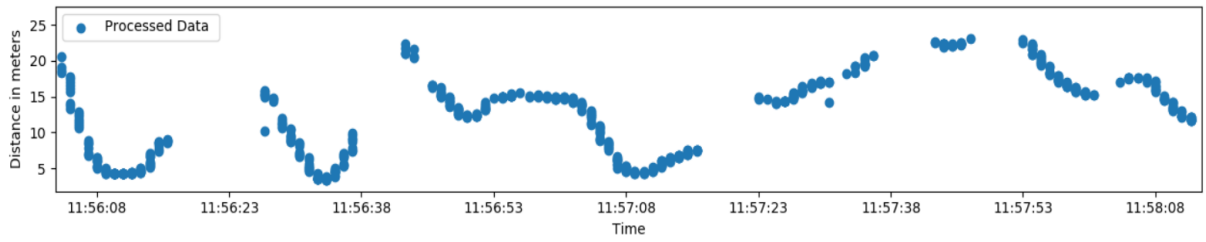
Figure 3.5 shows the trip map. The highlighted red route is the entire trip, the highlighted blue route is the section chosen for filtering. The three red dots are three instances of change in the car-following event. In the first instance the leading vehicle turns right eastbound on main campus drive, Raleigh, in the second event the leading vehicle turns left, northbound on Oval drive, Raleigh, and in the third event the leading vehicle was turning left, westbound on Centennial Parkway, Raleigh.

The equipped vehicle was following the same leading vehicle before and after the change in car-following events. The route map is generated using the GPS data retrieved from the developed equipment. Following are the stage-wise results of the filtering process, the data shown below belongs to the blue line on the map.



**Figure 3.6:** (a). Snapshots (b). highlights the noisy sections (c). ARIMA (0,1,1) prediction

In Figure 3.6b, the data points with noisy spikes are highlighted. The smooth curves denote the car following section and the oscillating spikes that are the noisy readings which are followed by the change in car-following readings. As shown by the images in Figure 3.6a, values are captured even if there are no vehicles present. These noises are due to objects in the environment such as lamp posts, bushes, objects on the shoulder, etc. The two-stage filtering process helps in detecting these changes in the car-following events. Figure 3.6c shows the prediction through ARIMA modeling and the measured data (raw data), using these two datasets the 2-stage filtering is performed and the following result is obtained.



**Figure 3.7:** The plot shows the fully processed output

In Figure 3.7, the blue dots are the filtered output data and the noisy data are clearly filtered out and only the spatial gap between vehicles is obtained as the final output.

## 4 TRAFFIC STREAM MODELS

### 4.1 Introduction

In this research data is investigated and analyzed through microscopic and macroscopic models. This chapter explains the theory behind the microscopic and macroscopic models.

### 4.2 Microscopic Traffic Models

Microscopic traffic measures are commonly used to estimate macroscopic models and car-following models are a microscopic [16]. In this research, the Wiedemann car-following model and its usage are discussed in detail.

#### 4.2.1 Wiedemann Car-Following Model

The two important information recorded in real-time are the gap between vehicles and speed of the following vehicle but, important information that is not measured in real-time would be the speed of the leading vehicle, which is estimated using the following formula;

$$\text{Speed of the leader, } v_l = v_f + \frac{\Delta d}{\Delta t}, \text{ mile/hour} \quad (4)$$

Where  $v_f$  is the instantaneous speed of the follower,  $\Delta d$  is the gap (rear bumper of the leading vehicle to the front bumper of the following vehicle) and  $\Delta t$  is the difference between time instances. The data collected can be visualized in various forms.

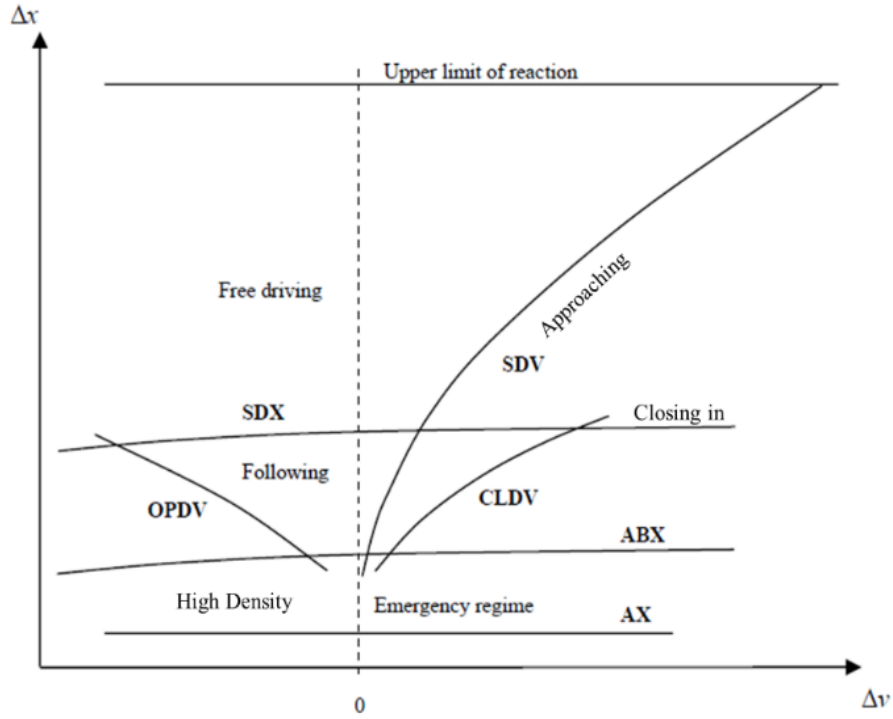
To implement the 1992 Wiedemann-Reiter car-following model, two important parameters are calculated [16]:

$$\text{Headway, } \Delta x = d + L, \text{ meters} \quad (5)$$

Where  $d$  is the gap (rear bumper of the leading vehicle to front bumper of the following vehicle) in meters and  $L$  is the length of the following vehicle in meters, and the difference in speed is;

$$\Delta v = v_f - v_l, \text{ mile/hour} \quad (6)$$

Where  $v_f$  is the instantaneous speed of the follower and  $v_l$  is the speed of the leader in mile/hour. The VISIM or Wiedemann car-following model is the largest parameterized model when compared to the AIMSUN, MITSIM, and Fritzsche model [16]. So, using the above two parameters  $\Delta v$ ,  $\Delta x$  along with certain calibration parameters, the thresholds for the VISIM car-following model are defined. There are in total 6 thresholds defined for this model.



**Figure 4.1:** Regime thresholds of the Wiedemann model [16].

AX would be the desired distance between two stationary vehicles;

$$AX = L_{n-1} + AX_{add} + RND1n * AX_{mult} \quad (7)$$

Where  $AX_{add}$  and  $AX_{mult}$  are calibration parameters whose values are 1.25 and 2.5, respectively [16].  $ABX$  is the desired distance between the leader and follower at low-speed differences;

$$ABX = AX + BX \quad (8)$$

$$BX = (BXadd + BXmult * RND1n) * \sqrt{v} \quad (9)$$

$$v = \{v_l : v_f > v_l, v_f : v_l \geq v_f\} \quad (10)$$

Where BXadd and BXmult are calibration parameters, whose values are 2 and 1, respectively [16]. The maximum distance maintained by the follower in a car-following scenario is defined as SDX;

$$SDX = AX + EX * BX \quad (11)$$

$$EX = EXadd + EXmult * (NRND - RND2_n) \quad (12)$$

Where EXadd and EXmult are calibration parameters, whose values are 1.5 and 0.55 [16]. SDV is the point where the driver realizes he/ she is approaching a slower vehicle;

$$SDV = \left( \frac{\Delta x - L_{n-1} - AX}{CX} \right)^2 \quad (13)$$

$$CX = CXconst * (CXadd + CXmult * (RND1n + RND2n)) \quad (14)$$

Where CXconst, CXadd and CXmult are calibration parameters; CX is rounded to 40 [16]. CLDV is the point where the driver realizes he/she is closing in on a slower vehicle and must decelerate to avoid a collision;

$$CLDV = SDV * EX^2 \quad (15)$$

Finally, the OPDV threshold where the driver realizes that his/her speed is not constrained by the leading vehicle,

$$OPDV = CLDV * (-OPDVadd - OPDVmult * NRND) \quad (16)$$



Where OPDVadd and OPDVmult are calibration parameters whose values are 1.5 and 1.5 respectively [16]. There are three normally distributed driver parameters namely NRND, RND1<sub>n</sub> and RND2<sub>n</sub>, whose values are N(0.5,0.15) [16]. For all calculations, the mean value of 0.5 has been used.

As shown in Figure 4.1, when  $\Delta x$  vs  $\Delta v$  is plotted against the Wiedemann thresholds, each data point can be classified into a specific regime. There are totally 6 regimes namely; emergency, high density, following, approaching, closing-in and free driving regime. Emergency and high-density regime are low speed - low distance regimes. Data falls within emergency and high-density regimes regime when the speed of the follower is greater than the leader and lower than the speed of the leader respectively. Free driving and closing-in are high speed - high distance regimes, data that falls within these regimes are due to speed of follower is lower than the leader and higher than the leader respectively. Approaching regime is a transition phase between free driving and closing-in regimes. Finally, following regime is centered between the other five regimes, data falls within this regime when the leader and follower have very small speed differences. Hence each data point will belong to one of the six car-following regimes.

### 4.3 Macroscopic Models

Macroscopic traffic models are explained through the relationship between Flow, Density and Speed. This research focusses on the relationship between speed and density.

#### 4.3.1 Local Density

The headway data ( $\Delta x$ ) gives information about the car-following distance maintained by the follower at every instant, from which the average spatial distance over the segment can be measured. Like the speed of the leader vehicle, the local density is also estimated using the captured information with the formula as;

$$\text{Local Density, } D_L = \frac{1609.34}{d+L} \text{ Vehicles/mile} \quad (17)$$

Where d is the gap (rear bumper of the leading vehicle to front bumper of the following vehicle) in meters and L is the length of the following vehicle in meters. Using  $D_L$ , the local density

distribution across the segment can be understood, unlike the stationary sensors which capture information only for a small portion of a segment.

The LIDAR device has a measurement limitation of 40m and considering the length of the following vehicle is 5m, local density less than 35 veh/mi cannot be measured. Based on the local density variation the driver's behavior pertaining to the environment and the traffic conditions can be studied.

### 4.3.2 Speed vs Density

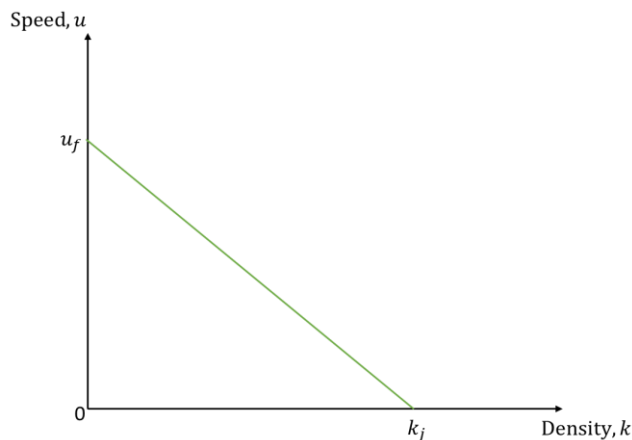
With the Local density estimated, instantaneous speed – local density plots can be plotted to study their relation. At the y-intercept, density is zero and the speed is termed as Free-flow speed and at the x-intercept speed is zero and density is termed as jam density. Some standard speed-density models are explained in the following section.

### 4.3.3 Standard macroscopic models

Macroscopic traffic stream models like Greenshields and Modified Greenberg are used to investigate the quality of the dynamic data from the arterial and freeway segment based on their best-fit parameters. In Greenshields model, as shown in Figure 4.2 the speed-density relationship is expressed as [23];

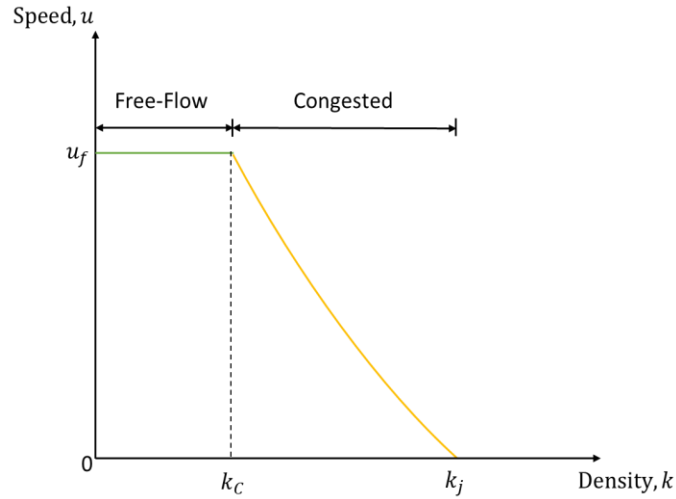
$$u = u_f \left(1 - \frac{k}{k_j}\right) \quad (18)$$

Where  $u$ ,  $u_f$ ,  $k$ , and  $k_j$  are the speed, free-flow speed, density, and jam density.



**Figure 4.2:** Greenshields Model

Unlike Greenshields, which is a single regime model, Modified Greenberg is a multi-regime model with 2 regimes where the data is categorized into the free-flow and congested regime, as shown in Figure 4.3. For density values below  $k_c$  the speed is free-flow speed  $u_f$ , and the speed-density relation for density above  $k_c$  is expressed as [23];



**Figure 4.3:** Modified Greenberg Model

$$u = u_m * \ln\left(\frac{k_j}{k}\right) \quad (19)$$

Where  $u$ ,  $u_m$ ,  $k$ , and  $k_j$  are the speed, optimum speed, density, and jam density.

## 5 DATA ANALYSIS AND RESULTS

### 5.1 Introduction

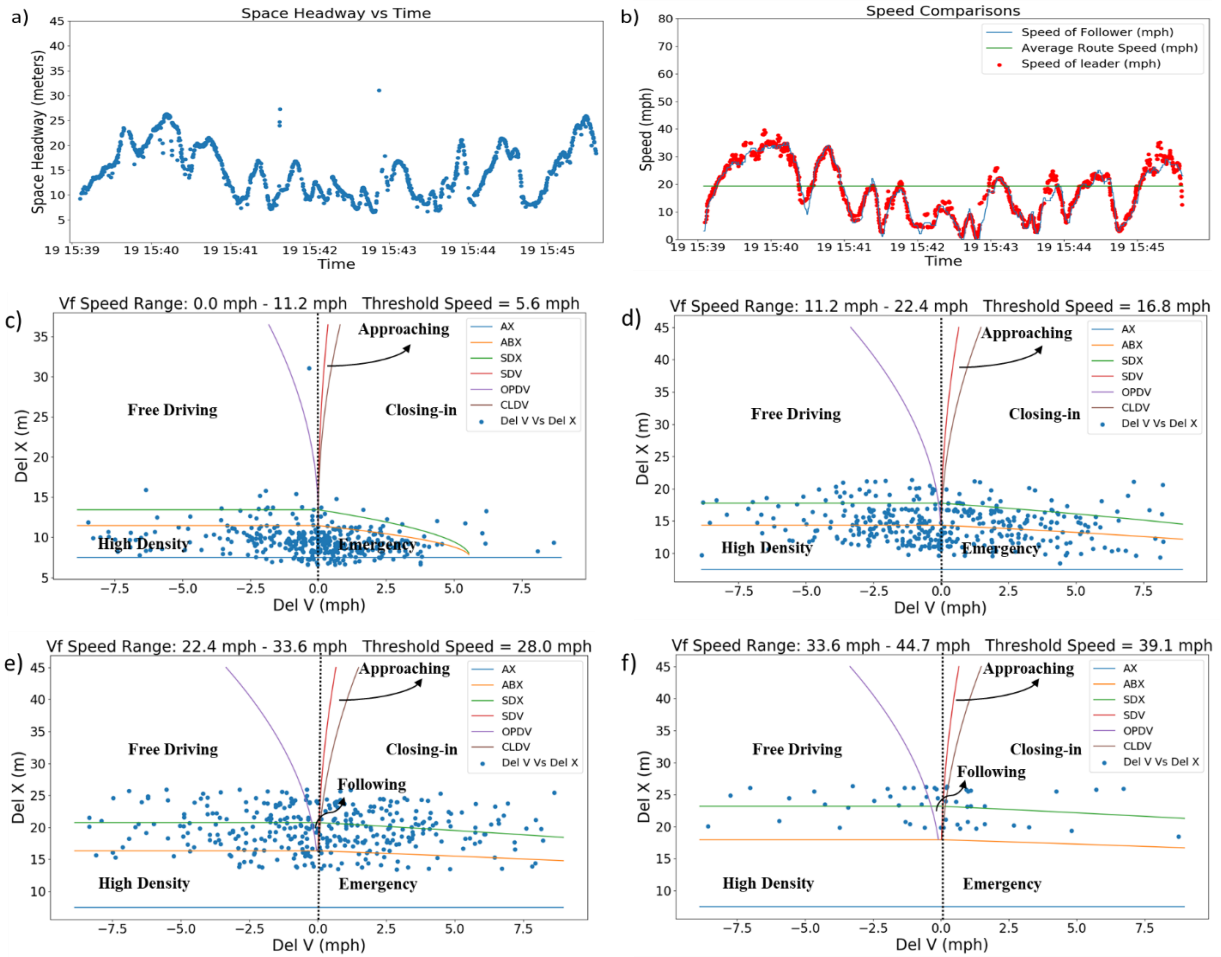
In this chapter, three methods of data investigations are discussed. Each method has a different perspective on driver behavior.

### 5.2 Trip Characteristics

As mentioned earlier various information such as headway, speed of follower, speed of the leader is obtained and Wiedemann car-following models are visualized to understand the actual traffic condition at the time of capturing. Since the speed of the follower is known at any point on the route, it can be compared to aggregated probe data collected by third-party companies such as HERE and INRIX. In this research, the instantaneous speed of the follower along the segment from the GPS device is compared with the data obtained from the Regional Integrated Transportation Information System (RITIS) [24], which are also compared to the estimated speed of the leading vehicle. The speed of the leader data is available only when there is valid spatial gap data of the leading vehicle i.e. when the vehicle is in range and its data are not filtered out due to noise.

#### 5.2.1 Arterial Trip Data

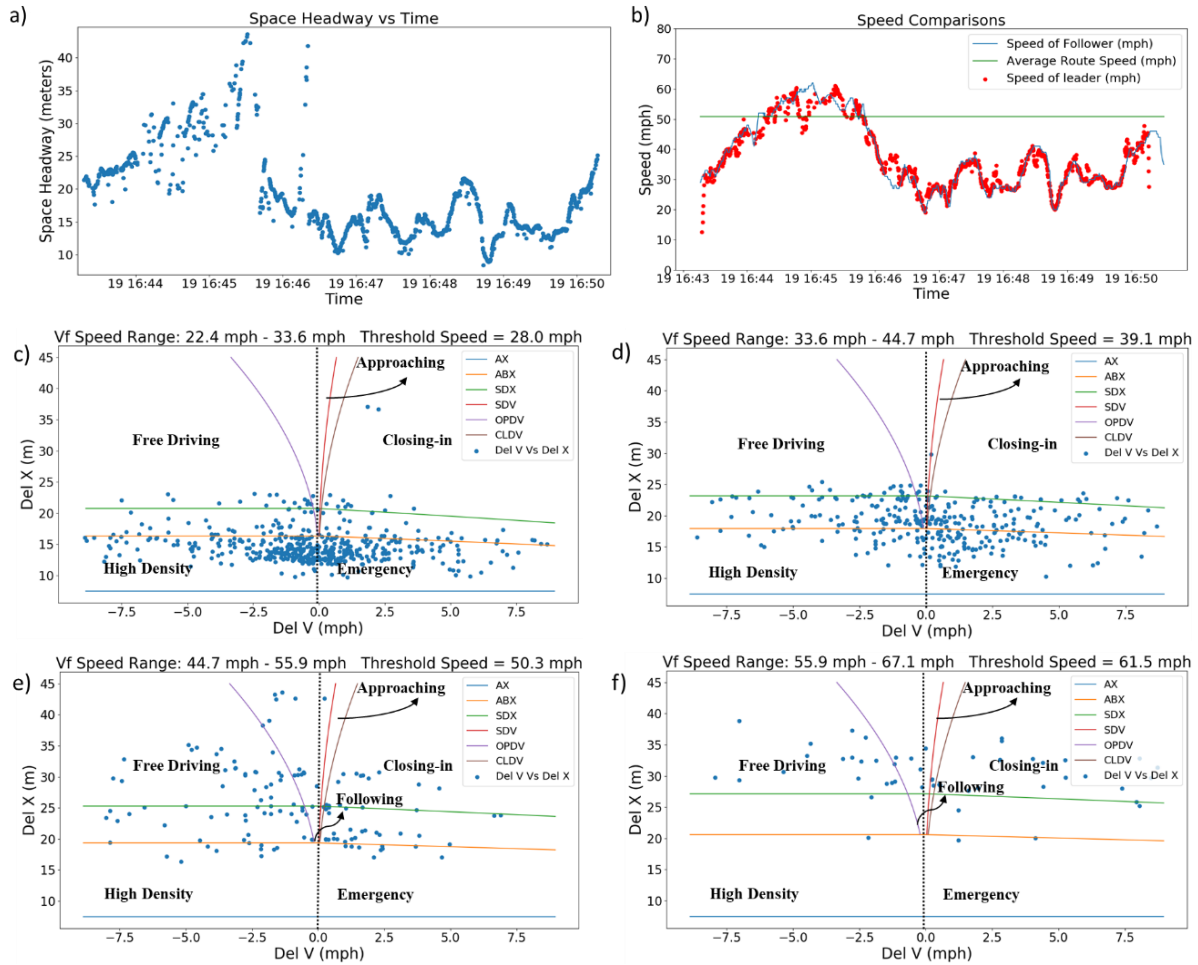
Figure 5.1 visualizes the various data gathered on the arterial segment during the PM peak period. Figure 5.1a) shows the headway data ( $\Delta x$ ) over time, b) shows the speed of follower ( $v_f$ ), speed of the leading vehicle ( $v_l$ ) along with the average speed across the segment at that time (from RITIS), c-f) shows the Wiedemann car-following graphs for various speed ranges. The “Del X” ( $\Delta x$ ) and “Del V” ( $\Delta v$ ) plotted on x and y-axis are obtained from equations 5 and 6 respectively. Ranges are specified at the top of the graph and the threshold speed ( $v_f$ ) value used to generate the thresholds is also mentioned. The threshold value is chosen as the midpoint of the range. Some speed ranges are not shown because they have a negligible amount of data points.



**Figure 5.1:** Sample data collected during PM peak on the arterial segment.

The definition of the thresholds labeled in Figure 5.1 are [17]: AX - the desired distance for stationary vehicles, ABX - the threshold for desired following distance for low speeds, the Emergency regime is as low speeds when the speed difference is positive i.e. speed of follower is greater than the speed of leader and vice versa would be the High-density regime. SDX – the threshold where the driver realizes he/she is falling far too behind, SDV – the threshold where the driver realizes he/she is approaching a slower vehicle (Approaching regime), CLDV – the threshold where the driver realizes he/she has to decelerate to avoid an accident (Closing-In regime), OPDV – the threshold for small speed variations for increasing distances (Free Driving regime).

## 5.2.2 Freeway Trip Data



**Figure 5.2:** Sample data collected during PM peak on the Freeway segment.

Like the arterial data, Figure 5.2 displays the data collected during the PM peak in the freeway segment. As expected, the speed range is slightly higher than the arterial segment.

## 5.2.3 Trip Statistics

Table 5.1 provides summary statistics for all four scenarios. The reported sample rate is consistent across scenarios. The sample rate here is defined as the number of valid samples per second.

**Table 5.1: Trip Statistics**

Scenarios	Arterial		Freeway	
	AM Off-peak	PM Peak	AM Off-peak	PM Peak
Start Time	10:01	15:39	11:13	16:43
End Time	10:11	15:45	11:19	16:50
Total Distance Traveled (miles)	2	2	4	4
Total Travel Time (s)	569	392	324	434
# Raw Headway Points	1,763	1,331	459	1380
Time with Valid Data Points (s)	491	376	102	341
# Valid Headway Points	1,654	1,293	306	1,179
Sample rate (%)	3.37	3.44	3.00	3.46
Average Space Headway (feet)	46.32	49.15	96.78	60.37
Average Route Speed, RITIS (MPH)	16	19	64	50
Average Follower Speed (MPH)	10	16	54	36
Average Leader Speed (MPH)	13	19	47	36

The average headway in the arterial scenarios is around 46 to 49 ft. In the two arterial scenarios the follower speed less than the average speed in the segment (RITIS) and the leader speed. The speed data distribution is varying, in the AM off-peak, around 88.64% of the speed data lies between 0 to 22.4MPH whereas in the PM peak 65.46% of the speed data lies between 0 to 22.4MPH and 30.28% lies between 33.6MPH to 44.7MPH. The data classification across different regimes in the two arterial scenarios are similar when compared. The data points are well spread across emergency, high density, Closing-in, and the free driving regime in both the scenarios.

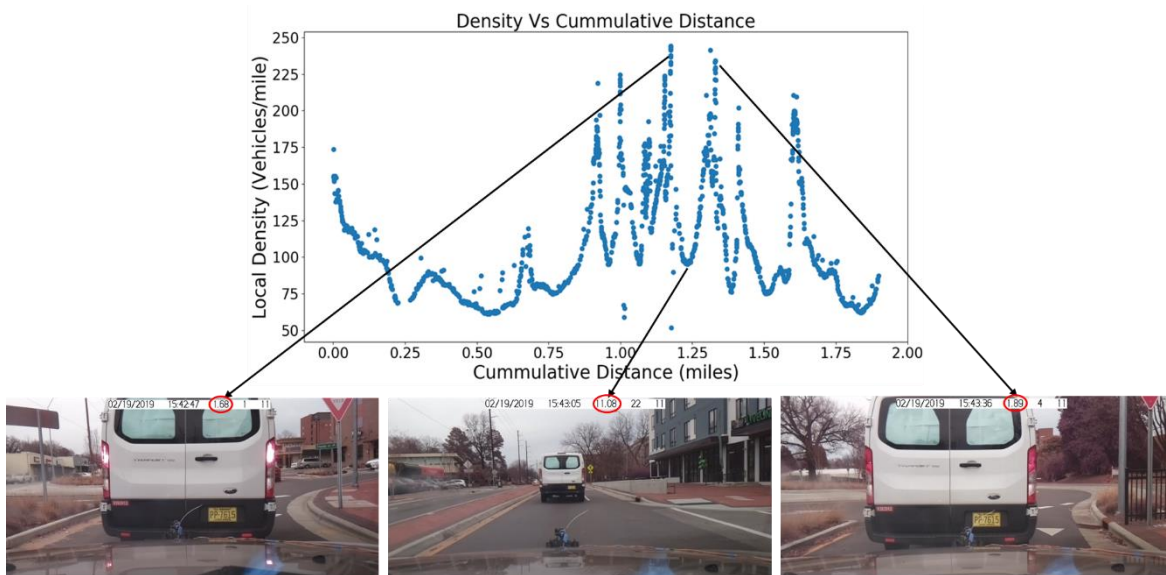
While considering the freeway scenarios, the total distance traveled in the freeway segment is 4 miles, and the number of samples collected in the AM off-peak scenario in the freeway is less mainly because of a lack of vehicles at that time of the day, but the sample rate is consistent. The average headway distance on the freeway in the AM off-peak is around 97 ft as expected due to

lack of traffic, but during the PM peak, it reduces to 60 ft. The average follower speed and the average leader speed are lesser than the average speed across the segment (RITIS).

### 5.3 Longitudinal Evolution of Density

The local density data are plotted across cumulative distance traveled and are compared with the photos captured in real-time, to gain a better understanding of the plots.

#### 5.3.1 Arterial Route

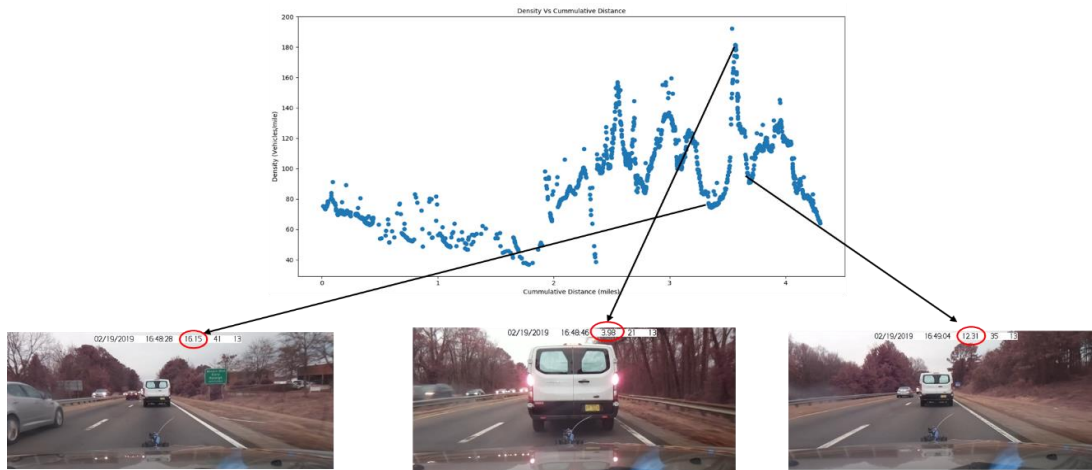


**Figure 5.3:** Local density profile across the arterial segment in the PM peak.

Figure 5.3 highlights the local density plot over cumulative distance for the arterial segment in the PM peak scenario, this plot helps in identifying the local density at precise locations across the corridor. Such plots of longitudinal evolution across a corridor provides a sense of traffic stream and road geometry enforced constraints on the driver. For example, the 3 spots on the plot are highlighted through actual images captured in real-time, the first image indicates the high density at the entrance of a roundabout, as vehicles are expected to yield, the queue builds up at the entrance of the roundabout, then in the second image the leading vehicle creates a large gap as a result of exiting the roundabout and correspondingly the density decreases and in the third image similar to the first one the leader yields at the entrance of another roundabout as the queue builds up the local density also increases.



### 5.3.2 Freeway Route



**Figure 5.4:** Local density profile across the freeway segment in the PM peak.

Like the arterial segment Figure 5.4 displays the local density distribution across the freeway corridor. So, as the headway decreases the local density increases and vice versa. When the local density is high for a segment then the congestion is high and vice versa. But when the local density is oscillating then it means that the traffic is moving.

### 5.3.3 Trip Statistics

Table 5.2 summarizes the average local density for every 0.25 mile of the AM off-peak and PM peak data from the arterial segment and every 0.5 miles of the AM off-peak and PM peak data from the freeway segment.

**Table 5.2:** Longitudinal Variation of Local Density across Sub-Segments

Average Local Density across Sub-Segments (vehicles/mile)					
Sub-Segment (miles)	Arterial		Sub-Segment (miles)	Freeway	
	AM Off-peak	PM Peak		AM Off-peak	PM Peak
0 - 0.25	74	111	0 - 0.5	78	71
0.25 - 0.5	49	77	0.5 - 1	57	60
0.5 - 0.75	141	78	1 - 1.5	41	53
0.75 - 1	158	129	1.5 - 2	43	92
1 - 1.25	148	148	2 - 2.5	40	115
1.25 - 1.5	123	138	2.5 - 3	54	102
1.5 - 1.75	162	127	3 - 3.5	42	123
1.75 - 2	85	71	3.5 - 4	47	89

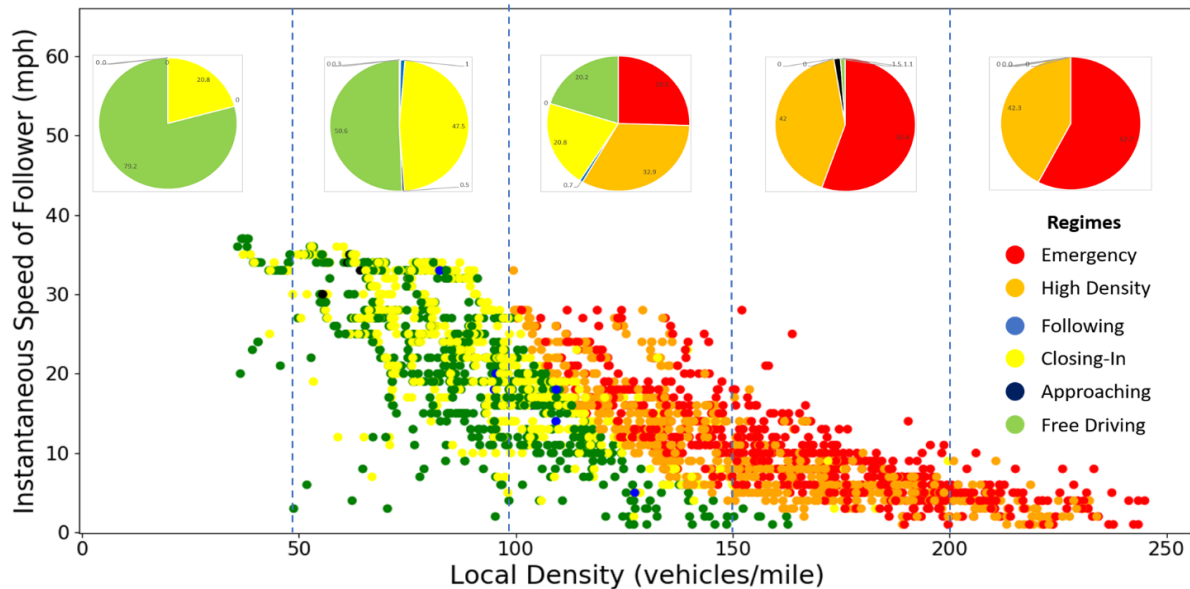
Table 5.2 gives the average local density distribution across sub-segments of the entire corridor. The Gorman street – Hillsborough intersection lies in the 0.5 – 0.75mile sub-segment. The 4 roundabouts and 6 signalized intersections lie within the 0.75 – 1.75mile sub-segment, hence there is a significant higher local density compared to other sub-segments during AM off-peak and PM peak. In the Freeway segment, due to lack of traffic during the AM off-peak, the local density is relatively low throughout the segment, but during the PM peak there is a significant increase in local density within the 1.5 – 3.5 mile mainly because there are few exits and merge sections within the sub-segment, which leads to a significant increase in local density. Hence considerable changes in local density between AM off-peak and PM peak, can be investigated by the traffic planners or regulatory officers, if found to be consistent and an exception.

## 5.4 Speed vs Density vs Wiedemann Model

In this section, the microscopic Wiedemann car-following model and macroscopic speed-density model are compared and plotted across each other to analyze the driver behavior.

### 5.4.1 Arterial Route

In Figure 5.5, the pie charts represent the regime distribution for every 50 vehicles/Mile (veh/mi) range. The speeds range between 0 – 40 MPH. In the arterial segment, only 4 regimes (the Free driving, closing-in, high density, and emergency regime) are predominant because the following regime and the approaching regime are more like a transition phase. Free driving and the closing-in are high-speed regimes at increasing and decreasing distances respectively. While the emergency regime and the high-density regimes are low-speed regimes at decreasing and increasing distances respectively. A driver is considered a safe/neutral if the free driving regime is maintained at high speeds and high-density regime at low speeds.



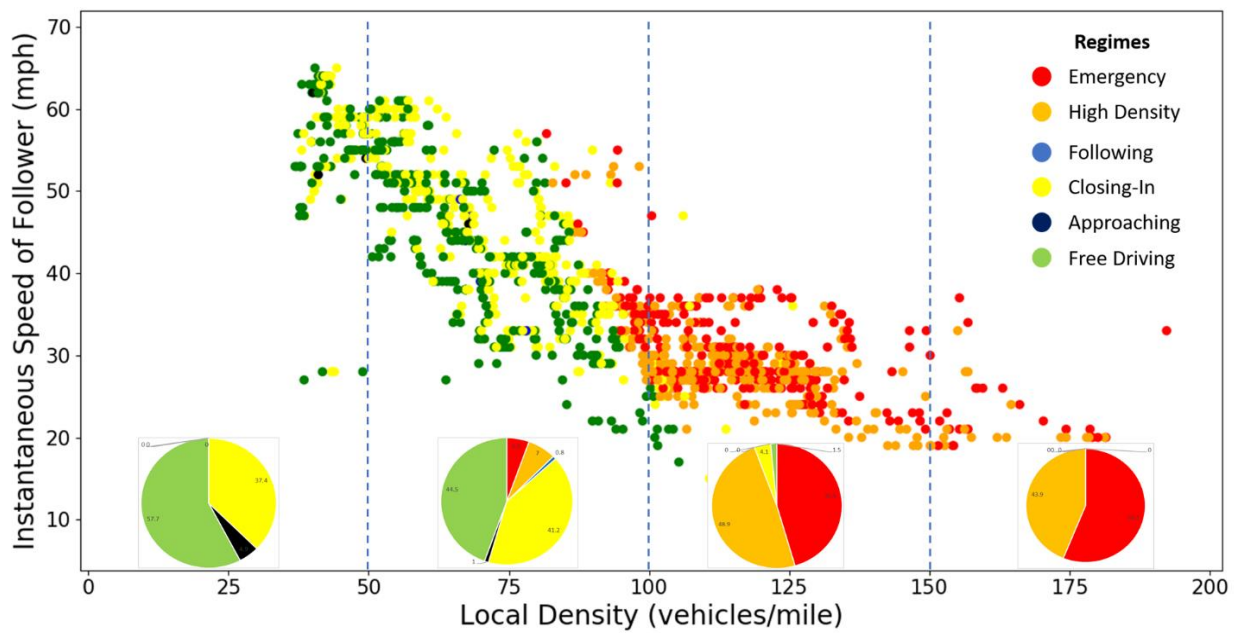
**Figure 5.5:** Instantaneous Speed-Local Density with Wiedemann Regimes for Arterial

Figure 5.5 displays a high percentage of the free-driving regime at a low local density of 0-50 veh/mi i.e. the driver maintains a safe distance at high speeds and low local densities. But there is a high percentage of the emergency regime at high local densities (greater than 150 veh/mi) i.e. the driver maintains very close distances at speeds higher than the leader, and chances of

collision are higher. Hence from these analyses, the driver behavior can be characterized as safe at low local densities and aggressive at high local densities in the arterial segment.

### 5.4.2 Freeway Route

Like Figure 5.5, in Figure 5.6, the pie charts represent the regime distribution for every 50 vehicles/mile (veh/mi) range. The overall speed ranges between 15 – 65 MPH. Like the arterial segment, only 4 regimes (the Free driving, closing-in, high density, and emergency regime) are predominant in the freeway as well.



**Figure 5.6:** Instantaneous Speed-Local Density with Wiedemann Regimes for Freeway

Figure 5.6 displays a high percentage of the free-driving regime at a low local density of 0-80 veh/mi i.e. the driver maintains a safe distance at high speeds and low local densities. But there is a high percentage of the emergency regime at local densities greater than 110 veh/mi i.e. the driver maintains very close distances at speeds higher than the leader, and chances of collision are higher. Hence from these analyses, the driver behavior can be characterized as safe at low local densities and aggressive at high local densities.

Hence through this method of analysis, each and every data point can be classified to a specific regime, and the percentage of data distributed across different regimes as shown in Table 5.1 can be used to model driver behavior, when data from multiple drivers are available.

### 5.4.3 Trip Statistics

From Table 5.3, in the AM off-peak scenario, 73.85% of the data lies in the closing-in and free driving regime and 71.21% of the speed data falls in the range 44.7 to 67.1 MPH in the freeway segment. In the PM peak scenario on the freeway, resembles the regime distribution across arterial roads but 78.06% of the speed data lies between 22.4 to 45.7 MPH much lower than the AM the off-peak scenario in the freeway segment, but for a similar regime distribution to the arterial segments the driver is at a higher speed range in the freeway.

**Table 5.3:** Trip Statistics

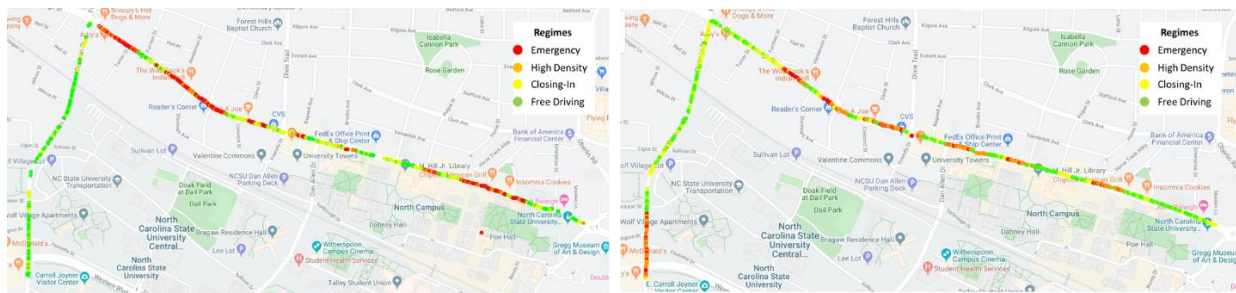
Scenarios	Arterial		Freeway	
	AM Off-peak	PM Peak	AM Off-peak	PM Peak
<b>% Follower Speed Distribution Range:</b>				
0 MPH to 11.2 MPH (%)	52.56	33.28	0	0
11.2 MPH to 22.4 MPH (%)	36.08	32.18	1.52	4.76
22.4 MPH to 33.6 MPH (%)	7.77	30.28	12.5	47.67
33. MPH to 44.7 MPH (%)	3.59	4.26	14.77	30.39
44.7 MPH to 55.9 MPH (%)	0	0	40.91	12.43
55.9 MPH to 67.1 MPH (%)	0	0	30.3	4.75
<b>% Time Spent in Wiedemann Regimes:</b>				
Emergency Regime (%)	24.26	23.52	11.44	24.96
High-Density Regime (%)	27.45	23.31	8.83	27.14
Approaching Regime (%)	0.1	0.2	2.61	0.4
Closing-In Regime (%)	18.27	25.83	36.27	22.48
Following Regime (%)	0.36	0.77	3.27	0.34
Free Driving Regime (%)	29.56	26.37	37.58	24.68

Based on the data distribution, at low speeds, the driver was more aggressive in the arterial segment, and at high speeds, the driver was more aggressive in the freeway segment.

### 5.4.4 Application and Correlation

This method of investigation can be used to analyze the regime distribution across the segment. As each data point is categorized to a specific regime and holds positional data (latitude and longitude), the information can be plotted on the map to better understand the driving behavior.

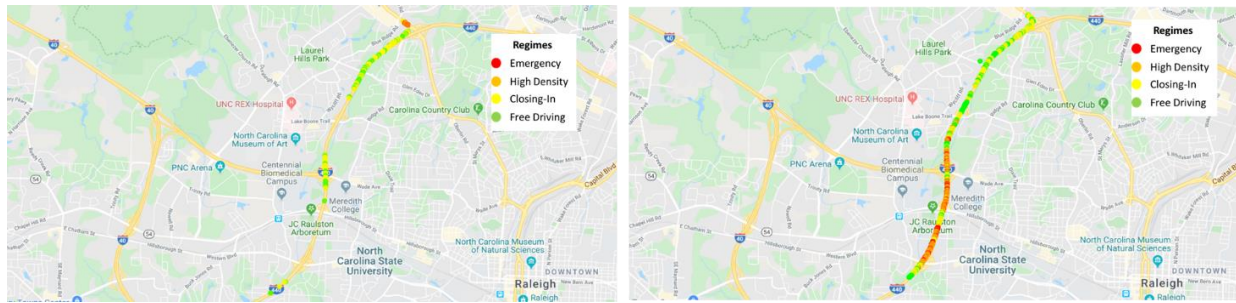
#### 5.4.4.1 Arterial Route



**Figure 5.7:** a) Regime distribution AM Off-Peak b) Regime distribution PM Peak – Arterial

From Figure 5.7a, during the AM off-peak hours, the northbound on Gorman street is not congested as there are only free-driving and closing-in regimes, but during the PM peak hours the Gorman street seems to be congested as there are emergency and high-density regimes are present at the beginning, as shown in Figure 5.7b. But at both periods, the Hillsborough street seems to be congested due to its 6 signalized intersections and 4 roundabouts, as shown in Table 5.2 between the 0.75 to 1.75-mile sub-segment.

### 5.4.4.2 Freeway Route



**Figure 5.8:** a) Regime distribution AM Off-Peak b) Regime distribution PM Peak - Freeway

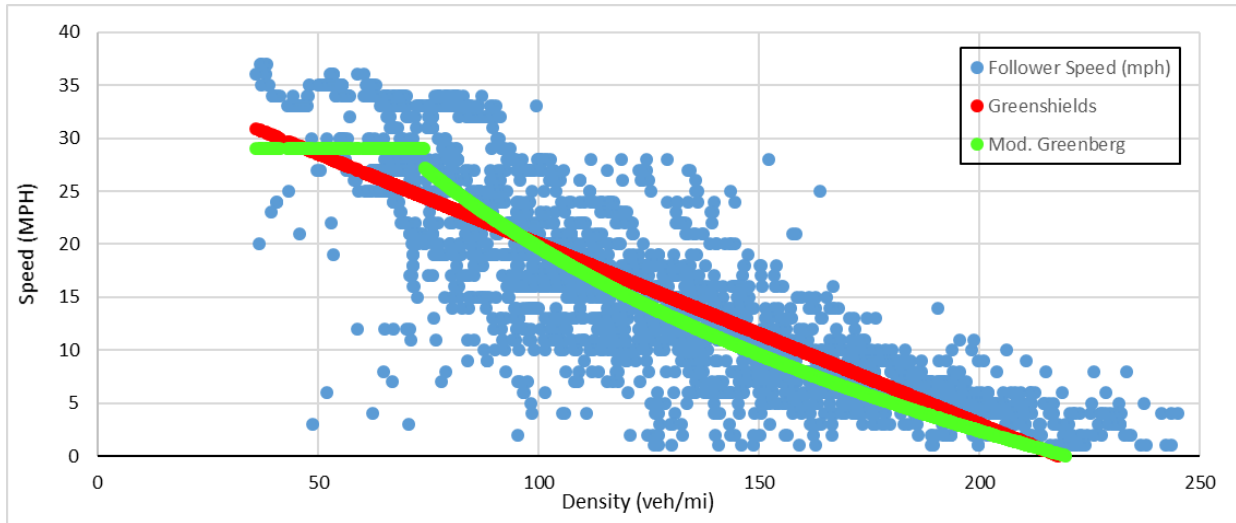
From Figure 5.8a, during the AM off-peak hours, the southbound on I-440 the data is very sparse, mainly because lack of congestion, and in such conditions on the freeways the distance maintained is more than the range of the sensor (40 meters). As shown in Table 5.2, during the PM peak hours there is lack of congestion in the first 1.5 miles sub-segment but, there is a sudden increase in congestion between the 1.5 – 3.5 miles sub-segment, mainly due to the presence of vehicle queues at the exits and speed slowdown at the merges, which can be evidently seen on Figure 5.8b.

## 5.5 Speed vs Density vs Standard Models

In this section, two simple but popular macroscopic traffic stream models– Greenshields, Modified Greenberg– are calibrated to the local density data of the freeway and arterial segments. Details of these two models can be found in this study [23].

### 5.5.1 Arterial Route

The fitted parameters were estimated by minimizing the sum squared differences of the observed and modeled speed. Figure 5.9 shows the observed and fitted speed-density plot.



**Figure 5.9:** Instantaneous Speed-Local Density data vs macroscopic models for Arterial.

Figure 5.9 and Table 5.4 show that Greenshields and Modified Greenberg have a reasonable fit to the observed instantaneous speed and local density data with the Modified R-square value of 70 and 71% respectively. Usually, the traffic stream models are fitted with the freeway data but for the purpose of characterizing the driving behavior, we have used the models for fitting the arterial data as well. The fitted free-flow speed and speed at capacity values are within reasonable ranges given that the posted speed limit at the segments was around 35 MPH. This segment consisted of 4 round-about and 8 signalized intersections.

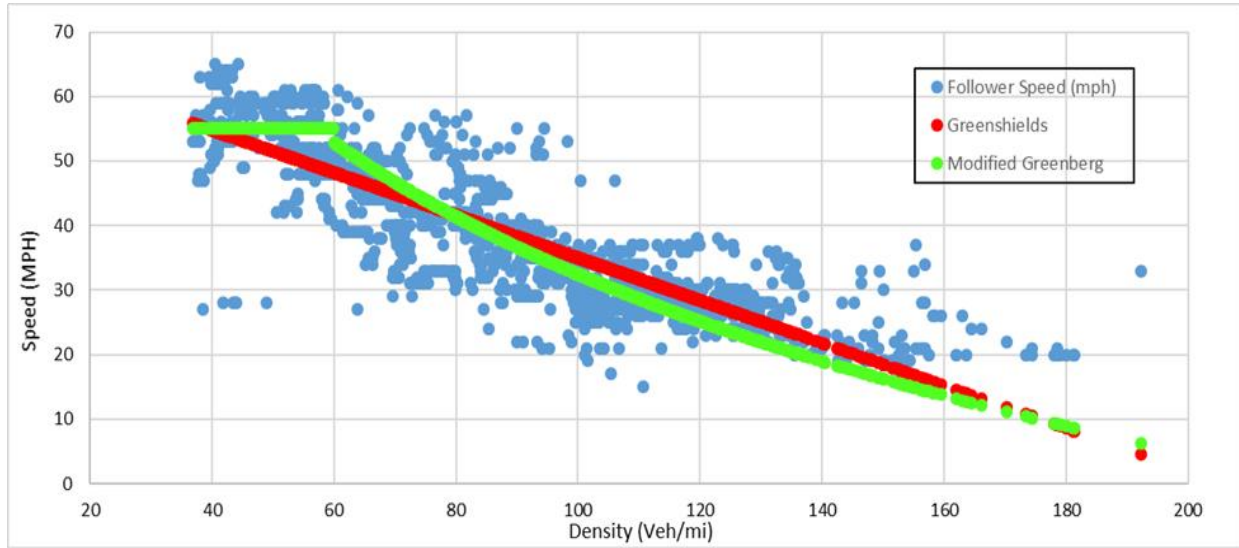


**Table 5.4:** Fitted Traffic Model Parameters - Arterial

Parameters	Greenshields	Modified Greenberg	Units
Free Flow Speed, $v_f$	37	29	MPH
Optimum Speed, $v_m$	N/A	25	MPH
Critical Density, $k_c$	N/A	74	veh/mi
Jam Density, $k_j$	218	220	veh/mi
Speed at Capacity, $v_{ca}$	19	25	MPH
Density at Capacity, $k_{ca}$	109	81	veh/mi
Flow at Capacity, $q_{ca}$	2017	2023	veh/hr
Rsquare	70	71	%
Modified Rsquare	70	71	%

The speed at capacity of 19 MPH and 25 MPH and a free flow speed of 37 MPH and 29 MPH were obtained as best fit values for Greenshields and Modified Greenberg models in the arterial segment respectively. The fitted model has a reasonable Modified  $R^2$  value and well fitted free-flow speed, but the jam density fitted by both the models is on the higher side as the believed range is around 190 – 200 veh/mi, hence in terms of jam density both the models do not fit the data well. The saturation flow rate suggests that the capacity of arterial segments does not exceed 1900 veh/hr [25], while the fitted capacity of the arterial segment is just over 2000 veh/hr for both the models. So, these analyses suggest that the driver was not very aggressive in the arterial segment as the capacity is slightly more than the conventional saturation flow rate.

## 5.5.2 Freeway Route



**Figure 5.10:** Instantaneous Speed-Local Density data vs macroscopic models for Freeway.

Figure 5.10 and Table 5.5 show Greenshields and Modified Greenberg have a reasonable fit to the observed instantaneous speed and local density data with the Modified R-square value of 72 and 70%, respectively. The fitted jam density value matches very closely with the widely used 190 veh/mi [26]. The fitted free-flow speed and speed at capacity values are within reasonable ranges given that the posted speed limit at the segments was 65 MPH. The speed at capacity of 34 MPH and 40 MPH and a free flow speed of 68 MPH and 55 MPH were obtained as best fit values for Greenshields and Modified Greenberg models in the freeway segment respectively. The fitted model has a reasonable Modified  $R^2$  value and well fitted free-flow speed, the expected jam density for a fitted model is expected to be around 190 veh/mi [25]. Hence by comparing the two models based on jam density, the Greenshields model outperforms the Modified Greenberg model. However, the number of observations in a free-flow condition is low in this dataset. This is because vehicles tend to maintain a large headway when traveling at a high speed, while the LIDAR unit used in this research is limited to about 40 meters.

**Table 5.5: Fitted Traffic Model Parameters - Freeway**

Parameters	Greenshields	Modified Greenberg	Units
Free Flow Speed, $v_f$	68	55	MPH
Optimum Speed, $v_m$	N/A	40	MPH
Critical Density, $k_c$	N/A	60	veh/mi
Jam Density, $k_j$	206	225	veh/mi
Speed at Capacity, $v_{ca}$	34	40	MPH
Density at Capacity, $k_{ca}$	103	83	veh/mi
Flow at Capacity, $q_{ca}$	3502	3311	veh/hr
Rsquare	72	70	%
Modified Rsquare	72	70	%

The capacity and the resulting flow at capacity are unusually high from the macroscopic traffic flow perspective. Conventional traffic flow theory suggests that the capacity of freeway segments does not exceed 2,400 veh/hr [25], while the fitted capacity here is above 3,300 veh/hr for both the models. This discrepancy is attributed to the fact that the observed data represent a single individual's naturalistic driving characteristics rather than the average traffic stream characteristics. For an individual driver, the interpretation of observing a flow rate of 3,300 veh/hr is that the driver is driving with a headway of approximately one second. It is unrealistic for all drivers in a traffic stream to keep such a short headway, an individual driver may certainly exhibit such an aggressive characteristic at some instances. These analyses prove that the driver is more aggressive on the freeway than the arterial.

### **5.5.3 Application and Correlation**

Section 5.4, characterizes the driving behavior at different local densities and speed ranges for arterial and freeway segments and section 5.5, characterizes the overall driving behavior. As discussed in section 5.4 the driver is more aggressive at low speeds in the arterial segment than in the freeway segment and at high speeds, the driver was more aggressive in the freeway segment than in the arterial segment. Comparing the overall driving behavior based on predicted flow capacity, section 5.5 proves that the driver was more aggressive in the freeway segment than in the arterial segment. These findings also underscore the importance of such a local-level speed-density analysis for evaluating both naturalistic driving and autonomous vehicle driving algorithms. Hence the methods of characterizing driving behavior as explained in section 5.4 and section 5.5 can be used to notify drivers of their driving behavior at the end of every trip, which might help in improving the quality of driving.

## 6 CONCLUSION AND FUTURE WORK

### 6.1 Goals and Objectives

Evolving from the stationary mode, the dynamic mode of data collection is a promising method for the future. The research describes a system comprising of a LIDAR, which is used to capture gap between vehicles, integrated with a GPS for timestamps, speed, and positional data, and a camera for data validation. A novel 2-stage noise removal process comprising of ARIMA prediction modeling in stage 1 followed by mean filtering in stage 2 is explained in detail. This 2-stage noise removal process refines the raw uninterpretable LIDAR data into a more understandable form. The final output data is a series of car-following data. With autonomous vehicles to hit the market in the near future, such modes of data collection would be more efficient compared to stationary devices.

The core of this research is based on analyzing local density and its applications. Similar sensor-based data is likely to be available with the introduction of connected and autonomous vehicles. Moreover, the data collected is microscale driving behavior data for a single driver with GPS. Also, approaches to model driving behavior have been developed by capturing the varying reaction of the single driver with the longitudinal evolution of local density along a corridor.

The data were used to categorize naturalistic driving trips on arterial and freeway segments both in peak and off-peak periods based on the car following regimes in the Wiedemann car-following models. The data highlighted the differences in the regime allocations between facility types and congestion levels.

Individual driver speed-density relationship can be established based on the local density and instantaneous speed. The speed-density data were fitted with Greenshields and Modified Greenberg model. Analysis was performed to estimate driver behavior using these models.

The developed approach can be repeated for multiple drivers in the traffic stream operating in different localized conditions, including interactions between human driver – human driver, human driver – automated vehicle, light-duty vehicle – heavy-duty vehicle. Such a locally developed driving behavior model will be feasible in the near future due to the predicted pervasiveness of sensor-equipped vehicles and mixed operation of different vehicle types.

## 6.2 Major Findings

This research is entitled to 4 major findings,

- The performance of the 2-stage filtering process is verified through error analysis. ARIMA (0,1,1) prediction model stands out among other ARIMA models by predicting values with the lowest Mean Square Error (MSE) of 0.13meters w.r.t the ground truth and the final output after the 2-stages of filtering has an MSE of 0.08meters w.r.t the ground truth.
- Focusing on the longitudinal car following behavior, the data presented in this research shows that for a lead vehicle within range, a LIDAR sensor can duplicate its trajectory over time. Also, insights on the local density at precise locations across the corridor are obtained, which explains the trend in driver behavior. More importantly, local density as a function of speed can be formulated to describe the driver (or in the case of automation, AV software) behavior.
- Using a combination of microscopic (Wiedemann car-following model) and macroscopic (speed – local density) models, the relation between them is well highlighted, by classifying each valid data point to a specific car-following regime. The analysis verifies that the driver was driving safely if most of the data lie in the free-driving regime than the closing-in regime for high speed & high distances and in the high-density regime than the emergency regime for low speed & low distances.
- The dynamically collected data fits the macroscopic models reasonably as the Modified R-square value was around 70% for both the models in both arterial and freeway segments. The driver behavior was found to be aggressive in the freeway segment as both the models predicted a flow capacity of more than 3300 veh/hr, where the conventional flow capacity according to the HCM-6 model is 2400 veh/hr. In the arterial sections, the predicted flow capacity for both the models were around 2000 veh/hr, where the conventional saturation flow rate according to the HCM 2000 is 1900 veh/hr; hence this proves that the driver was aggressive in the freeway segment when compared to the arterial segment.

## 6.3 Impact

Some of the applications for driver behavior characterization are driving tests, where the driving test inspector can study the driver behavior from the time the learner's license was issued and also during the driving test, and another application would be for insurance companies where insurance

premiums can be based on the driving behavior. Self-motivated drivers who constantly want to drive safely will be interested in such data, to improve their driving behavior and when multiple vehicles have this system, then based on accumulative driver behavior in a region, traffic jams can be predicted. Also, such driving characteristics will help in developing and modeling robust AV software to handle human driving exceptions when AVs coexist with human drivers in mixed traffic conditions.

## **6.4 Limitations**

Some of the limitations of the discussed methodologies and research are listed below;

- While using local density, the data at times can over-report or under-report the actual situation as the data pertains to a single driver; hence it is important to scale this method of data collection and analyze large amounts of data from different drivers in the same segment.
- Depending on the range and capability of the sensor, the local density estimated from the captured gap between vehicles may vary from device to device, which may lead to under-reported ranges of local density. Like in the sensor used for this research, local density below 35 veh/mi cannot be estimated, as the range of the sensor is around 40m.

## **6.5 Future Work**

If vehicle manufacturers provide the data from LIDAR like sensors fixed in the vehicle to the users through the OBD port, then the need for an external sensor can be ruled out, and the data can be directly obtained from the OBD port. However, the raw data might need to be processed. The OBD data can also be wirelessly transferred to smartphones [14] and can be logged to the remote servers. Researchers can post-process the data for noise reduction, and this data can be used to study driving behavior through macroscopic traffic stream models and microscopic car-following regimes such as the Wiedemann model. This data may be used for Fuel Efficiency Score (FES) analysis to study trip-based fuel consumption measures [5]. Further research is proposed in the area of lane-changing behavior, and in determining other safety criteria beyond Wiedemann regimes, such as time to collision and safety margins.

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