Exact and Inexact Methods for Solving the Problem Of View Selection for Aggregate Queries

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Abstract. We present a study of the following warehouse view-selection problem: Given a frequency distribution on parameterized aggregate queries on a data warehouse, return definitions of aggregate views that, when materialized in the warehouse, would reduce the evaluation costs of the frequent queries. Optimizing the layout of stored data using view selection has a direct impact on the performance of data warehouses. However, the optimization problem is intractable, even under natural restrictions on the types of queries of interest. We introduce an integer-programming model to obtain optimal solutions for the warehouse view-selection problem, and propose a heuristic to obtain competitive inexact solutions where our exact method is inapplicable. We show that both our approaches can be used to solve realistic-size instances of the problem. In addition, we experimentally compare our methods to those of Harinarayan et al. (1996) and Shukla et al. (1998), and delineate applicability areas for these and our approaches.

Keywords: business intelligence, data reporting, OLAP, business intelligence cycle, schema specification selection, view selection, data warehouse design, data analysis tools.

1 Introduction

As data warehouses keep growing in size, evaluating many common queries — such as aggregate queries — in OLAP may require significant transformations of large volumes of stored data. Aggregate queries are widely used in data warehouses and decision support. Optimization based on the reuse of query answers is particularly promising for aggregate queries, as often an enormous amount of data is scanned to produce a single aggregate value. As a result, the requirement of good overall performance of frequent and important business intelligence queries necessitates optimal choices in choosing and executing query plans. A significant aspect of query performance is the choice of auxiliary data (e.g., indexes) used in query answering. In modern commercial database systems, a common type of auxiliary data is materialized views — relations that were computed by answering certain queries on the (original) stored data in the database and that can be used to provide, without time-consuming runtime transformations, “precompiled” information that is relevant to the user query. We give an example of using materialized views to answer select-project-join queries with aggregation in a star-schema (see Kimball et al. (2002)) data warehouse.

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Example 1. Consider a data warehouse with three stored relations: Sales(CID, DateID, QtySold, Discount), Customer(CID, CustName, Address, City, State), and Time(DateID, Day, Month, Year). Here, Sales is the fact table, and Customer and Time are dimension tables.

Let the query workload have two queries, Q1 and Q2. Q1 asks for the total quantity of products sold per customer in the last quarter of the year 2006. Q2 asks for the maximal product quantity sold per year for all years after 2000 to customers in North Carolina.

Q1: SELECT c.CID, SUM(QtySold)
FROM Sales s, Time t, Customer c
WHERE s.DateID = t.DateID AND s.CID = c.CID
AND Year = 2006 AND Month >= 10 AND Month <= 12
GROUP BY c.CID;

Q2: SELECT t.Year, MAX(QtySold)
FROM Sales s, Time t, Customer c
WHERE s.DateID = t.DateID AND s.CID = c.CID
AND Year > 2000 AND State = 'NC'
GROUP BY t.Year;

We can use techniques from Harinarayan et al. (1996) to show that the following view V can be used to give exact answers to each of Q1 and Q2.

V: SELECT s.CID, Year, Month, State, SUM(QtySold) AS SumQS, MAX(QtySold) AS MaxQS
FROM Sales s, Time t, Customer c
WHERE s.DateID = t.DateID AND s.CID = c.CID GROUP BY s.CID, Year, Month, State;

Evaluating the queries Q1 and Q2 using the view V is likely to be more efficient than using their original definitions, as using V allows the DBMS to avoid taking expensive joins of the stored tables and may also save some time in grouping and aggregation. □

We consider the following warehouse view-selection problem: Given a frequency distribution on parameterized aggregate queries on a star-schema data warehouse, and given a set of constraints (e.g., a storage limit on the amount of disk space that can be used to store materialized views), return definitions of views that, when materialized, would satisfy the constraints and reduce the evaluation costs of the frequent queries. As design of materialized views is an important component of query processing in data warehouses (see Baralis et al. (1997), Harinarayan et al. (1996), Kalmis et al. (2002), Shukla et al. (1998), Theodoratos et al. (1997), and Yang et al. (1997)) and of automated query-performance tuning (see IBM and Microsoft; Shasha et al. (2002)), the problems of selecting views and of answering queries using views have been studied thoroughly in the literature.

Generally, spending more time on designing views tends to pay off, as greater improvement can thereby be achieved in the query performance. As the number of beneficial views tends to be prohibitive even for simple query workloads (Agrawal et al. (2000); Chirkova et al. (2002); Harinarayan et al. (1996)), it is not practical to use exhaustive enumeration to obtain derived data that would globally minimize query costs. Several approaches (see, e.g., Agrawal et al. (2000); Gupta et al. (1997); Harinarayan et al. (1996); Shukla et al. (1998)) have been proposed to efficiently design good-quality sets of derived data for SQL queries. We continue the work of Gupta et al. (1997) and Harinarayan et al. (1996) of studying view-selection algorithms that are competitive, that is, provide optimality guarantees on their outputs without necessarily exploring the entire search space of views. We present a formal model of warehouse view selection, explore competitive techniques for designing and using views in this context, experimentally compare our techniques to previous approaches of Harinarayan et al. (1996) and Shukla et al. (1998), and delineate applicability areas for all of the methods involved.

Our specific contributions are as follows:
1. We model warehouse view selection as an integer-programming (IP) problem and give references to similar IP structures in the literature. Our exact method for solving the view-selection problem uses our IP model and returns optimal solutions. In addition, we propose an heuristic that reduces, in the input to the IP model, the size of the search space of useful views, and provides an inexact method for solving the problem.

2. With our IP model and heuristic, we use standard IP-solver software to solve optimally or near-optimally realistic-size instances of the problem on the popular TPC-H benchmark (described in TPC-H) and on real data in the Sloan Digital Sky Survey (SDSS) dataset (described in Szalay et al. (2002)).

3. We study the applicability of our exact and inexact methods for two versions of the view-selection problem, determined by whether the table for the view resulting from joining all the base relations (we call this view raw-data view) is part of the solution.

4. We experimentally compare our two methods with the heuristic approaches of Harinarayan et al. (1996) and Shukla et al. (1998) and delineate the applicability areas of each approach.

In our experiments we solved hundreds of problem instances, both on TPC-H data (described in TPC-H) and on the SDSS dataset (described in Szalay et al. (2002)). The problem instances used both randomly generated query workloads and queries related by the ancestor-descendant relationship in the sense of the structure used by Harinarayan et al. (1996).

After outlining related work, in Section 2 we provide the background and formal definitions. Section 3 introduces our IP model of the view-selection problem. We report our experimental results and theoretical analysis in Section 4 (for our IP model) and in Section 5 (for the heuristic we propose in the same section). We report our comparative experiments and our comparison conclusions in Section 6.

Related Work

Designing and using derived data to improve query performance has long been studied in data-intensive systems. A wealth of theoretical results (see Halevy (2001) for a survey) and some practical solutions by Agrawal et al. (2001), Chaudhuri et al. (1995), and Chaudhuri et al. (1998) have been accumulated on using views and indexes in query answering. Answering aggregate queries using views was considered in relation to data warehouses and data cubes by Agarwal et al. (1996), Chaudhuri and Dayal (1997), Gray et al. (1997), and Widom (1995); results on answering each query using a single view were presented by Gupta et al. (1995), and Srivastava et al. (1996). Recent work of Afrati and Chirikova (2005) and Cohen et al. (1999) considered rewriting aggregate queries using multiple views.

Considerable work has been done on efficiently selecting views and indexes for general SQL queries by Agrawal et al. (2000) and in particular for aggregate queries (e.g., the works by Afrati and Chirikova (2005), Gupta et al. (1997), Harinarayan et al. (1996), Kalnis et al. (2002), and Shukla et al. (1998)). Yang et al. (1997) proposed algorithms, including an IP approach, for selecting materialized views to minimize the sum cost of processing the given queries and of maintaining all the views. Agrawal et al. (2000), and Agrawal et al.
(2001) introduced an end-to-end approach and a system architecture for designing and using materialized views and indexes to answer queries.

In this paper we study the problem of selecting views for aggregate queries on star-schema data warehouses. The setting and assumptions we use generalize those by Gupta et al. (1997), Harinarayan et al. (1996), Kalnis et al. (2002), and Shukla et al. (1998) (in contrast to those by Yang et al. (1997)) — that is, we seek to minimize the total execution costs of the frequent queries under a storage-limit constraint. At the same time, one novelty of our work is in obtaining efficiently optimal or near-optimal solutions for problem instances of realistic sizes, for two versions of the view-selection problem. In the first version, we assume similarly to the approach by Harinarayan et al. (1996) that the raw-data view is always part of the solution set of materialized views. We lift this restriction in the second version of view selection; the resulting problem arises in practice in settings where it is too expensive to maintain efficiently the result of joining all base tables, including data-integration settings where certain views are materialized in the mediator to improve query-processing efficiency (see Halevy (2001)). Our extensive experimental evaluation of the proposed methods allows us to delineate applicability areas for our approaches to view selection, as well as for the methods by Harinarayan et al. (1996), Kalnis et al. (2002), and Shukla et al. (1998).

2 Preliminaries and Problem Specification

We consider relational select-project-join queries with grouping and aggregation (SPJGA queries), posed on star-schema data warehouses (Chaudhuri and Dayal (1997); Kimball et al. (2002)). Similarly to Gupta et al. (1997); Harinarayan et al. (1996); Kalnis et al. (2002); Shukla et al. (1998), we assume application settings where users frequently ask a limited number of parameterized SPJGA queries, such as itemized daily/weekly/monthly sales reports for a variety of parameters for products, locations, etc. Thus, we assume parameterized queries, by allowing arbitrary constant values (i.e., placeholders instead of fixed constants) in the WHERE clauses of the queries, and assume that specific values of these constants are not known in advance.

We consider star-schema data warehouses with a single fact table and a small fixed number of dimension tables, under the following realistic assumptions. First, in each base table all rows have a single fixed (upper bound on) length. Second, the fact table has many more (in fact, magnitudes more) rows than each dimension table. Finally, we assume that each base table has a single index, on the table’s key.

Our cost model is as follows. We consider the costs of answering queries using unindexed materialized views, such that each query can be evaluated using just one view and no other data, as in Example 1. (This setting is the same as in Harinarayan et al. (1996); Kalnis et al. (2002); Shukla et al. (1998).) Given a query workload $Q$ and a set of views $V$ that have been precomputed on a database $D$, the total cost of evaluating $Q$ using $V$ is the sum of the costs of evaluating all the queries in $Q$, such that each query is evaluated using a view in $V$. The sum is weighted to reflect the relative frequency (or importance) of individual queries.
We consider the following warehouse view-selection problem: Given a star-schema data warehouse and for a given frequency distribution on parameterized SPJ queries, our goal is to minimize the evaluation costs of the queries, by selecting and precomputing views that can be used in answering the queries. We consider this minimization problem under a storage-space limit, which is an upper bound on the amount of disk space that can be allocated for the views. Thus, our problem inputs are of the form $I = (D, Q, b)$, where $D$ is a database, $Q$ is a workload of parameterized queries, with a frequency/importance value $f_j$ for each query $j$ in $Q$, and $b$ is the (positive integer) value of the storage limit.

We use the following definitions of solutions and of the optimal viewset problem (OVP):

**Definition 1.** For a problem input $I = (D, Q, b)$, a set of views $V$ is an admissible viewset if (1) each query in $Q$ can be rewritten using $V$, and (2) $V$ satisfies the storage limit $b$.

**Definition 2.** For a problem input $I = (D, Q, b)$, an optimal viewset is a set of views $V$ defined on $D$, such that (1) $V$ is an admissible viewset for $I$, and (2) $V$ minimizes the cost of evaluating $Q$ on the database $D_V$, among all admissible viewsets for $I$. Here, $D_V$ is the database that results from adding to $D$ the relations for all the views in $V$ computed on $D$.

**Definition 3.** (Problem OVP) For a given problem input $I = (D, Q, b)$, find an optimal viewset. A solution for a given instance of OVP consists of a set of materialized views $V$ (which includes the raw-data view on $D$ and all additional views that we choose to materialize) and an association between each element of $Q$ and its corresponding element of $V$.

We also consider a variation OVP$'$ of the optimal-viewset problem: Unlike OVP, in OVP$'$ we do not require that the raw-data view be materialized as part of the solution. In Section 4 we present an experimental comparison of two versions of our proposed approach, one for OVP and the other for OVP$'$.

For the class of SPJGA queries that we consider, our search space of views is the view lattice introduced by Harinarayan et al. (1996) and adopted in a number of research projects, including those by Kalnis et al. (2002) and Shukla et al. (1998). We now discuss and justify our choice of the search space of views and our cost model.

The view lattice described in Harinarayan et al. (1996) that we use as our search space includes all star-join views with grouping and aggregation (JGA views) on the base tables, such that each view has aggregation on all the attributes aggregated in the input queries, using all the aggregation functions used in the queries. Such views, illustrated by view $V$ in Example 1, are called “multiaggregate views” (see Afrati and Chirkova (2005)). A SPJGA query $Q$ can be answered using a JGA view $V$ if the grouping attributes of $V$ are a superset of the union of attributes in the GROUP BY clause of $Q$ and of the attributes in the WHERE clause of $Q$ that are compared to constants. By definition, each query $Q$ can be answered using the top view (raw-data view) in the lattice.

In our cost model, the cost of answering a single SPJGA query using a JGA view is the size of the view, as justified in Harinarayan et al. (1996), Kalnis et al. (2002), and Shukla et al. (1998). Note that in our problem setting, given an input query $Q$ and a view $V$ that can answer $Q$, it is enough to compare the cost of answering $Q$ using $V$ to the cost of answering...
Q using only the raw-data view, rather than to the cost of answering Q using the original base relations in the data warehouse. The reason is, under our assumptions these two costs are directly proportional to each other.

We now argue why considering just the views in our JGA view lattices is a reasonable option in finding optimal or near-optimal sets of views to materialize when seeking to minimize the costs of answering sets of parameterized SPJGA queries under a storage limit. (Whenever we refer to finding optimal solutions of this problem, we consider optimality with respect to our view lattices.) First, it is more efficient to answer any SPJGA query using a single JGA view than using a query plan that involves joins of base relations or views. Second, when the values of the constants of a parameterized query are not known in advance, the only option to minimize the response time of all queries in Q is to materialize a single eligible JGA view. Finally, using multiaggregate JGA views permits us to use a single view to answer queries with different aggregation functions, as illustrated by Example 1.

3 Integer Programming Models for OVP and OVP’

In this section we propose integer programming (IP) models for the optimal-viewset problems OVP and OVP’, and discuss methodologies for solving these IP models. Since we use these IP models to obtain globally optimal solutions for OVP and OVP’, we refer to this approach as an “exact method” for solving OVP and OVP’.

We use the following notation to represent the input $\mathcal{I} = (\mathcal{D}, Q, b)$ in our IP model:

$\alpha_i$ : Size of the view $i$, for all $i \in IV$, where IV is the index set for all possible views;

$\beta$ : storage limit;

$\gamma_{ij}$ : evaluation cost of answering query $j$ by using view $i$, for all $i \in IV$ and $j \in Q$.

We let $c_{ij} = +\infty$ if view $i$ cannot be used to answer query $j$; otherwise we have $c_{ij} = \alpha_i \cdot f_j$, where $\alpha_i$ is as defined above and $f_j$ is the frequency (or importance) of query $j$. We further define the following decision variables for the IP model.

\[ x_i = \begin{cases} 
1 & \text{if view } i \text{ is materialized} \\
0 & \text{otherwise} 
\end{cases} \quad \text{for all } i \in IV \\
\]

and

\[ y_{ij} = \begin{cases} 
1 & \text{if we use view } i \text{ to answer query } j \\
0 & \text{otherwise} 
\end{cases} \quad \text{for all } i \in IV \text{ and } j \in Q \\
\]

The optimal-viewset problem OVP can now be stated as the following IP model.

\[
\begin{align*}
\text{Minimize} & \quad \sum_{i \in IV} \sum_{j \in Q} c_{ij} y_{ij} \\
\text{subject to} & \quad \sum_{i \in IV} \alpha_i x_i \leq b \quad \text{(1)} \\
& \quad \sum_{i \in IV} y_{ij} = 1 \quad \forall j \quad \text{(2)} \\
& \quad y_{ij} \leq x_i \quad \forall i, j \text{ such that } c_{ij} \neq +\infty \quad \text{(3)} \\
& \quad x_1 = 1 \\
& \quad x_i, y_{ij} \in \{0, 1\} \quad \forall i, j \\
\end{align*}
\]

(OVIP)
Constraint (1) limits the size of the materialized views to be no more than the storage space $b$. Constraint (2) states that each query is answered by exactly one view in the set of views. Constraint (3) guarantees that query $j$ can be answered by view $i$ only if view $i$ is already materialized. Constraint (4) states that the raw-data view is always materialized. The remaining constraints are simply the binary requirements for $x_i$ and $y_{ij}$.

We can also modify this model into an IP model for the problem $OVP'$ (see note after Definition 3 in Section 2) by removing constraint (4). This is equivalent to stating that the raw-data view is not required to be materialized. We refer to this modified model as $OVIP'$.

The structure of this IP model is similar to those for the uncapacitated facility location problem (UFL) and the $k$-median problem. These two problems are well studied in the literature, and relatively large instances of the corresponding IP models can be solved within reasonable time. Several heuristic approaches for solving these problems have also been reported. See Cormenjols et al. (1984) and Krarup et al. (1983) for the facility location problem and Mulvey et al. (1979) for the $k$-median problem.

A key difference between this IP model and those for the UFL and $k$-median problems is the presence of relatively large numbers of variables in this model due to the large size of the index set $IV$. If we have $K$ attributes in the data base, the corresponding size of the set $IV$ is $2^K$, which leads to $2^K$ variables of type $x_i$ and $|Q| 2^K$ variables of type $y_{ij}$. For a lattice with $K = 15$ attributes this implies 32,708 $x_i$-variables and 32,708 $|Q|$ $y_{ij}$-variables. Comparatively, in a typical UFL or $k$-median problem the size of the corresponding $IV$ set is no more than a few hundreds. As a result, the algorithmic strategies that are proven to be effective for solving those models turn out to be not as effective for solving $OVIP$. In Sections 4 and 5 we discuss some strategies for reducing the size of the set $IV$ and thereby the size of the corresponding $OVIP$ model.

Note that due to the special structure of this IP model the binary requirement for $y_{ij}$ can be replaced by a simple non-negativity restriction without affecting the corresponding optimal solution for this model. See Parker et al. (1988) for a discussion of this subject and its theoretical underpinning. This relaxation has a significant impact on reducing the overall computational effort required to solve the IP model, and we use it throughout this paper and in all our experiments.

4 A Computational Experiment with the IP Model

As discussed in Section 3, solving the proposed IP models $OVIP$ or $OVIP'$ allows us to obtain optimal (exact) solutions to problems $OVP$ or $OVP'$, respectively. In this section we discuss the results of an experiment that we conducted in order to investigate various computational aspects of the proposed model, and determine the limits on the size of problem instances that we can solve in practice using this approach and with today’s technology. We put our results in perspective in Section 6.

We begin by proposing an approach for reducing the search space of views in our exact method. As mentioned earlier, a key hurdle in solving realistic instances of the IP model $OVIP$ (or $OVIP'$) is the relatively large number of variables in the model, in particular the binary variables $x_i$. The maximum number of such variables is equal to the size of the set
IV, i.e., $2^K$. In practice we can reduce the size of IV — and hence the number of variables in the model — without affecting the optimal value of OVIP (or OVIP'), by removing from this set every view $i$ that cannot be used to answer at least one of the queries in the set $Q$ (for obvious reasons no such view can be in the optimal solution of OVIP or OVIP'). We refer to the resulting (reduced) index set as $IV'$. The reduction in size (i.e., $IV'$ versus $IV$) depends on the specific queries in the set $Q$. For each instance in our experiment we construct the corresponding reduced set $IV'$ and report its size.

To determine the limits of the size of the instances that we can solve in practice using our exact method, we constructed and solved a large collection of instances of the problem. All experiments were run on a machine with a 3GHz Intel P4 processor, 1GB RAM, and a 80GB hard drive running Windows XP SP2, and using the IP solver CPLEX/AMPL 9.0. This software uses a branch-and-bound algorithm for solving the IP model, and solves the corresponding linear programming relaxation models using the simplex algorithm.

In Section 4.1 we discuss the datasets that we used in the experiments. In Section 4.2 we report the execution time for a collection of instances from these datasets, and make some observations. Finally, in Section 4.3 we present the results of further experiments that offer additional insight on the applicability of our proposed exact methods.

4.1 Datasets

We used two datasets in our experiments: (1) a TPC-H database benchmark (TPC-H), and (2) a real dataset which is a modified version of the Sloan Digital Sky Survey (SDSS) dataset (Szalay et al. (2002)). Figure 1 shows the sizes of the stored tables for the TPC-H dataset. Size estimates for the lattice were obtained by running the queries for all views on the TPC-H stored data with scale factor of 0.1 and by extrapolating the answer sizes to the sizes of the data (scale factor of 1) used in the experiments. For the SDSS dataset, whose sizes of the stored tables are shown in Figure 2, the view sizes were measured on the original database. The observations we made in our experiments were consistent across the two datasets; therefore, in reporting our results in this section we only use examples from the TPC-H dataset.

4.2 Execution Time

The execution times that we report here pertain to instances from four different TPC-H datasets, i.e., raw-data views with 7, 13, 15, and 17 attributes. (To obtain some raw-data views for the experiments, we used joins of TPC-H tables.) The number of nodes in the view lattices (i.e., the size $|IV|$ of the set IV) for these datasets are 128, 8192, 32768, and 131072, respectively. For each raw-data view we constructed the IP model OVIP for several instances of the problem, each instance with a different query workload $Q$ and storage limit $b$. We solved each instance using the software package CPLEX/AMPL with a time limit of thirty seconds on the execution time. In Table 1 we give detailed characteristics of twelve

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3 In fact, since in our view lattice we have $a_i \geq a_j$ for every pair $(i,j)$ such that view $i$ is an ancestor of view $j$, we can go even further and exclude each node that is not an ancestor of at least two queries in the set $Q$. 

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instances of the problem that we could solve within this time limit. Each row of this table corresponds to one instance and gives the number of attributes, the size of the view lattice, the number of queries in the workload \( Q \), and the storage capacity for that instance. For all instances in this experiment we assume that the frequency \( f_j \) associated with each query \( j \) in \( Q \) is equal to 1. For each instance we also give the size \( |IV'| \) of the set \( IV' \), the corresponding number of \( x_i \) and \( y_{ij} \) variables, and the associated execution time that we measured for solving that instance. We make the following observations.

1. Aside from the number of attributes and queries, the size of the IP model (as measured by the number of \( x_i \)-variables) and its corresponding execution time also depend on the number of view-lattice nodes that are actually included in the model, i.e., on the cardinality of the set \( IV' \). This size is usually larger if some workload queries are placed relatively low in the lattice. Hence, the largest IP model in our experiment does not necessarily pertain to the instance with the largest number of attributes and/or queries. In fact, the largest IP model that we were able to solve within our stated time limit was for instance 11 in Table 1, which is on a 17-attribute lattice with 5 queries. This model has 20,136 \( x_i \)-variables and 100,680 \( y_{ij} \)-variables, and its execution time is 7.03 seconds. The largest instance of \( OVP \) that we were able to solve, however, pertains to instance 12 in Table 1 which is also on the 17-attribute lattice and has 15 queries. The corresponding IP model has 13,755 \( x_i \)-variables and 206,325 \( y_{ij} \)-variables, and its execution time is only 2.64 seconds (see Asgharzadeh Talebi et al. (2005)). Further, the largest IP model does not necessarily pertain to the longest overall execution time, since the latter also depends on the growth of the search tree in the context of the branch and bound algorithm. In fact, the longest execution time in our experiments pertains to instance 4 in Table 1 with a 7-attribute view lattice and 50 queries. The corresponding IP model has 112 \( x_i \)-variables and 560 \( y_{ij} \)-variables, and its execution time is 13.00 seconds.

2. In many instances, while solving the IP model we also observed that the runtime of CPLEX/AMPL for solving the model is only slightly larger than its runtime for solving the corresponding LP relaxation. Intuitively, a reason for this phenomenon could be that

| Instance ID | Num. of attr. | \(|IV|\) | Num. of queries in the workload | Capacity (num. rows) | \(|IV'|\) | Num. of \(x_i\)'s | Num. of \(y_{ij}\)'s | Execution time (sec.) |
|-------------|---------------|----------|---------------------------------|----------------------|----------|----------------|------------------|----------------------|
| 1           | 7             | 128      | 7                               | 702,709              | 60       | 60            | 60 \(\times\) 7   | 0.12                 |
| 2           | 7             | 128      | 15                              | 2,237,482            | 73       | 73            | 73 \(\times\) 15   | 0.03                 |
| 3           | 7             | 128      | 20                              | 2,796,908            | 76       | 76            | 76 \(\times\) 20   | 0.07                 |
| 4           | 7             | 128      | 50                              | 5,020,880            | 112      | 112           | 112 \(\times\) 50  | 13.00                |
| 5           | 13            | 8,192    | 5                               | 604,668              | 5,984    | 5,984         | 5,984 \(\times\) 5 | 0.85                 |
| 6           | 13            | 8,192    | 8                               | 1,264,194            | 4,104    | 4,104         | 4,104 \(\times\) 8 | 0.45                 |
| 7           | 13            | 8,192    | 30                              | 4,535,645            | 2,893    | 2,893         | 2,893 \(\times\) 30 | 1.55                 |
| 8           | 15            | 32,768   | 5                               | 1,002,359            | 4,468    | 4,468         | 4,468 \(\times\) 5 | 0.45                 |
| 9           | 15            | 32,768   | 8                               | 1,522,810            | 17,464   | 17,464        | 17,464 \(\times\) 8 | 3.89                 |
| 10          | 15            | 32,768   | 20                              | 3,291,654            | 3,389    | 3,389         | 3,389 \(\times\) 20 | 1.20                 |
| 11          | 17            | 131,072  | 5                               | 890,108              | 20,136   | 20,136        | 20,136 \(\times\) 5 | 7.03                 |
| 12          | 17            | 131,072  | 15                              | 2,101,790            | 13,755   | 13,755        | 13,755 \(\times\) 15 | 2.64                 |

Table 1. Description of the twelve problem instances in the experiments.
the lower bound obtained for OVIP via its LP relaxation is relatively strong, hence it leads to quick fathoming of most branches in the corresponding branch-and-bound tree. This observation is not uncommon among other IP models with similar structures, such as the UFL problem that we mentioned earlier. In our experiments, every time that CPLEX/AMPL was not able to solve the IP model within our stated time limit, it was also unable to solve its LP relaxation. We report on the quality of this lower bound in detail in Li et al. (2005).

3. The execution time is expected to grow at an exponential rate with the size of the IP model; hence we do not expect it to be practical to solve much larger instances of this IP model using CPLEX/AMPL. At the same time, the instances that we are able to solve are of realistic sizes in practice (cf., e.g., the problem instances used in the experiments in Shukla et al. (1998)), as exemplified in the last few instances in Table 1. This demonstrates that we can use a standard IP solver to obtain verifiably optimal solutions for practical instances of the problem.

4. In our experiments we also studied whether the ancestor-descendant relationships between workload queries influence the runtime or outcome for our approach. In particular, we studied problem instances with “single-path” query workloads, that is, with workloads $Q$ where for each query $Q \in Q$, each remaining query in $Q$ is either a descendant or an ancestor of $Q$ in the view lattice. It is observed in Kotidis et al. (1999) that workload queries with such relationships are likely to occur in query sessions by a single user in data warehouses, where the user performs roll-ups and drill-downs on the data of interest. In our study, we did not observe significant differences in the runtime or outcome for our approach depending on the type of relationships among workload queries. Rather, as mentioned earlier, we observed that the placement of individual queries in the view lattice has a bigger influence on how efficiently the problem instance can be solved by our approach.

4.3 Further Experimental Observations

In addition to observing the execution time for solving the OVIP model as reported above, we also carried out several related experiments with this IP model. In this section we present a summary of our findings.

An alternative measure for size requirement: View sizes and query costs are typically measured in units of rows (see, e.g., Gupta et al. (1997); Harinarayan et al. (1996); Shukla et al. (1998)). At the same time, the units of bytes are the actual measure of storage requirements and of query costs in database-management systems, because the cost of answering a query using a view is proportional to the number of disk blocks occupied by the view. In order to investigate any possible effect that this modification in units might have on the execution time for solving the IP model, we ran additional experiments where we expressed in bytes both the size requirement for the views and the cost of answering queries using those views. We observed that changing the units does not have any appreciable impact on the execution time for the IP model, but it could result in different optimal solutions. The results for four representative instances are reported in Table 2.
As units of bytes (instead of rows) is a more realistic measure in the context of view selection, we posit that these units should be employed as the primary units of measurement in problem input. Further details are available in Li et al. (2005).

<table>
<thead>
<tr>
<th>Instance ID</th>
<th>Num. of grouping attrib.</th>
<th>Query workload (query indexes)</th>
<th>Units of rows</th>
<th>Units of bytes</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>storage limit</td>
<td>optimal viewset</td>
</tr>
<tr>
<td>1</td>
<td>7</td>
<td>{55, 59, 125, 126}</td>
<td>899,418</td>
<td>{55, 126, 127}</td>
</tr>
<tr>
<td>2</td>
<td>7</td>
<td>{1, 7, 53, 76, 111, 115}</td>
<td>1,084,770</td>
<td>{1, 53, 76, 127}</td>
</tr>
<tr>
<td>3</td>
<td>13</td>
<td>{1792, 3013, 5392, 6096, 7063}</td>
<td>900,541</td>
<td>{1792, 5392, 8191}</td>
</tr>
<tr>
<td>4</td>
<td>13</td>
<td>{1185, 5224, 6401, 6672}</td>
<td>836,835</td>
<td>{6401, 6672, 8191}</td>
</tr>
</tbody>
</table>

Table 2. Solving the OVIP problem for units of rows and bytes.

**Solving the OVIP' model:** Recall that the only difference between OVIP and OVIP' is that in OVIP' the top raw-data view in the view lattice is not required to be materialized. This version of the problem can arise, for instance, in situations where it may be too expensive to maintain the raw-data view relation, and it is desirable to explore solutions which do not force that relation to be materialized. These situations include data-integration settings where certain views are materialized in the mediator to improve query-processing efficiency (see Halevy (2001)). (Recall that in many cases, the top raw-data view in the view lattices by Harinarayan et al. (1996) is the result of joining several base relations in the star schema.) We carried out a set of experiments in which we constructed and solved several instances of the OVIP' model and compared the results with those for the corresponding OVIP models. The details of our experiments are presented in Asgharzadeh Talebi et al. (2005) and Li et al. (2005). In these experiments we observed the following:

- there is no appreciable difference between the computational requirements for solving OVIP and OVIP', and
- although in some instances the results obtained via OVIP and OVIP' are identical (i.e., OVIP' selects the raw-data view in the optimal set), there are also many instances for which OVIP' obtains solutions with significantly smaller objective-function values.

5 **A Heuristic Procedure for Solving OVIP**

In this section we present an inexact (heuristic) method for solving the optimal viewset problem OVIP. The main idea used in this heuristic method is to further prune the search space for candidate views and hence the size of the corresponding IP model, thus allowing larger instances of the problem to be solved in reasonable execution time. Of course when we do so, we can no longer guarantee that the optimal solution for the IP model OVIP (or OVIP') is in fact optimal for the corresponding problem OVP (or OVP').

As observed in Section 4, a key issue in the context of practical solvability of the IP model OVIP (or OVIP') is the size of the corresponding reduced viewset IV'. Recall that the size of this set can be quite large even if the number of queries in the set Q is relatively small. As long as we wish to guarantee that the optimal solution for OVIP (or OVIP') is
in fact optimal for the underlying \( OVP \) (or \( OVP' \)), we need to include all elements of the candidate set \( IV' \) in the IP model. But if we do not seek this guarantee of optimality, we can further reduce the size of the set by removing all elements (i.e., nodes of the lattice) that we deem as not-so-promising elements of the set \( IV' \) in the IP model. This could lead to significant reduction in the size of the corresponding model \( OVIP \) (or \( OVIP' \)).

To this end we limit ourselves to a subset of \( IV' \) consisting of views that either correspond to some queries in \( Q \) or are ancestors of two or more of these queries. We define a view (or query) \( v_1 \) to be an ancestor for another view (or query) \( v_2 \) if the collection of attributes that define \( v_2 \) is a proper subset of the collection of attributes that define \( v_1 \); in this context we refer to \( v_2 \) as the child (or descendant) of \( v_1 \). We refer to the resulting collection of views as a restricted viewset \( IVr \). We then construct and solve the corresponding IP model with this restricted viewset, which would likely have fewer variables than the original \( OVIP \) (or \( OVIP' \)). We refer to this IP model as \( OVIPr \) (or \( OVIPr' \)). In Section 5.1 we outline a procedure by which we construct the restricted viewset \( IVr \) and the resulting input matrix for the corresponding IP model, and discuss its computational requirements. In Section 5.2 we report the results of a computational experiment with the corresponding IP model \( OVIPr \).

5.1 Restricted Viewset \( IVr \)

Given a dataset \( D \) with \( k \) attributes and a set of queries \( Q \) on \( D \), we define \( Q' \) to be a subset of \( Q \) consisting of those elements of \( Q \) that are not themselves a child or a descendant of another element of \( Q \). We now define a node of the view lattice to be an \( i \)-level ancestor of \( Q \), for \( i = 2, 3, \ldots, |Q'| \), if it is an ancestor for \( i \) distinct elements of \( Q' \) and its size is less that the sum of the sizes of these distinct elements. Using this terminology, we refer to the views associated with elements of the set \( Q' \) as the 1-level ancestors of \( Q \). For all \( r \) such that \( 1 \leq r \leq |Q'| \), we define the \( r \)-level restricted viewset for \( Q \) as the set of all \( i \)-level ancestors of the set \( Q \) for all \( i \in \{1, \ldots, r\} \). This \( r \)-level restricted viewset is the set of views in the view lattice that we use to construct the corresponding restricted version \( OVIPr \) of the IP model \( OVIP \).

Note that if we let \( r = |Q'| \) then the resulting \( OVIPr \) is guaranteed to produce an optimal solution for the original problem. At the same time, this IP model could be quite large. We submit that even if we limit the value of \( r \) to be much smaller than \( |Q'| \), members of the \( r \)-level restricted viewset \( IVr \) form a potentially promising collection of views for the queries in \( Q \). Hence the resulting IP model \( OVIPr \) is likely to produce good solutions for the original problem. Note that for low values of \( r \) the size of the resulting IP model \( OVIPr \) would be significantly smaller than the size of the original \( OVIP \), hence an IP solver such as CPLEX is likely to solve this problem with noticeably lower execution time. But as stated earlier, when we use \( OVIPr \) with \( r < |Q'| \) we can no longer guarantee that its optimal solution is also optimal for the original \( OVP \). When we employ the IP model with the \( r \)-level restricted viewset \( IVr \) to solve a given problem \( OVP \) (or \( OVP' \)), we refer to the resulting procedure as the \( r \)-level heuristic procedure. In the next subsection we report the results of a limited computational experiment with this model.
At this point we need to be mindful of the additional computational effort required to construct the restricted viewset $IV_r$ and the corresponding IP model $OVIP_r$. This computational effort is proportional to the maximum number of nodes in the set $IV_r$, i.e., $\sum_{i=1}^{r} C_i^{\|Q\|}$, where $C_i^{\|Q\|} = \binom{\|Q\|}{i-\|Q\|}$ is the combination $\|Q\|$ choose $i$.

In this heuristic procedure, there are two major steps: In the first step we build the restricted viewset $IV_r$ consisting of $\sum_{i=1}^{r} C_i^{\|Q\|}$ views. In order to build a view at level $i$, for $2 \leq i \leq r$, we need to take the union of the attributes of $i$ distinct queries. The order of complexity of this operation is $O(i)$. Thus, the computational requirement of this step is $O(\sum_{i=1}^{r} iC_i^{\|Q\|})$. The second step is to build the input matrix for the corresponding IP model. To do so, for each selected view we need to find out which of the $|Q|$ queries in the query workload can be answered by that view. In the worst case, for each view this will take time $O(|Q|k)$, where $k$ is the number of attributes in the lattice. Thus, the computational requirement of this step is $O(|Q|k\sum_{i=1}^{r} C_i^{\|Q\|})$. Considering the computational requirements of these two steps, the overall computational requirement of the heuristic procedure is $O(\sum_{i=1}^{r} iC_i^{\|Q\|} + |Q|k\sum_{i=1}^{r} C_i^{\|Q\|})$, which is $O((r+k|Q|)|Q|^{r})$ or simply $O(|Q|^{r+1})$.

For low values of $r$ this effort is relatively small, but it increases rapidly with $r$. Note that the computational experiments that we report in Section 5.2 show that we are likely to obtain good results even with low values of $r$.

### 5.2 A Computational Experiment with $OVIP_r$

Our objective in this section is to recommend a reasonable value for $r$. To do so, we solve five instances optimally using the $OVIP$ model. Then we solve each instance using the $OVIP_r$ model with $r = 1$. For those instances for which we do not get the optimal solution using $OVIP_r$ with $r = 1$, we use $OVIP_r$ with $r = 2$. We continue increasing the value of $r$ and proceed in a similar manner until we get optimal solutions for all instances.

These five instances are constructed in the following manner. All instances are on the 17 attribute TPC-H dataset. In instances 1 and 3, each query in $Q$ has 6, 7, or 8 attributes and in instances 2 and 4, each query in $Q$ has 11, 12, or 13 attributes. In these instances the number of attributes for each query is randomly selected between 6 and 13. We also assume that the frequency associated with each query is equal to one. Furthermore, we select the specific queries in instances 1 and 3 from the lower levels of the lattice, and select queries in instances 2 and 4 from the upper levels of the lattice. The results of our experiments are presented in the first five rows of Table 3.

In this table, for each instance we report the number of queries, sizes of the sets $IV'$ and $IV_r$, and the ratio of the cost obtained by the heuristic $(v(OVIP_r))$ to the optimal cost $(v(OVIP))$. Based on our experimental results, we make the following observations:

1. In one instance (instance ID 2), we find the optimal solution using $OVIP_r$ with $r = 1$.
2. In the remaining four instances (instances 1, 3, 4, and 5), we find the optimal solution using $OVIP_r$ with $r = 2$.
3. For each instance, the size of the set $IV_r$ is significantly smaller than the size of the set $IV'$. (On average, the ratio $|IV'|/|IV_r|$ is 160 when $r = 2$.)

13
| Instance ID | Number of queries in Q | r | |IV| | |IVr| |v(OVIP)| CPLEX execution time (sec.) for OVIP | CPLEX execution time (sec.) for OVIPr |
|------------|-----------------------|---|---|---|---|---|---|---|---|
| 1          | 5                     | 1 | 2 | 4663 | 6 | 1.045 | 1.67 | 0.01 |
|            |                       |   |   |      | 16 | 1.000 |       | 0.02 |
| 2          | 5                     | 1 | 2 | 2511 | 6 | 1.000 | 0.74 | 0.01 |
|            |                       |   |   |      | 14 |       |       |     |
| 3          | 10                    | 1 | 2 | 5436 | 11 | 1.059 | 3.16 | 0.01 |
|            |                       |   |   |      | 47 | 1.000 |       | 0.04 |
| 4          | 10                    | 1 | 2 | 986  | 11 | 1.014 | 0.44 | 0.01 |
|            |                       |   |   |      | 42 | 1.000 |       | 0.03 |
| 5          | 15                    | 1 | 2 | 5129 | 15 | 1.048 | 6.44 | 0.01 |
|            |                       |   |   |      | 105| 1.000 |       | 0.09 |
| 6          | 40                    | 1 | 2 | 17422| 41 | -      | -    | 0.34 |
|            |                       |   |   |      | 624| -      | -    | 1.62 |

Table 3. Instances solved for OVIPr.

3. For each instance, the execution time for solving OVIPr with CPLEX is significantly lower than the execution time for solving OVIP with CPLEX. In these instances, the time for building the set IVr is negligible.

Using our heuristic algorithm, we solved a large instance on the 17 attribute TPC-H dataset with forty queries where the number of attributes in each query is between 6 and 13. We assumed that the frequency associated with each query is equal to one. Due to the large size of the corresponding OVIP model, we were not able to solve this instance optimally within the time limit of fifteen minutes. However, using our heuristic with r = 1 and r = 2, we were able to solve it in 0.34 and 1.62 seconds, respectively. Information about this instance is presented in the last two rows (instance ID 6) of Table 3, and the corresponding values of the solutions obtained via OVIPr with r = 1 and r = 2 for this instance are \( v(OVIPr) = 148,514,000 \) and \( v(OVIPr) = 144,020,000 \), respectively. Obviously, we can no longer guarantee that the solution obtained via OVIPr with r = 2 is an optimal solution for the corresponding OVIP.

6 Experimental Comparison with Other Heuristic Procedures

To further evaluate our approaches for solving the warehouse view-selection problem, we have experimentally compared the effectiveness of our exact and inexact methods with that of two other heuristic procedures previously proposed for this problem. One procedure, presented by Harinarayan et al. (1996), is based on the principle of greedy construction; throughout this section we refer to it as procedure HHRU. The second procedure, proposed by Shukla et al. (1998), provides a performance improvement over HHRU while having the same solution-quality guarantees, provided that the problem input satisfy certain restrictions; we refer to this procedure as SDN. This section presents our experimental results. Further, based on an analysis of our experimental comparisons and of the contributions of the view-selection approach of Kalnis et al. (2002), we delineate applicability areas of our exact and inexact methods and of the approaches of Harinarayan et al. (1996), Kalnis et al. (2002), and Shukla et al. (1998) in the space of practically relevant instances of the warehouse view-selection problem.
We note that the approaches of both Harinarayan et al. (1996) and Shukla et al. (1998) are applied to instances in which every node of the view lattice is in the query set $Q$ with unit frequency. To compare our methods with the results presented in those papers, we first carry out an experiment in which we consider only problem instances of this type. We refer to these instances as Group 1 instances. We solve each instance in this group using each of the three approaches $HHRU$, $SDN$, and $OVIP$. (Note that applying $OVIPr$ to such instances would not add any additional insights, since the restricted viewset $IVr$ would be identical to $IV$.) These results are presented in Section 6.1. We then run a second experiment in which we allow the query set $Q$ (that is, the queries with nonnegligible frequencies) to be a relatively small subset of the nodes of the view lattice. We refer to these instances as Group 2 instances. Both procedures $HHRU$ and $SDN$ can be easily adjusted to solve these instances. In this case, we solve each instance of the problem using each of the four procedures $HHRU$, $SDN$, $OVIP$, and $OVIPr$. The results are presented in Section 6.2.

To carry out this comparative study, we developed an independent computer program for each of $HHRU$ and $SDN$. Each program is written in C, uses the same data structures and subroutines as our implementations of $OVIP$ and $OVIPr$, and was run on the same machine that we used for solving the $OVIP$ models, as described in Section 4.

6.1 A Computational Experiment with Group 1 Instances

In this subsection we present experimental results that compare the performance of procedures $HHRU$, $SDN$, and $OVIP$, for the case where the input queries are all the nodes in the lattice, and the frequency of each query is equal to one. The experiments in this section are over six data lattices, which are the 5, 6, and 7 attribute TPC-H data lattices and the 5, 6, and 7 attribute SDSS data lattices. For each data lattice, we set the value of storage space to be the size of the top view plus $\alpha \times$ (sum of the sizes of all of the views in the lattice except for the top view), and set $\alpha = 0.01, 0.05, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7$. Thus, for each data lattice we solved nine problem instances.

Figure 3, which presents the results on the TPC-H data lattices, and Figure 4, which shows the results on the SDSS data lattices, compare the quality of the solutions of $HHRU$ and $SDN$ with the optimal solutions produced by our $OVIP$ procedure. In these figures the horizontal axis represents the value of $\alpha$, and the vertical axis depicts the ratio of the cost of the solution obtained via a heuristic procedure to the corresponding optimal cost, averaged over three instances. For example, when $\alpha = 0.1$ and for the $HHRU$ algorithm, for each of the instances on the 5, 6, and 7 attribute lattices with $\alpha = 0.1$, we measured the cost of the solution obtained using $HHRU$, divided it by the corresponding optimal cost, and took the average of these three ratios. From Figures 3 and 4 we can observe that the overall performance of the $HHRU$ algorithm is better than that of the $SDN$ algorithm. Also, we observe that when the storage space limit is relatively tight ($\alpha = 0.01, 0.05$) or relatively loose ($\alpha = 0.7$), $SDN$ gives solutions whose corresponding costs are close to those obtained via $HHRU$. Moreover, for both $HHRU$ and $SDN$, when the storage space limit is tight ($\alpha = 0.01$), the cost of the solutions obtained are relatively close to the corresponding optimal costs.
In our experiments we also measured the execution time for each instance. We observed that the execution time of the SDN algorithm is significantly less than those for each of OVIP and HHRU. Also, in none of the instances did the OVIP execution time exceed the HHRU execution time.

6.2 A Computational Experiment with Group 2 Instances

In this group of instances we allowed the query set \( Q \) to be a relatively small subset of the nodes of the view lattice. We modified the algorithms of HHRU and SDN to allow for this condition; in addition, we modified SDN to guarantee that it return the (top) raw-data view in each solution. The goal of the experiments was to compare our inexact method \( OVIP_r \) (with \( r = 2 \)) with the modifications of algorithms HHRU and SDN.

In the first set of experiments, whose results are presented in Table 4, the first nine instances are on a 7-attribute TPC-H data lattice. In all of these instances, the number of queries in \( Q \) is five, and the number of attributes of each query is chosen randomly between one and six. The tenth instance is on a 13-attribute TPC-H data lattice. In this instance, there are ten queries, and the number of attributes of each query is a random number between one and twelve. We assume that the frequency of each query in the set \( Q \) equals one. We solved each instance with each of \( OVIP_r \) (with \( r = 2 \)), HHRU, and SDN, and report here the ratios of the costs obtained for each heuristic to the optimal cost.

<table>
<thead>
<tr>
<th>Instance</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>SDN/HHRU</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
</tr>
<tr>
<td>SDN/OVIP</td>
<td>1.053</td>
<td>1.037</td>
<td>1.081</td>
<td>1.000</td>
<td>1.000</td>
<td>1.039</td>
<td>1.031</td>
<td>1.000</td>
<td>1.059</td>
<td>1.005</td>
</tr>
</tbody>
</table>

Table 4. Instances solved on TPC-H data lattices to compare the heuristic algorithms.

We did similar experiments over a 7-attribute SDSS data lattice. We solved nine instances, each with five queries, where the number of attributes in each query was a random number between 1 and 6. Again, we assumed that the frequency of each query equals one. The results are presented in Table 5.

<table>
<thead>
<tr>
<th>Instance</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
</tr>
</thead>
<tbody>
<tr>
<td>SDN/HHRU</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
</tr>
<tr>
<td>SDN/OVIP</td>
<td>1.395</td>
<td>1.000</td>
<td>1.671</td>
<td>1.075</td>
<td>1.000</td>
<td>1.000</td>
<td>1.211</td>
<td>1.012</td>
<td>1.624</td>
</tr>
<tr>
<td>SDN/OVIP</td>
<td>1.000</td>
<td>1.127</td>
<td>1.422</td>
<td>1.000</td>
<td>1.056</td>
<td>1.278</td>
<td>1.209</td>
<td>1.137</td>
<td>1.423</td>
</tr>
</tbody>
</table>

Table 5. Instances solved on SDSS data lattices to compare the heuristic algorithms.

From the results shown in Tables 4 and Table 5 we observe that in some instances the quality of solutions obtained using HHRU is better than the quality obtained using SDN. However, in some other instances the quality of solutions obtained using SDN is better than that obtained using HHRU. Furthermore, we observe that in all the instances we found optimal solutions using \( OVIP_r \) with \( r = 2 \). In addition, in these experiments we
also observed that on this collection of instances the execution time of SDN is significantly lower than that for each of HHRU and OVIPr, and that the execution time of OVIPr is significantly lower than that for HHRU.

We also tried to solve a larger instance on the 17 attribute TPC-H lattice with forty queries using both HHRU and SDN. This is the same instance that we reported earlier as instance 6 in Table 3. As mentioned earlier, we were not able to solve this instance optimally (using OVIP) due to its relatively large size, and the corresponding values obtained via OVIPr with \( r = 1 \) and with \( r = 2 \) are \( v(OVIPr) = 148514000 \) and \( v(OVIPr) = 144020000 \) obtained in 0.34 and 1.62 seconds, respectively. When we tried to solve this instance using HHRU and SDN, HHRU did not terminate in 15 minutes, and SDN terminated in 0.68 seconds with \( v(SDN) = 215866080 \), which is 45% higher than the \( v \) obtained via OVIPr with \( r = 1 \) and 50% higher than the \( v \) obtained via OVIPr with \( r = 2 \).

In our last set of experiments we considered instances where the frequencies associated with queries in the set \( Q \) are not all equal to one. Specifically, we used the Zipfian frequency distribution with the skewness parameter equal to one. We solved five such instances over a 15-attribute TPC-H data lattice, where in each instance the number of elements in the set \( Q \) was equal to ten and the frequency associated with each query was obtained from the Zipfian distribution. Also, we solved five instances on a 7-attribute SDSS data lattice. The number of queries in the latter instances varied between three and five.

For brevity, we refrain from giving details regarding these instances. Our observations on these experiments can be summarized as follows:

1. In all of the instances, OVIPr (with \( r = 2 \)) found the optimal solution.
2. For all the instances, the size of \( IVr \) was significantly smaller than the size of \( IV' \). On average, the ratio \( \frac{|IV'|}{|IVr|} \) was 106 for the instances on the 15-attribute TPC-H data lattice and 8 for the instances on the 7-attribute SDSS data lattice.
3. For each instance, the execution time for solving OVIPr with CPLEX was significantly lower than the execution time for solving OVIP with CPLEX. In these instances, the time for building the set \( IVr \) was negligible. We further observed that this reduction in execution time is more significant for larger instances.

6.3 Applicability Areas for Warehouse View-Selection Methods

In this subsection we delineate applicability areas for our exact and inexact methods and for the approaches of Harinarayan et al. (1996), Kalnis et al. (2002), and Shukla et al. (1998) in the space of practically relevant instances of the warehouse view-selection problem. We begin by briefly summarizing the four view-selection approaches introduced in Kalnis et al. (2002); we refer to those as “randomized-search methods.” These four heuristic approaches are (a) random search, (b) iterative improvement (II) where moves are allowed only if they result in a better solution in the next step, (c) simulated annealing (SA), and (d) a combination of II and SA. In Kalnis et al. (2002) the authors experimentally compare their randomized-search methods with the algorithm HHRU. (In addition, it is mentioned in Kalnis et al. (2002) that for many problem instances, the quality of the solutions obtained by SDN might be significantly lower than that of HHRU.) In the experiments, the four randomized-search
methods are compared with each other, while the HHRU solutions are used to normalize the results. While each randomized-search method is significantly faster than HHRU, it appears that the quality of the HHRU solutions is higher than that of each randomized-search method in many of the experiments reported in Kalnis et al. (2002). Based on these results as reported in Kalnis et al. (2002), we conclude that for the goal of solution quality, HHRU should probably be chosen over the randomized-search methods of Kalnis et al. (2002) wherever HHRU is applicable, i.e., when its execution time is not excessive. At the same time, the approaches of Kalnis et al. (2002) may be a better option for very high-dimensional problem instances, even though they provide no guarantees on solution quality. (We are unable to make conclusions about the solution quality of the approaches of Kalnis et al. (2002), as those have not been experimentally compared with optimal methods, such as our exact method.)

In comparing our exact and inexact methods to the algorithms HHRU and SDN, our conclusions are as follows:

1. Our exact method OVIP/OVIP' is guaranteed to provide optimal solutions:
   (a) for both Group 1 and Group 2 problem instances for view-lattice sizes of up to seven dimensions (cf. the experimental results of Shukla et al. (1998) for SDN, which are given for lattices of sizes up to six dimensions only), and
   (b) for much larger view-lattice sizes (up to at least 17 dimensions) for Group 2 instances, depending on the number/positioning of the input queries with nonzero frequencies.

2. Based on our experimental results, \( r = 2 \) in OVIPr is an appropriate value for the levels of views in the lattice that we should consider.

3. The HHRU approach is never preferable to our proposed exact and inexact methods in solution quality or in runtime efficiency.

4. In terms of the quality of solution, while SDN is comparable to HHRU when the storage-space constraint is "very tight" or "very loose" (see Figures 3 and 4), the quality of the solutions obtained by these algorithms is usually inferior to that for our proposed approaches. Intuitively, SDN picks the views in the order of their sizes. Typically, the views that can answer many queries are of large size and will not be picked by SDN, yet in many cases the size of such views is smaller than the sum of the sizes of the queries that they can answer. Unlike our approaches, SDN does not appear to give good opportunities for such views to be selected.

5. In terms of runtime efficiency, SDN is always the method of choice.

6. Through the construction of instances with special structure, we have shown that in the worst case, the solution value obtained by HHRU (and hence by SDN) can be arbitrary far from the optimal value (see Asgharzadeh Talebi et al. (2006)).
Bibliography


### TPC-H Tables

<table>
<thead>
<tr>
<th>Name</th>
<th>Size (bytes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lineitem</td>
<td>2,147,483,547</td>
</tr>
<tr>
<td>Part</td>
<td>1,193,906</td>
</tr>
<tr>
<td>Supplier</td>
<td>14,188,544</td>
</tr>
<tr>
<td>PartSupp</td>
<td>5,830,541</td>
</tr>
<tr>
<td>Customer</td>
<td>244,883,456</td>
</tr>
<tr>
<td>Orders</td>
<td>482,877,440</td>
</tr>
<tr>
<td>Nation1</td>
<td>2,103</td>
</tr>
<tr>
<td>Nation2</td>
<td>2,103</td>
</tr>
<tr>
<td>Region</td>
<td>396</td>
</tr>
</tbody>
</table>

**Fig. 1.** Sizes of the TPC-H tables.

### SDSS Tables

<table>
<thead>
<tr>
<th>Name</th>
<th>Size (bytes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SpecObjAll</td>
<td>200,851,705</td>
</tr>
<tr>
<td>PhotoObj</td>
<td>38,206,539</td>
</tr>
<tr>
<td>Plate</td>
<td>69,035</td>
</tr>
<tr>
<td>Segment</td>
<td>621</td>
</tr>
<tr>
<td>Field</td>
<td>919</td>
</tr>
<tr>
<td>Neighbors</td>
<td>1,321</td>
</tr>
</tbody>
</table>

**Fig. 2.** Sizes of the SDSS tables.

### Average Deviation from Optimal for TPC-H

**Fig. 3.** Comparison of HHRU, SDN, and OVIP for TPC-H data lattices (OVIP provides the optimal solutions).

### Average Deviation from Optimal for SDSS

**Fig. 4.** Comparison of HHRU, SDN, and OVIP for SDSS data lattices (OVIP provides the optimal solutions).