

**A COMPREHENSIVE, MATRIX FREE ALGORITHM FOR  
ANALYSIS OF VARIANCE**

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#12/2

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SAMPLE PROBLEMS

The following simple examples have been prepared principally to illustrate the different features of the program - options, model specification, computations, output - in many different combinations. They do not necessarily represent the most likely use of the program in analyzing each set of data. The unbalanced data sets used in the first two examples were taken from Searle [19]. The first data set is used in Chapter 7 to illustrate the two-way classification with interaction. The second is used in Chapter 6 to illustrate the two-way nested classification. The third example involving balanced data with 2 crossed factors, 2 nested factors, and interaction terms appears in Appendix B of [12]. The final example, a Latin square, was extracted from Statistical Methods by G. N. Snedecor (5th Edition, page 308). These sample problems have all been run in batch mode.

```
F(A,B) L(I(3),J(4))
DATA FORMAT AND INPUT DATA-
(IX,2I2,F4.0)
1 1 8.
1 1 13.
1 1 9.
1 3 12.
1 4 7.
1 4 11.
2 1 6.
2 1 12.
2 2 12.
2 2 14.
3 2 9.
3 2 7.
3 3 14.
3 3 16.
3 4 10.
3 4 14.
3 4 11.
3 4 13.
```

O C O.  
 C(S(8),2,A,C,R)  
 CELL SUMS, FREQUENCIES, AND MEANS-

CELL	SUM	FREQ.	MEAN
1	C.30000000D 02	3.	0.10000000D 02
2	(MISSING CELL)		
3	C.12000000D 02	1.	0.12000000D 02
4	C.18000000D 02	2.	0.50000000D 01
5	C.18000000D 02	2.	0.90000000D 01
6	C.26000000D 02	2.	0.13000000D 02
7	(MISSING CELL)		
8	(MISSING CELL)		
9	(MISSING CELL)		
10	C.16000000D 02	2.	0.80000000D 01
11	C.30000000D 02	2.	0.15000000D 02
12	C.48000000D 02	4.	0.12000000D 02

CLASSIFICATION SUMS, FREQUENCIES, AND MEANS-

I.

1	C.60000000D 02	6.	0.10000000D 02
2	C.44000000D 02	4.	0.11000000D 02
3	C.94000000D 02	8.	0.11750000D 02

J.

1	C.48000000D 02	5.	0.96000000D 01
2	C.42000000D 02	4.	0.10500000D 02
3	C.42000000D 02	3.	0.14000000D 02
4	C.66000000D 02	6.	0.11000000D 02

..  
 1 0.19800000D 03 18. 0.11000000D 02  
 OPTICS- S= 8, T=0.0500, I=100, R=1, V=0, G=0, P=0  
 M+A(I)+E(J)+AB(IJ)

E/R LIST-

4	3	2	1
THE RANK OF THE M DESIGN MATRIX IS 8			
ITERATION 1, SSR(FULL MDEL)=	0.22600000D 04,		
SSE(FULL MDEL)=	0.56000000D 02		

H AB(IJ)  
 E/R LIST-

-4	3	2	1
ITERATION 0, TRACE=	4.000000000		
ITERATION 1, TRACE=	4.875000000		
ITERATION 2, TRACE=	5.543113426		
ITERATION 3, TRACE=	5.886175169		
ITERATION 4, TRACE=	5.585797608		

THE RANK OF THE F DESIGN MATRIX IS 6  
 FROM RANK COMPUTATIONS- DF(NUM)= 2, DF(DEN)= 10

ITERATION 1, SSRH=	0.1415687D 04
ITERATION 2, SSRH=	0.18605379D 04
ITERATION 3, SSRH=	0.20375067D 04
ITERATION 4, SSRH=	0.21180574D 04
ITERATION 5, SSRH=	0.21566817D 04
ITERATION 6, SSRH=	0.21811740D 04
ITERATION 7, SSRH=	0.21947132D 04
ITERATION 8, SSRH=	0.22034435D 04
ITERATION 9, SSRH=	0.22093714D 04
ITERATION 10, SSRH=	0.22135449D 04
ITERATION 11, SSRH=	0.22165550D 04
ITERATION 11, F=	3.879, PROB(F) .GT. 0.0559 VS. F LEVEL OF 0.0500
SSR(REDUCED MDEL)=	0.22165550D 04

H A(I)  
 E/R LIST-

4 -3 2 1  
 ITERATION 0. TRACE= 6.66666667  
 ITERATION 1. TRACE= 7.09722222  
 ITERATION 2. TRACE= 7.567604784  
 ITERATION 3. TRACE= 7.886480000  
 ITERATION 4. TRACE= 7.989797654  
 THE RANK OF THE F DESIGN MATRIX IS 8  
 FROM RANK COMPUTATIONS- DF(NUM)= 0, DF(DEN)= 10  
 H E(J)  
 E/R LIST-

4 3 -2 1  
 ITERATION 0. TRACE= 6.00000000  
 ITERATION 1. TRACE= 6.66666667  
 ITERATION 2. TRACE= 7.407407407  
 ITERATION 3. TRACE= 7.882944673  
 ITERATION 4. TRACE= 7.995432683  
 THE RANK OF THE H DESIGN MATRIX IS 8  
 FROM RANK COMPUTATIONS- DF(NUM)= 0, DF(DEN)= 10  
 O(P)

OPTIONS- S= 8, T=0.0500, I=100, R=1, V=0, G=0, P=1  
 H AB(IJ)  
 E/R LIST-

-4 3 2 1  
 ITERATION 0. TRACE= 4.00000000  
 ITERATION 1. TRACE= 4.67500000  
 ITERATION 2. TRACE= 5.543113426  
 ITERATION 3. TRACE= 5.886175169  
 ITERATION 4. TRACE= 5.989797608

THE RANK OF THE F DESIGN MATRIX IS 6  
 FROM RANK COMPUTATIONS- DF(NUM)= 2, DF(DEN)= 10

ITERATION 1. SSRH= 0.14159687D 04  
 ITERATION 2. SSRH= 0.18605379D 04  
 ITERATION 3. SSRH= 0.20375067D 04  
 ITERATION 4. SSRH= 0.21180574D 04  
 ITERATION 5. SSRH= 0.21586817D 04  
 ITERATION 6. SSRH= 0.21811740D 04  
 ITERATION 7. SSRH= 0.21947132D 04  
 ITERATION 8. SSRH= 0.22034435D 04  
 ITERATION 9. SSRH= 0.22093714D 04  
 ITERATION 10. SSRH= 0.22135449D 04  
 ITERATION 11. SSRH= 0.22165550D 04  
 ITERATION 12. SSRH= 0.22187605D 04  
 ITERATION 13. SSRH= 0.22203929D 04  
 ITERATION 14. SSRH= 0.22216091D 04  
 ITERATION 15. SSRH= 0.22225191D 04  
 ITERATION 16. SSRH= 0.22232018D 04  
 ITERATION 17. SSRH= 0.22237150D 04  
 ITERATION 18. SSRH= 0.22241013D 04  
 ITERATION 19. SSRH= 0.22243922D 04  
 ITERATION 20. SSRH= 0.22246116D 04  
 ITERATION 21. SSRH= 0.22247769D 04  
 ITERATION 22. SSRH= 0.22249017D 04  
 ITERATION 23. SSRH= 0.22249958D 04  
 ITERATION 24. SSRH= 0.22250669D 04  
 ITERATION 25. SSRH= 0.22251205D 04  
 ITERATION 25. F= 3.114, PROB(F) .GT. 0.0880 VS. F LEVEL OF 0.0500  
 SSR(REDUCE MODEL)= 0.22251205D 04

C(Z,V,G)  
 OPTIONS- S= 8, T=0.0500, I=100, R=1, V=1, G=1, P=1  
 M+A(I)+E(J)

THE RANK OF THE N DESIGN MATRIX IS 6  
ITERATION 64, SSR(FULL MODEL)= 0.22252857D 04,  
SSE(FULL MODEL)= 0.90714289D 02

ESTIMATES OF EXPECTED CELL MEANS-

CELL	ESTIMATED MEAN
1	C.87146775D C1
2	C.88574223D 01 (MISSING CELL)
3	C.13285080D C2
4	C.10285360D 02
5	C.10928171D C2
6	C.11070915D 02
7	C.15498573D 02 (MISSING CELL)
8	C.12498853D 02 (MISSING CELL)
9	C.97864389D 01 (MISSING CELL)
10	C.99291833D 01
11	C.14356841D 02
12	C.11357121D 02

G-INVERSE SOLUTION-

A

1	-C.10950847D 01
2	C.11184084D 01
3	-C.23323708D-C1

B

1	-C.15709570D C1
2	-C.14282126D 01
3	C.29994450D C1
4	-C.27535484D-C3

1	C.11380720C C2
---	----------------

F(A,B) L(1(2),J(3))  
DATA FORMAT AND INPUT DATA-  
(IX,2I2,F4.0)

1	1	5.
1	2	8.
1	2	10.
1	2	9.
2	1	8.
2	1	10.
2	2	6.
2	2	2.
2	2	1.
2	2	3.
2	3	3.
2	3	7.
0	0	0.

C(Z,C,P,V,G)

CLASSIFICATION SUMS, FREQUENCIES, AND MEANS-

I.

1	C.32000000D 02	4.	C.80000000D 01
2	C.40000000D 02	8.	C.50000000D 01

J

1	C.25000000D 02	3.	C.76666667D 01
2	C.39000000D 02	7.	C.55714286D 01
3	C.10000000D 02	2.	C.50000000D 01

\*\*

1	C.72000000D 02	12.	C.60000000D 01
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OPTICS- S= 8, T=0.0500, I=100, R=1, V=0, G=0, P=0

M+A(I)+E(IJ)

E/R LIST-

2 3 2 1  
THE RANK OF THE M DESIGN MATRIX IS 5  
ITERATION 1, SSR(FULL MDEL)= 0.51600000 03,  
SSE(FULL MDEL)= 0.26000000 02

H B(IJ)  
E/R LIST-

-2 3 -2 1  
THE RANK OF THE H DESIGN MATRIX IS 2  
FROM RANK COMPUTATIONS- DF(NUM)= 3, DF(DEN)= 7  
ITERATION 1, SSRH= 0.45600000 03  
ITERATION 1, F= 5.385\*, PROB(F) .GT. 0.0311 VS. F LEVEL OF 0.0500  
SSR(REduced MDEL)= 0.45600000 03

H A(I)  
E/R LIST-

2 -3 -2 1  
ITERATION 0, TRACE= 4.16666667  
ITERATION 1, TRACE= 4.30555556  
ITERATION 2, TRACE= 4.517746914  
ITERATION 3, TRACE= 4.767431561  
ITERATION 4, TRACE= 4.945912107

THE RANK OF THE H DESIGN MATRIX IS 5  
FROM RANK COMPUTATIONS- DF(NUM)= 0, DF(DEN)= 7  
O(Z,V,G)

OPTICS- S= 8, T=0.0500, I=100, R=1, V=1, G=1, P=0  
M+A(I)+E(IJ)

THE RANK OF THE M DESIGN MATRIX IS 5  
ITERATION 1, SSR(FULL MDEL)= 0.51600000 03,  
SSE(FULL MDEL)= 0.26000000 02

ESTIMATES OF EXPECTED CELL MEANS-

CELL	ESTIMATED MEAN
1	0.50000000 01
2	0.90000000 01
3	0.00000000 00 (MISSING CELL)
4	0.50000000 01
5	0.30000000 01
6	0.50000000 01

G-INVERSE SOLUTION-

B  
1 0.33333333D 00  
2 0.43333333D 01  
3 -0.46666667D 01  
4 0.33333333D 01  
5 -0.26666667D 01  
6 -0.66666667D 00

A  
1 -0.50000000D 00  
2 0.50000000D 00

1 0.51666667D 01  
C(G)  
OPTICS- S= 8, T=0.0500, I=100, R=1, V=1, G=0, P=0  
M+A(I)

THE RANK OF THE M DESIGN MATRIX IS 2  
ITERATION 1, SSR(FULL MDEL)= 0.45600000 03,  
SSE(FULL MDEL)= 0.86000000 02

ESTIMATES OF EXPECTED CELL MEANS-

CELL	ESTIMATED MEAN
1	0.80000000 01
2	0.80000000 01
3	0.80000000 01 (MISSING CELL)

```
4 C.50000000D 01
5 C.50000000D 01
6 C.50000000D 01
```

```
F A(I)
THE RANK OF THE F DESIGN MATRIX IS 1
FROM RANK COMPUTATIONS- DF(NUM)= 1, DF(DEN)= 10
ITERATION 1, F= 2.791, PROB(F) .GT. 0.1231 VS. F LEVEL OF 0.0500
SSR(REduced MODEL)= 0.43200000D 03
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```
F(A,B,C,D) L(I(2),J(2),K(2),L(2))
DATA FORMAT AND INPUT DATA-
```

```
(IX,4I2,FS,2)
1 1 1 1 6.01
1 1 1 1 5.95
1 1 1 1 5.85
1 1 1 1 6.43
1 1 1 2 6.35
1 1 1 2 7.00
1 1 1 2 5.50
1 1 1 2 6.00
1 1 2 1 6.00
1 1 2 1 7.15
1 1 2 1 7.35
1 1 2 1 7.20
1 1 2 2 7.10
1 1 2 2 6.15
1 1 2 2 7.50
1 1 2 2 7.15
1 2 1 1 5.87
1 2 1 1 6.18
1 2 1 1 5.90
1 2 1 1 6.33
1 2 1 2 5.64
1 2 1 2 5.55
1 2 1 2 6.03
1 2 1 2 6.64
1 2 2 1 6.08
1 2 2 1 6.17
1 2 2 1 6.13
1 2 2 1 7.62
1 2 2 2 6.55
1 2 2 2 5.40
1 2 2 2 7.20
1 2 2 2 6.66
2 1 1 1 6.00
2 1 1 1 5.60
2 1 1 1 6.60
2 1 1 1 5.54
2 1 1 2 5.50
2 1 1 2 5.45
2 1 1 2 6.00
2 1 1 2 6.05
2 1 2 1 6.25
2 1 2 1 5.75
2 1 2 1 5.60
2 1 2 1 6.40
2 1 2 2 6.17
2 1 2 2 6.33
2 1 2 2 6.32
2 1 2 2 5.57
```

2 2 1 1 6.30  
 2 2 1 1 6.35  
 2 2 1 1 7.00  
 2 2 1 1 9.05  
 2 2 1 2 6.55  
 2 2 1 2 5.90  
 2 2 1 2 5.67  
 2 2 1 2 6.30  
 2 2 2 1 5.30  
 2 2 2 1 6.10  
 2 2 2 1 6.50  
 2 2 2 1 6.55  
 2 2 2 2 6.10  
 2 2 2 2 6.10  
 2 2 2 2 6.30  
 2 2 2 2 6.75  
 C C C C 0.00

C(Z,A,C,R,V)

CELL SUMS, FREQUENCIES, AND MEANS-

CELL	SUM	FREQ.	MEAN
1	0.242400000	02	4. 0.606000000 01
2	0.252500000	02	4. 0.631250000 01
3	0.277000000	02	4. 0.692500000 01
4	0.275000000	02	4. 0.697500000 01
5	0.242800000	02	4. 0.607000000 01
6	0.240600000	02	4. 0.601500000 01
7	0.260000000	02	4. 0.650000000 01
8	0.258100000	02	4. 0.745250000 01
9	0.239400000	02	4. 0.598500000 01
10	0.230000000	02	4. 0.575000000 01
11	0.240000000	02	4. 0.600000000 01
12	0.247500000	02	4. 0.619750000 01
13	0.287000000	02	4. 0.717500000 01
14	0.244200000	02	4. 0.610500000 01
15	0.248500000	02	4. 0.621250000 01
16	0.252500000	02	4. 0.631250000 01

CLASSIFICATION SUMS, FREQUENCIES, AND MEANS-

IJK.

1	0.454900000	02	8. 0.618625000 01
2	0.556000000	02	8. 0.695000000 01
3	0.483400000	02	8. 0.604250000 01
4	0.558100000	02	8. 0.697625000 01
5	0.469400000	02	8. 0.586750000 01
6	0.487500000	02	8. 0.609875000 01
7	0.531200000	02	8. 0.664000000 01
8	0.501000000	02	8. 0.626250000 01

IJ.L

1	0.519400000	02	8. 0.649250000 01
2	0.531500000	02	8. 0.664375000 01
3	0.502800000	02	8. 0.628500000 01
4	0.538700000	02	8. 0.673375000 01
5	0.475400000	02	8. 0.599250000 01
6	0.477500000	02	8. 0.597375000 01
7	0.535500000	02	8. 0.669375000 01
8	0.496700000	02	8. 0.620875000 01

IJ..

1	0.105090000	03	16. 0.656812500 01
2	0.104150000	03	16. 0.650937500 01
3	0.557300000	02	16. 0.598312500 01
4	0.102220000	03	16. 0.645125000 01



I.KL					
	1	C.48520000D	02	8.	0.60650000D 01
	2	C.49310000D	02	8.	0.61637500D 01
	3	C.53700000D	02	8.	0.67125000D 01
	4	0.57710000D	02	8.	0.72137500D 01
	5	C.52640000D	02	8.	0.65800000D 01
	6	C.47420000D	02	8.	0.59275000D 01
	7	0.48850000D	02	8.	0.61062500D 01
	8	C.50040000D	02	8.	0.62550000D 01
I.K.					
	1	C.97830000D	02	16.	0.61143750D 01
	2	C.11141000D	03	16.	0.69631250D 01
	3	C.10006000D	03	16.	0.62537500D 01
	4	0.58890000D	02	16.	0.61806250D 01
I..L					
	1	C.10222000D	03	16.	0.63867500D 01
	2	0.10702000D	03	16.	0.66887500D 01
	3	C.10149000D	03	16.	0.63431250D 01
	4	0.57460000D	02	16.	0.60912500D 01
I...					
	1	C.20924000D	03	32.	0.65387500D 01
	2	C.15895000D	03	32.	0.62171875D 01
.JKL					
	1	0.48180000D	02	8.	0.60225000D 01
	2	C.48250000D	02	8.	0.60312500D 01
	3	C.51700000D	02	8.	0.64625000D 01
	4	0.52690000D	02	8.	0.65862500D 01
	5	C.52980000D	02	8.	0.66225000D 01
	6	0.48480000D	02	8.	0.60600000D 01
	7	C.50850000D	02	8.	0.63552500D 01
	8	C.55060000D	02	8.	0.68825000D 01
.JK.					
	1	C.56430000D	02	16.	0.60268750D 01
	2	0.10439000D	03	16.	0.65243750D 01
	3	C.10146000D	03	16.	0.63412500D 01
	4	0.10591000D	03	16.	0.66193750D 01
.J..L					
	1	C.55880000D	02	16.	0.62425000D 01
	2	C.10094000D	03	16.	0.63087500D 01
	3	C.10383000D	03	16.	0.64893750D 01
	4	0.10354000D	03	16.	0.64712500D 01
.J..					
	1	C.20082000D	03	32.	0.62756250D 01
	2	0.20737000D	03	32.	0.64803125D 01
..KL					
	1	C.10116000D	03	16.	0.63225000D 01
	2	0.96730000D	02	16.	0.60456250D 01
	3	C.10255000D	03	16.	0.64093750D 01
	4	C.10775000D	03	16.	0.67343750D 01
..K.					
	1	C.19789000D	03	32.	0.61840625D 01
	2	0.21030000D	03	32.	0.65718750D 01
...L					
	1	C.20371000D	03	32.	0.63659375D 01
	2	C.20448000D	03	32.	0.63900000D 01
....					
	1	0.40819000D	03	64.	0.63779688D 01

OPTICS- S= 8, T=0.0500, I=100, R=0, V=0, G=0, P=0  
M+A(I)+B(IJ)+C(K)+AC(IK)+EC(IJK)/  
+D(IJL)+CD(IJKL)

E/R LIST-  
 4 7 2 5 4 11 2 9 4 7 2 5 4 3 2 1  
 ITERATION 1. SSR(FULL MODEL)= 0.26179143D 04.  
 SSE(FULL MODEL)= 0.19523775D 02

H A(I)  
 E/R LIST-  
 4 7 2 5 4 11 2 -9 4 7 2 5 4 3 2 1  
 FROM RANK COMPUTATIONS- DF(NUM)= 1, DF(DEN)= 48  
 ITERATION 1. SSRH= 0.26162599D 04  
 ITERATION 1, F= 4.068\*, PROB(F) .GT. 0.0466 VS. F LEVEL OF 0.0500  
 SSR(REduced MODEL)= 0.26162599D 04

H B(IJ)  
 E/R LIST-  
 4 7 2 -5 4 11 2 9 4 7 2 -5 4 3 2 1  
 FROM RANK COMPUTATIONS- DF(NUM)= 2, DF(DEN)= 48  
 ITERATION 1. SSFH= 0.26161336D 04  
 ITERATION 1, F= 2.189, PROB(F) .GT. 0.1212 VS. F LEVEL OF 0.0500  
 SSR(REduced MODEL)= 0.26161336D 04

C(2)  
 OPTICNS- S= 8, T=0.0500, I=100, R=0, V=0, G=0, P=0  
 H C(K)  
 FROM RANK COMPUTATIONS- DF(NUM)= 1, DF(DEN)= 48  
 ITERATION 1, F= 5.916\*, PROB(F) .GT. 0.0178 VS. F LEVEL OF 0.0500  
 SSR(REduced MODEL)= 0.26155079D 04

H AC(IK)  
 FROM RANK COMPUTATIONS- DF(NUM)= 1, DF(DEN)= 48  
 ITERATION 1, F= 8.358\*, PROB(F) .GT. 0.0059 VS. F LEVEL OF 0.0500  
 SSR(REduced MODEL)= 0.26145149D 04

H BC(IJK)  
 FROM RANK COMPUTATIONS- DF(NUM)= 2, DF(DEN)= 48  
 ITERATION 1, F= 0.982, PROB(F) .GT. 0.3837 VS. F LEVEL OF 0.0500  
 SSR(REduced MODEL)= 0.26171154D 04

H D(IJL)  
 FROM RANK COMPUTATIONS- DF(NUM)= 4, DF(DEN)= 48  
 ITERATION 1, F= 1.131, PROB(F) .GT. 0.3534 VS. F LEVEL OF 0.0500  
 SSR(REduced MODEL)= 0.26160750D 04

H CD(IJKL)  
 FROM RANK COMPUTATIONS- DF(NUM)= 4, DF(DEN)= 48  
 ITERATION 1, F= 1.605, PROB(F) .GT. 0.1873 VS. F LEVEL OF 0.0500  
 SSR(REduced MODEL)= 0.26153023D 04

D(V,G)  
 OPTICNS- S= 8, T=0.0500, I=100, R=0, V=1, G=1, P=0  
 M+A(I)+C(K)+AC(IK)  
 ITERATION 1. SSR(FULL MODEL)= 0.26108833D 04.  
 SSE(FULL MODEL)= 0.26554806D 02

ESTIMATES OF EXPECTED CELL MEANS-  
 CELL ESTIMATED MEAN  
 1 0.61143750D 01  
 2 0.61143750D 01  
 3 0.69631250D 01  
 4 0.69631250D 01  
 5 0.61143750D 01  
 6 0.61143750D 01  
 7 0.69631250D 01  
 8 0.69631250D 01  
 9 0.62537500D 01  
 10 0.62537500D 01  
 11 0.61806250D 01  
 12 0.61806250D 01  
 13 0.62537500D 01

14 C.62537500D 01  
 15 C.61806250D C1  
 16 C.61806250D C1

G-INVERSE SOLUTION-

AC  
 1 -0.23046E75D 00  
 2 0.23046E75D 00  
 3 0.23046E75D 00  
 4 -0.23046E75D 00

A  
 1 C.16078125D 00  
 2 -0.16078125D 00

C  
 1 -0.19350625D 00  
 2 C.19350625D 00

1 C.63775688D 01

F(R,C,T) L(1(3),J(3),K(3))  
 DATA FORMAT AND INPUT DATA-

(1X,3I2,F6.0)

1 1 1 60E.  
 1 2 2 885.  
 1 3 3 940.  
 2 1 2 715.  
 2 2 3 10E7.  
 2 3 1 766.  
 3 1 3 844.  
 3 2 1 711.  
 3 3 2 832.  
 0 0 0 0.

C(2,R,V,G)

OPTICS- S= 8, T=C.0500, I=100, R=1, V=0, G=0, P=0  
 M+R(I)+C(J)+T(K)

E/R LIST-

C	0	0	5	0	3	2	1
VECTOR	1.	ITERATICS	6.	TRACE=			0.771783175
VECTOR	5.	ITERATICS	6.	TRACE=			1.543566350
VECTOR	9.	ITERATICS	6.	TRACE=			2.315349525
VECTOR	11.	ITERATICS	6.	TRACE=			3.087132699
VECTOR	15.	ITERATICS	6.	TRACE=			3.858915874
VECTOR	16.	ITERATICS	6.	TRACE=			4.630699049
VECTOR	21.	ITERATICS	6.	TRACE=			5.402482224
VECTOR	22.	ITERATICS	6.	TRACE=			6.174265399
VECTOR	26.	ITERATICS	6.	TRACE=			6.946048574

THE RANK OF THE M DESIGN MATRIX IS 7

ITERATION 1. SSRM= 0.34562651D 07  
 ITERATION 2. SSRM= 0.49923829D 07  
 ITERATION 3. SSRM= 0.56751019D 07  
 ITERATION 4. SSRM= 0.59785326D 07  
 ITERATION 5. SSRM= 0.61133906D 07  
 ITERATION 6. SSRM= 0.61733276C 07  
 ITERATION 7. SSRM= 0.61995662D 07  
 ITERATION 8. SSRM= 0.62118056D 07  
 ITERATION 9. SSRM= 0.62170675D 07  
 ITERATION 10. SSRM= 0.62194062D 07  
 ITERATION 11. SSRM= 0.62204456D 07  
 ITERATION 12. SSRM= 0.62205075D 07  
 ITERATION 13. SSRM= 0.62211129D 07  
 ITERATION 14. SSRM= 0.62212041D 07

ITERATION 15, SSRM= 0.62212447D 07  
 ITERATION 16, SSRM= 0.62212627D 07  
 ITERATION 17, SSRM= 0.62212707D 07  
 ITERATION 18, SSRM= 0.62212743D 07  
 ITERATION 19, SSRM= 0.62212758D 07  
 ITERATION 20, SSRM= 0.62212765D 07  
 ITERATION 21, SSRM= 0.62212769D 07  
 ITERATION 22, SSRM= 0.62212770D 07  
 ITERATION 23, SSRM= 0.62212771D 07  
 ITERATION 24, SSRM= 0.62212771D 07  
 ITERATION 25, SSRM= 0.62212771D 07  
 ITERATION 26, SSRM= 0.62212771D 07  
 ITERATION 27, SSRM= 0.62212771D 07  
 ITERATION 27, SSR(FULL MODEL)= 0.62212771D 07,  
 SSE(FULL MODEL)= 0.48428908D 04

H R(I)  
 E/R LIST-

0 0 0 -5 0 3 2 1  
 THE RANK OF THE F DESIGN MATRIX IS 5  
 FROM RANK COMPUTATIONS- DF(NUM)= 2, DF(DEN)= 2  
 ITERATION 1, SSRH= 0.62153769D 07  
 ITERATION 1, F= 1.218 , PROB(F) .GT. 0.4509 VS. F LEVEL OF 0.0500  
 SSR(REduced MODEL)= 0.62153769D 07

F C(J)  
 E/R LIST-

0 0 0 5 0 -3 2 1  
 THE RANK OF THE F DESIGN MATRIX IS 5  
 FROM RANK COMPUTATIONS- DF(NUM)= 2, DF(DEN)= 2  
 ITERATION 1, SSRH= 0.61740636D 07  
 ITERATION 1, F= 9.749 , PROB(F) .GT. 0.0996 VS. F LEVEL OF 0.0500  
 SSR(REduced MODEL)= 0.61740636D 07

F T(K)  
 E/R LIST-

0 0 0 5 0 3 -2 1  
 THE RANK OF THE H DESIGN MATRIX IS 5  
 FROM RANK COMPUTATIONS- DF(NUM)= 2, DF(DEN)= 2  
 ITERATION 1, SSRH= 0.61178409D 07  
 ITERATION 1, F= 21.358 , PROB(F) .GT. 0.0541 VS. F LEVEL OF 0.0500  
 SSR(REduced MODEL)= 0.61178409D 07

E